
**Fine ceramics (advanced ceramics,
advanced technical ceramics) —
Determination of thermal diffusivity of
monolithic ceramics by laser flash
method**

*Céramiques techniques — Détermination de la diffusivité thermique des
céramiques monolithiques par la méthode flash laser*



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Foreword

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Fine ceramics (advanced ceramics, advanced technical ceramics) — Determination of thermal diffusivity of monolithic ceramics by laser flash method

1 Scope

This International Standard specifies the test method for the determination of thermal diffusivity from room temperature to 1700 K by the laser flash method for homogeneous monolithic ceramics with porosity less than 10 %.

2 Normative references

The following referenced documents are indispensable for the application of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

ISO 3611, *Micrometer callipers for external measurement*

3 Terms and definitions

For the purposes of this document, the following terms and definitions apply.

3.1

thermal diffusivity

thermal conductivity divided by the product of specific heat capacity and density

3.2

thermal conductivity

density of heat flow rate divided by temperature gradient under steady state condition

3.3

specific heat capacity

heat capacity per unit mass

3.4

pulse width

τ_p

full width of half maximum (FWHM) which is the time duration when the laser pulse intensity is larger than the half of its maximum value on time basis

3.5

centroid of laser pulse

chronological centroid of laser light energy

3.6

spatial energy distribution of pulse heating

energy density of the laser beam incident at each point on the front face of the specimen

3.7

transient temperature curve

transient temperature change of the rear face of the specimen after the light pulse heating

3.8

transient radiance curve

transient change of the spectral radiance from the rear face of the specimen after the light pulse heating

NOTE It should be noted that the observed transient curve is proportional to the change of the spectral radiance rather than the change of temperature when a radiation thermometer or a radiation detector is used to observe the transient temperature rise of the specimen after the light pulse heating.

3.9

maximum temperature rise

$\Delta T_{\max}$

difference between the steady temperature before the pulse heating and the maximum temperature of the rear face of the specimen after the pulse heating

NOTE See Figure 1.

3.10

half rise-time

$t_{1/2}$

time until $\Delta T_{\max}/2$ is attained from the pulse heating

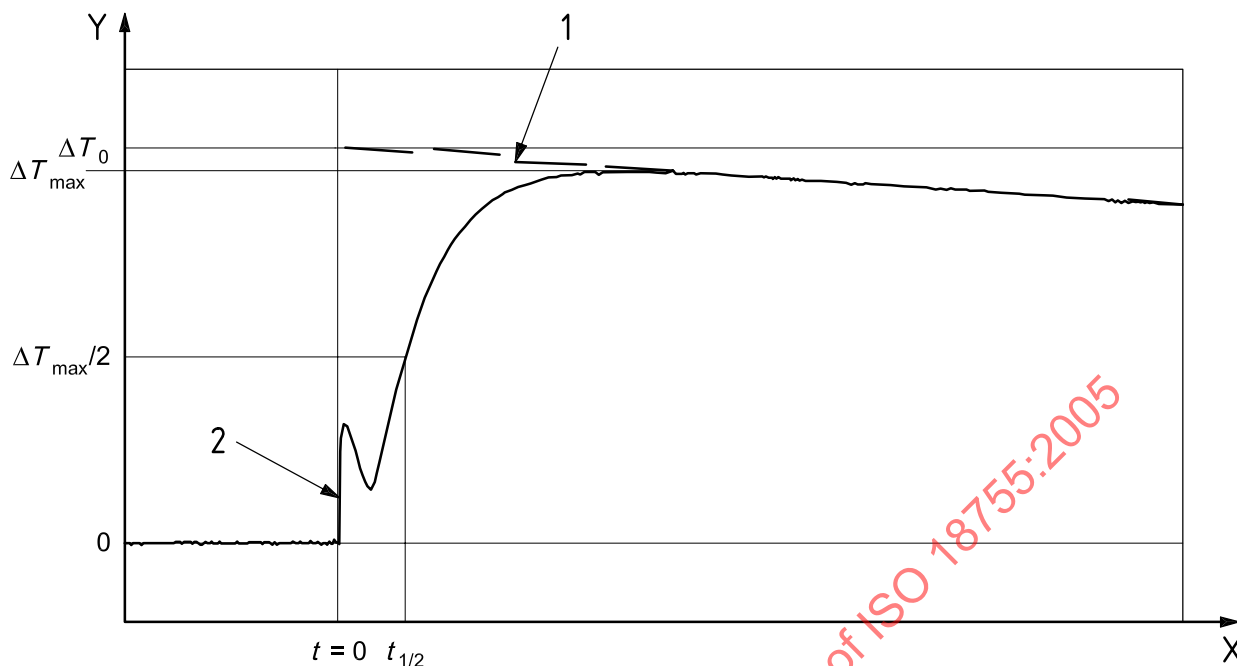
3.11

characteristic time of heat loss

τ_c

time of heat loss determined when the cooling region is fitted with an exponential function, $\Delta T_0 \exp(-t/\tau_c)$

NOTE See Figure 1.



Key

X: time

Y: temperature rise

1 exponential function $[\Delta T_0 \exp(-t/\tau_c)]$

2 initial noise

Figure 1 —Transient temperature curve of the rear face of the specimen after a light pulse heating onto the front face of the specimen

3.12

extrapolated temperature rise

ΔT_0

temperature rise determined when the cooling region is fitted with an exponential function, $\Delta T_0 \exp(-t/\tau_c)$

3.13

initial noise superimposed on transient temperature curve

initial spike and/or hump superimposed on the initial part of the transient temperature curve, due to transmitted and/or scattered light from the heating laser pulse and/or electrically induced noise associated with the laser pulse discharge

3.14

homogeneity of specimen

degree of homogeneity of local thermal diffusivity over the specimen

4 Apparatus

The apparatus shall be designed for obtaining the thermal diffusivity from the transient temperature curve of the rear face of a specimen after the laser pulse is irradiated onto the front face of the specimen, and shall consist of the following principal components as shown in Figure 2.

4.1 Specimen holder

The specimen holder shall hold the specimen stable, with minimum thermal contact, and shall be designed to suppress stray lights from the laser beam being transmitted to the transient detector.

A diaphragm with aperture diameter slightly larger than the specimen diameter should be placed close to the front face of the specimen, and another diaphragm with aperture diameter smaller than the specimen diameter and larger than the target size of radiative detection should be placed close to the rear face of the specimen.

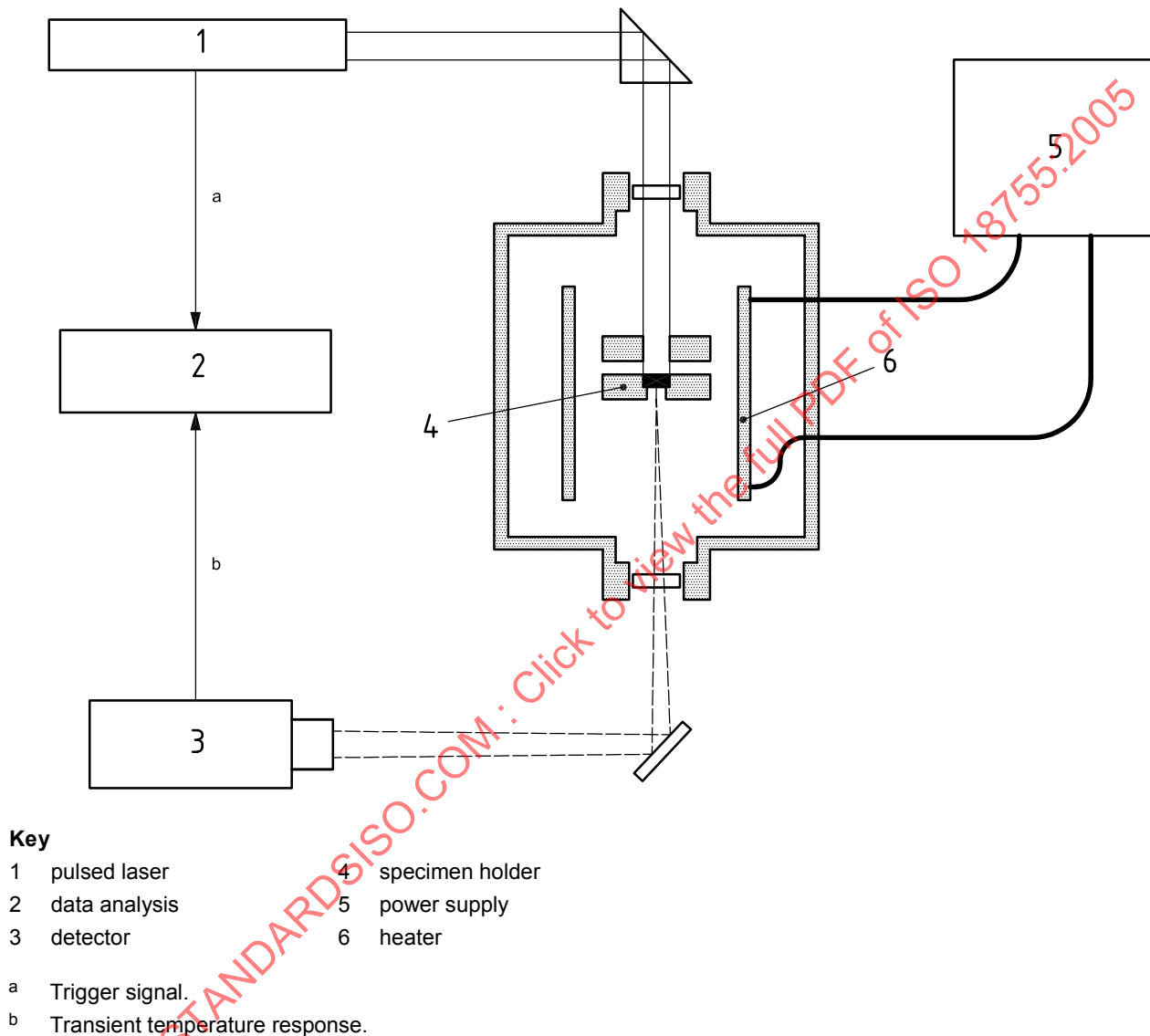


Figure 2 — Block diagram of laser flash apparatus for measuring thermal diffusivity

4.2 Pulse laser

The pulse laser shall be capable of emitting the light pulse with pulse duration preferably shorter than 1,0 ms in full width at half maximum (FWHM). The specimen should be irradiated uniformly by the light pulse.

When a pulse laser is used for the light pulse, the direct beam profile is often irregular because of multi-mode oscillation. In this case, the beam should be converted to a uniform beam using beam-homogenizing optics.

4.3 Thermometer for measuring steady-state temperature of the specimen

The steady-state temperature of the specimen before pulse heating should be measured by a thermocouple, or an equally or more reliable thermometer.

The thermocouple shall be positioned such that it does not interrupt the light pulse heating onto the front face of the specimen, or the radiation from the rear face of the specimen. If the specimen does not react with the thermocouple, a thin thermocouple should be contacted with the specimen to measure the specimen temperature with minimal uncertainty. If the thermocouple junction cannot be allowed to contact the specimen because of chemical reaction with the specimen, or because it interrupts the setting of the specimen, or because of the system design, the tip should be placed as close as practical to the specimen in the same plane.

4.4 Detector for measuring transient temperature rise of rear face of the specimen

The transient temperature rise curve on the rear face of the specimen shall be observed with a non-contact radiation thermometer or a radiation detector. The frequency response of the detector and its associated electronics should be faster than 10 kHz. The target diameter of the radiation detector should be smaller than 50 % of the diameter for disk specimens, or 50 % of the shortest side-length for square and rectangular specimens.

4.5 Environment for measurements

Measurements may be performed under open air, under an inert gas atmosphere, or under vacuum at room temperature. For higher temperature measurements, an appropriate inert atmosphere or vacuum shall be used, when necessary, to protect furnace parts and specimen holders from oxidation and to protect the specimen and its coating from structure/phase changes and compatibility problems.

4.6 Temperature control unit

For higher temperature measurements, the specimen should be kept at a stable temperature by electric heaters before pulse heating. Drift and fluctuation of the temperature should be less than 0,01 K/s.

4.7 Data acquisition unit

The transient detector signal should be amplified and converted to the digital signal using a digital oscilloscope or an AD converter which is input to a personal computer for computation of the thermal diffusivity. The frequency response of the amplifier and the AD conversion should be faster than 10 kHz. The resolution of the AD conversion should be larger than 10 bits, more than 1000 data points should be sampled with the sampling time faster than 1 % of the half rise-time " $t_{1/2}$ ".

5 Specimen

5.1 Shape and dimension of specimens

The specimen shall be a flat plate of circular, square or rectangular shape. The specimen diameter or side shall be between 5 mm and 15 mm.

The specimen thickness shall be chosen to be as follows:

- a) thicker than 0,5 mm and thinner than 5 mm;
- b) sufficiently thick that the $t_{1/2}$ value is larger than 5 times the pulse width.

The uniformity of the specimen thickness shall be smaller than 1,0 %.

5.2 Coating on the specimen

If the specimen does not have a high absorption coefficient for the heating laser beam or a high emissivity for radiative temperature detection, the surfaces of the specimen shall be coated with a thin, opaque, preferably black layer. The coating shall be dense enough to prevent penetration of the laser beam or thermal radiation at the observed wavelength, and should be resistive against laser pulse heating at high temperatures. Coating thickness should be a minimum commensurate with excluding directly transmitted laser pulse.

NOTE Suitable coatings for many ceramic materials include evaporated, sputtered carbon or sprayed colloidal graphite. If the test specimen reacts with carbon at high temperatures, a metal coating, such as platinum, gold or nickel may alternatively be used. The surface of the test specimen may, with advantage, be roughened to improve adhesion of the coating. The coating thickness dependence must be evaluated for the observed thermal diffusivity, if the contribution of coatings is not negligible.

5.3 Reference specimen

Reference specimens can be used to evaluate uncertainty of thermal diffusivity measurements by a laser flash apparatus. The uncertainty is obtained as the difference between the measured value and the reference value of thermal diffusivity of the reference specimen.

NOTE There are no certified reference materials for thermal diffusivity measurements authorized by national or international organizations yet, although several materials are used as such (see Annex E).

Care should be taken in the use of these references to ensure that the half rise-time and the thermal diffusivity value are similar to those of the test materials.

6 Measurement procedure

The specimen shall be measured under the following procedures.

6.1 Measurement of specimen thickness

Measure the thickness of the specimen to an accuracy of 0,5 % or better, using a micrometer in accordance with ISO 3611.

6.2 Surface treatment

Carry out the surface treatment in accordance with 5.2.

6.3 Determination of flash time of the laser pulse and the chronological profile of the laser pulse

The chronological trace of the laser pulse versus the same trigger signal to initiate laser flash thermal diffusivity measurements shall be observed. If the FWHM of the laser pulse duration is larger than 1 % of the half rise-time, correction for the finite pulse time shall be made following one of the procedures stated in Annex B.

6.4 Temperature and atmosphere control

Insert the test specimen in the apparatus and position the thermocouples. The atmosphere should be such that the specimen is not subjected to any chemical change under the measured temperature range.

6.5 Stability of specimen temperature

The specimen temperature shall be controlled with drift smaller than 0,01 K/s.

6.6 Energy of pulse heating

Irradiate the specimen with the laser pulse at an intensity of as low energy as possible, commensurate with an acceptable noise level.

NOTE Refer to Annex D about nonlinearity of spectral radiance on temperature.

6.7 Measurement temperature

Record the measurement temperature as $T_0 + \Delta T_{\max}$, where T_0 is the initial steady-state temperature and $\Delta T_{\max}$ is the maximum temperature rise of the specimen recorded by the thermocouple in contact with the specimen or the calibrated radiation thermometer.

NOTE A thermocouple below 0,15 mm in diameter, which is directly contacted to the rear or side surface of a specimen mechanically or with a paste, is preferable to estimate $\Delta T_{\max}$.

6.8 Record

The transient temperature curve should be recorded for a duration at least until 10 times the half-rise-time, in order to make reliable evaluation of measurements, including heat-loss correction and evaluation of nonuniform heating effect.

7 Data analysis

7.1 Calculation based on the half-rise-time method

The standard algorithm to calculate thermal diffusivity from the laser flash method is the half-rise-time method, in which the analytical equation is fitted to the transient temperature curve at t , the height of a half of maximum temperature rise of the transient temperature or radiance response curve above the base line " $\Delta T_{\max}/2$ " over the half-rise-time.

If the measurement is valid when made under the above-mentioned ideal initial and boundary conditions, the thermal diffusivity, α , is represented by the following equation based on the half-rise-time method:

$$\alpha = \frac{0,1388 d^2}{t_{1/2}} \quad (1)$$

where $t_{1/2}$ is the time delay when the temperature of the rear face reaches one-half of the maximum temperature rise $\Delta T_{\max}$ after the front face was heated by the laser pulse.

7.2 Criteria for applicability of the half-rise-time method

In order that the rise-time can be validly applied, the following initial and boundary conditions must be satisfied:

- The duration of the laser pulse is short, compared with the characteristic time of heat diffusion ($\text{FWHM} < 1\%$ of $t_{1/2}$).
- The front face of the specimen is uniformly heated by the light pulse.
- The specimen is adiabatic during the period of measurement after the light pulse heating.
- The specimen is uniform (in geometry) and is homogeneous.
- The specimen is opaque (nontransparent and nontranslucent) to the light pulse and to thermal radiation.

If these conditions are satisfied, the heat flow becomes one-dimensional and the temperature of the rear face of the specimen changes according to an analytical equation (See Annex A).

The thermal diffusivity value shall be determined by fitting this equation to the observed transient temperature curve. Theoretically, if the measurement is made under the above-mentioned ideal conditions, the calculated thermal diffusivity value should be independent of the position along the transient curves. Therefore, any point on the transient temperature curve can be analyzed to yield the thermal diffusivity, α . This will be given by Equation (2) as follows;

$$\alpha = \frac{K_x d^2}{t_x} \quad (2)$$

where

d is the specimen thickness, in metres;

t_x is the time for the specimen rear face to reach a fraction of the maximum temperature rise, in seconds (see Table 1);

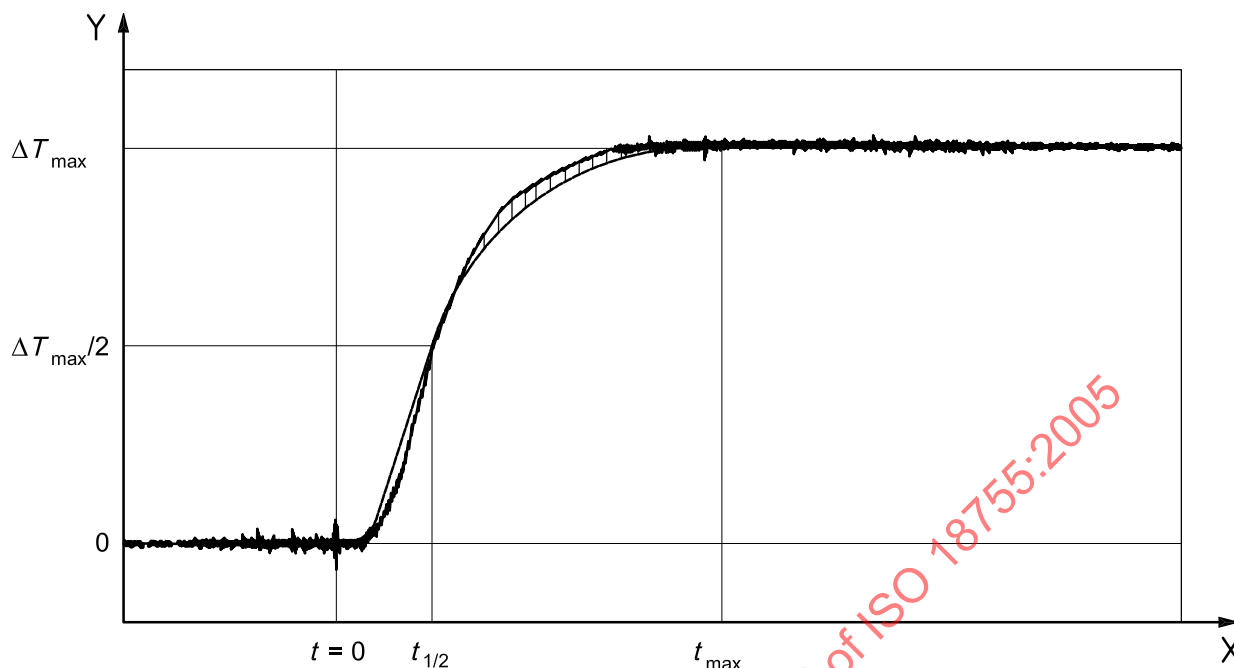
x is the percentage of the maximum rise in temperature;

K_x is a constant relating α to d and t_x , in the case of ideal measurements.

Calculate the thermal diffusivity at fractional temperature rises other than $t_{1/2}$. If the values at $t_{0,3}$, $t_{0,5}$ and $t_{0,7}$ calculated using the relevant values of K_x in Table 1 are all within $\pm 2\%$ then it can be assumed that the half-rise-time method is applicable without any correction. If the spread of thermal diffusivity values so calculated is greater than $\pm 2\%$, the possibility of non-ideal initial and/or boundary conditions, imperfect design and/or operation of the laser flash apparatus, or problems associated with the specimen, must be considered.

Table 1 — Values of constant K_x for a range of transient times

$x\%$	K_x	t_x
10	0,0662	$t_{0,1}$
20	0,0843	$t_{0,2}$
30	0,1012	$t_{0,3}$
40	0,1190	$t_{0,4}$
50	0,1388	$t_{1/2}$
60	0,1622	$t_{0,6}$
70	0,1919	$t_{0,7}$
80	0,2332	$t_{0,8}$
90	0,3036	$t_{0,9}$

**Key**

X: time

Y: temperature rise

Figure 3 — Averaged deviation of the transient temperature curve (solid curve) from the Parker's equation having the observed half rise-time (broken curve)

The applicability of the half-rise-time method can alternatively be checked through the averaged deviation of the transient temperature curve from the Parker's equation corresponding to the experimentally determined half rise-time as shown in Figure 3. The averaged deviation is calculated over the region from the half rise-point to the maximum point normalized by the maximum temperature rise " $\Delta T_{\max}$ ". If the averaged deviation is within $\pm 1\%$ then it can be assumed that no corrections apply.

If the averaged deviation is greater than $\pm 1\%$, the possibility of non-ideal initial and/or boundary conditions, imperfect design and/or operation of the laser flash apparatus, or problems associated with the specimen, shall be considered, as follows.

a) Imperfect design and/or operation of the laser flash apparatus:

- 1) superposition of stray light or electrical noise on the transient temperature response curve;
- 2) excessive drift of steady-state temperature;
- 3) insufficient response time of radiation detector and/or amplifier;
- 4) non-negligible heat exchange with the specimen holder;
- 5) effect of non-linearity of spectral radiance.

b) Problems associated with the specimen:

- 1) thermal resistance of coating;
- 2) poor flatness of the specimen;
- 3) large void or inhomogeneous distribution of pores.

c) Non-ideal initial and boundary conditions:

- 1) nonuniform heating effects;
- 2) finite pulse time effect;
- 3) radiation heat loss.

First, check Items a), b) and item c) 1) and improve them to make the measurements closer to the ideal conditions.

NOTE During practical measurement by the laser flash method it is difficult always to satisfy the ideal initial and boundary conditions. Annex C and the Bibliography give examples of analyses for non-ideal conditions which may be applied as appropriate. Annex D gives information on other sources of error. If the position is still not acceptable, then corrections for items c) 1) and c) 2) are necessary via appropriate algorithms.

Examples of such analyses are given in Annex C. Details of all the procedures employed shall be given in the measurement report.

8 Measurement report

The following information should be recorded in the measurement report:

a) General information

- 1) The name and address of the testing establishment.
- 2) The date of measurements.
- 3) A unique identification of the report.
- 4) A reference to this International Standard.
- 5) The name of the laser flash apparatus used.

b) Light pulse

- 1) The type of the pulse light source.
- 2) Duration of the light pulse in full width at half maximum (optional).
- 3) Energy of one light pulse (optional).
- 4) Statement of spatial profile of the laser beam.

c) Specimen

- 1) A description of the material; (material type, manufacturing code, batch number, date of receipt).
- 2) Method of cutting, grinding and/or polishing specimens from supplied material.
- 3) Shape of the specimen (disk, square plate or rectangular plate).
- 4) Diameter or side length of the specimen.
- 5) Thickness of the specimen.

d) Coating

- 1) Use of coating (Yes or No).
- 2) Coated material.
- 3) Coating procedure.
- 4) Thickness of coating (optional).

e) Thermometry

- 1) Thermometer used for steady-state temperature measurements.
- 2) Thermometer or radiation detector used for measuring transient temperature or radiance rise of the specimen rear face after light pulse heating.

f) Data acquisition (optional)

- 1) Response time of the transient temperature measurements.

g) Data analysis

- 1) The type of the analytical solution on which the data analysis is founded.
- 2) The data analysis algorithm (half-rise-time method, least-square-fit method, non-linear least-square method, equiareal method or logarithmic method).

h) Corrections

- 1) Calculated values of heat-loss corrections, if any, giving full details if the methods are not given in Annex B or C.
- 2) Calculated values of nonuniform heating corrections, if any, giving full details if the methods are not given in Annex B or C.
- 3) Calculated values of finite pulse time correction, if any, giving full details if the methods are not given in Annex B.
- 4) Calculated values of nonlinearity of spectral radiance correction, if any, giving full details if the methods are not given in Annex B or C.
- 5) Calculated values of coating thermal resistance corrections, if any, giving full details.

i) Measured results

- 1) The measurement temperature(s), in kelvins or degrees Celsius.
- 2) The half rise-time, in seconds.
- 3) The calculated thermal diffusivity value(s) in m^2/s .

j) Other important information

- 1) Discussion of errors and correction procedures.
- 2) Comments about the measurement and measurement results.

Annex A (informative)

Principle of laser flash thermal diffusivity measurements

A.1 Ideal condition

The analytical solution for laser flash thermal diffusivity measurements has been given by Parker et al. [1] under the following conditions.

- a) The duration of the laser pulse is negligibly short compared to the characteristic time of heat diffusion.
- b) The front face of the specimen is uniformly heated by a light pulse.
- c) The specimen is adiabatic during the measurement after the light pulse heating.
- d) The specimen is uniform (in geometry) and is homogeneous.
- e) The specimen is opaque (nontransparent and nontranslucent) to the light pulse and to thermal radiation.

If these conditions are satisfied, the heat flow becomes one-dimensional and the temperature of the rear face of the specimen changes according to the following equation:

$$T(t) = \Delta T \left[1 + 2 \sum_{n=1}^{\infty} (-1)^n \exp \left(-(\pi n)^2 \frac{t}{\tau_0} \right) \right] \quad (\text{A.1})$$

where

$$\Delta T = Q / C$$

Q is the total energy absorbed by the specimen;

C is the heat capacity of the specimen;

$\tau_0 = \frac{d^2}{\alpha}$ is the characteristic time of heat diffusion across the specimen;

α is the thermal diffusivity of the specimen.

Annex B (informative)

Correction for non-ideal initial and boundary conditions

B.1 General

The calculation of thermal diffusivity using Equation (1) is modified if the pulse transit time is less than 100 times the duration of the heat pulse, or if heat is lost from the specimen. Examples of modifications applying to the calculation method are given in B.2 to B.3.

The mathematical derivation given in Annex A assumes that no heat is lost from the specimen during the time taken for the heat pulse to pass through it. [2-5] For good conductors at temperatures close to ambient, this is a reasonable approximation, but for poor conductors and for most samples at high temperatures, corrections for heat losses will almost certainly be applicable.

Provided that use of a suitable holder design has minimized heat lost from the specimen by conduction, and that the duration of the transient is short enough for heat lost by convection to be neglected (there are no convective losses if the measurement is performed in a vacuum), the main source of heat loss is by radiation from the specimen surfaces. The best way to analyze heat loss is to compare the entire experimental curve with one or more of the many theoretical models available. Examples of analytical methods are given in Annex C.

B.2 Effect of finite pulse time

Several analytical calculations have been reported in order to correct the effect of the finite duration time of the heating laser pulse [6-8]. If the pulse width is much shorter than the half rise-time of the transient temperature curve, the laser pulse heating can be approximated by Dirac's delta function located at the chronological centroid of laser light energy [9].

When $t_{1/2}$ is less than 100 times the heat pulse duration, the finite pulse time effect should be corrected. Two widely used correction methods are the centroid method and the triangular pulse method described as follows.

B.2.1 Centroid method [9]

If $t_{1/2}$ is larger than 3 times the Pulse width (τ_p), the finite pulse time effect can be corrected by shifting the time origin of the data analysis to the chronological centroid of the laser pulse (t_g). Thus, $t_{1/2}$ should be replaced by $t_{1/2} - t_g$.

B.2.2 Determination of chronological centroid of laser pulse

The chronological centroid of the laser pulse (t_g) should be determined by one of the following procedures.

B.2.2.1 Real time method

Measure the waveform of the laser pulse by a detector of frequency response faster than 10 μ s, and calculate the centroid directly from the observed waveform.

B.2.2.2 Integration method

Prepare a metallic sheet thin enough that the heat diffusion time across it is shorter than 3 μ s. Then, the chronological trace of the temperature rise of the metallic film is proportional to the integrated energy of the

laser beam from the starting point of the laser pulse. The waveform of the laser pulse is derived as the derivative of the chronological trace of the temperature rise.

B.2.3 Triangular pulse approximation [6]

The shape of the heat pulse from a neodymium-glass laser and a flash-lamp can be approximated by a triangular pulse of duration τ with a maximum occurring at β , where β is a fraction between zero and one.

This is most easily achieved by using a fast-response photodiode (as used in several laser calorimeters) or by measuring the change in resistance of a thin (approximately 25 μm) tantalum foil strip when subjected to the heat pulse. The parameters τ and β usually change with the heat pulse power, and so should be determined at the power to be used.

Once τ and β are known, the thermal diffusivity α is given by the equation:

$$\alpha = \frac{C_1 d^2}{C_2 t_{1/2} - \tau} \quad (\text{B.1})$$

where

the constants C_1 and C_2 are given in Table B.1 for values of β ;

d is the specimen thickness.

The finite pulse time correction given in Equation (B.1) should not be used for $t_{1/2}$ less than 10τ .

Table B.1 — Finite pulse time correction constants

β	C_1	C_2
0,15	0,34844	2,5106
0,28	0,31550	2,2730
0,29	0,31110	2,2454
0,30	0,30648	2,2375

B.3 Effect of radiative heat losses

The thermal diffusivity shall be calculated from Equation (B.2), introducing correction factors if radiative heat losses cannot be neglected.

$$\alpha = 0,1388 k_{rhl} d^2 / t_{1/2} \quad (\text{B.2})$$

where

α is the thermal diffusivity (m^2/s);

d is the thickness of the specimen at room temperature (m);

k_{rhl} is the correction factor relating to heat loss from the specimen.

The following boundary condition is introduced instead of the adiabatic boundary condition, in order to formulate an analytical solution under the radiative heat losses. The other assumptions are the same as the ideal conditions.

Heat losses from the specimen can be expressed by the Newtonian cooling law and the Biot number can be defined.

There are a few algorithms to calculate thermal diffusivity from the data obtained by the laser pulse methods which take the radiative heat loss into consideration [10-17]. Cape and Lehman [14] gave a general solution for the laser flash thermal diffusivity measurements which took the radiative heat losses into consideration. The contribution of the radiative heat loss is expressed by a non-dimensional parameter called the Biot number. Cape and Lehman presented an approximate formula for their general solution. Josell et al. found that coefficients of higher order terms in Cape and Lehman's equation are not correct and presented the corrected equation as follows [16]:

$$T(t) = \Delta T \sum_{n=0}^{\infty} A_n \exp\left(-X_n^2 \frac{t}{\tau_0}\right) \quad (\text{B.3})$$

$$A_n = 2(-1)^n \cdot X_n^2 (X_n^2 + 2Y + Y^2)^{-1},$$

$$X_0 = (2Y)^{1/2} (1 - Y/12 + 11Y^2/1440),$$

$$X_n = n\pi + \frac{2Y}{n\pi} - \frac{4Y^2}{(n\pi)^3} + \left\{ \frac{16}{(n\pi)^5} - \frac{2}{3(n\pi)^3} \right\} Y^3 + \left\{ -\frac{80}{(n\pi)^7} + \frac{16}{3(n\pi)^5} \right\} Y^4 \quad (n \geq 1),$$

where

$$\Delta T = Q/C$$

Q is the total energy absorbed by the specimen;

C is the heat capacity of the specimen;

$\tau_0 = d^2/\alpha$ is the characteristic time of heat diffusion across the specimen;

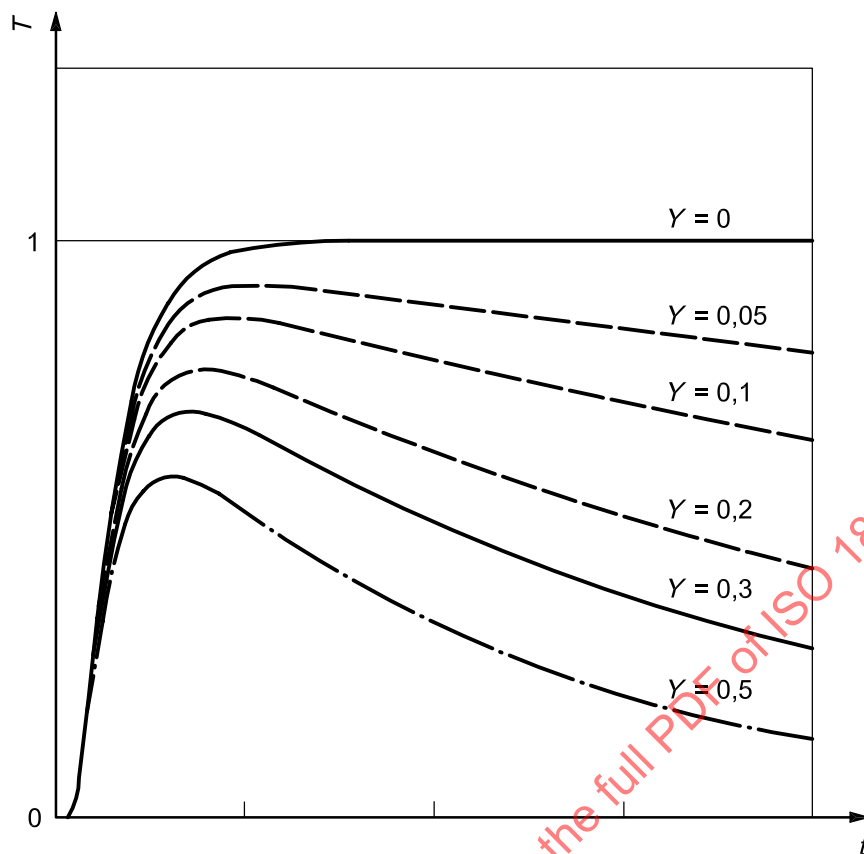
α is the thermal diffusivity of the specimen;

$Y = kd/\lambda$ is the Biot number.

Figure B.1 shows plots of Equation (B.3) for different values of parameter “Y”.

There are a few algorithms to calculate thermal diffusivity from the data obtained by the laser pulse methods which take the radiative heat loss into consideration. Among them, Cowan's method [13] and Clark and Taylor's method [15] are most commonly used. Their methods are in contrast with each other because the former uses the cooling part of the curve, whereas the latter uses the heating part of the curve to correct for the radiative heat loss. Takahashi et al. [17] proposed a correction method similar to Cowan's method. Their method calculates the correction factor for radiative heat loss from the ratio of $t_{1/2}$ to τ_c , which is the characteristic time of heat loss.

In order to apply Cowan's method or Takahashi's method successfully, drift of the steady-state temperature and conduction heat loss must be small. On the other hand, Clark and Taylor's method requires a high signal-to-noise ratio.

**Key***t*: time*T*: normalized temperature rise**Figure B.1 — Plots of Equation (B.3) for different values of the parameter “Y”****B.3.1 Cowen's method**

According to Cowen's algorithm, the correction factor k_{rhl} , is given by Equation (B.4):

$$k_{rhl} = A + Bn + Cn^2 + Dn^3 + En^4 + Fn^5 + Gn^6 + Hn^7 \quad (\text{B.4})$$

$$n = 2\Delta T_{10} / \Delta T_{\max}$$

where ΔT_{10} is the temperature rise at $10t_{1/2}$

A: 0,39499

B: 1,20301

C: - 2,06077

D: 2,04296

E: - 0,96565

F: 0,17347

G: 0

H: 0

when ΔT_5 : temperature rise at $5t_{1/2}$

A : - 0,74729

B : 8,92744

C : - 28,65631

D : 49,63425

E : - 49,03007

F : 27,78776

G : - 8,41414

H : 1,05579

B.3.2 Azumi and Takahashi's method [17]

According to this algorithm, the correction factor k_{rhl} , is given by Equation (B.5):

$$k_{rhl} = 1 - B_1 \left(\sqrt{1 + A_1 \cdot c \cdot t_{1/2}} - 1 \right) \quad (\text{B.5})$$

where the following values should be substituted for A_1 and B_1 :

When $L \leq 0,4$

$$A_1 = 96 / (1 + L)$$

$$B_1 = 0,084$$

When $0,4 < L \leq 1,0$

$$A_1 = 89 [1 + 1,24 (1 - L) - 2,70 (1 - L)^2]$$

$$B_1 = 0,08 [1 - 1,13 (1 - L) + 2,01 (1 - L)^2]$$

When $L > 1,0$

$$A_1 = 89$$

$$B_1 = 0,080$$

where

$$L = d / r$$

r is the radius of the specimen, or radius of the circle having the same area as the specimen if the specimen is not a true circle.

B.3.3 Clark and Taylor's method [15]

Heat-loss corrections based on the Clark and Taylor rise curve data also use ratio techniques. For the $t_{0,75}/t_{0,25}$ ratio, which is the time to reach 75 % of $\Delta T_{\max}$ divided by the time to reach 25 % of $\Delta T_{\max}$, the ideal value is 2,272. Determine this ratio from the experimental data. Then calculate the correction factor k_{rhl} from the following equation:

$$k_{rhl} = -0,3461467 + 0,361578(t_{0,75}/t_{0,25}) - 0,06520543(t_{0,75}/t_{0,25})^2 \quad (\text{B.6})$$

Corrections based on many other ratios can also be used.

B.4 Correction for thermal expansion

A thermal diffusivity calculated by the procedure in the main text is the apparent thermal diffusivity " $\alpha_0(T)$ " based on the specimen thickness at room temperature.

The correct thermal diffusivity based on the specimen thickness at the measurement temperature " $\alpha(T)$ " is derived by the following equation.

$$\alpha(T) = \left(\frac{d_T}{d_0} \right)^2 \cdot \alpha_0(T) \quad (\text{B.7})$$

where

d_0 is the specimen thickness at room temperature;

d_T is the specimen thickness at the measurement temperature " T ".

Annex C (informative)

Data analysis algorithms to calculate thermal diffusivity from observed temperature history curve under non-ideal initial and boundary conditions

C.1 Logarithmic method

The thermal diffusivity is calculated from Equation (C.1) based on the logarithmic method [18-21].

$$\alpha = -d^2 / 4h \quad (\text{C.1})$$

where h is the inclination of strength line obtained when $\ln(\sqrt{t} \cdot \Delta T)$ is plotted in respect to $1/t$ in the rising region ($0,3 < \Delta T / \Delta T_{\max} < 0,6$) of temperature rise curve(s).

C.2 Least-square-fit methods

An observed transient temperature curve after pulse heating should be least-square fitted with the analytical solution of the thermal diffusion equation with variable parameters, including the thermal diffusivity value, under the initial and boundary conditions corresponding to the measurement condition [22]. The thermal diffusivity value is determined as one of the fixed parameters in the least-square-fitted analytical solution.

C.3 Non-linear least-square methods [23]

Watt [11] gave the theoretical background with the wide applicability on the pulse heating methods, where the temperature response $T(x, r, t)$ at time t in cylindrical coordinates (x, r) is accompanied with two subsidiary equations (C.3) and (C.4).

$$T(x, r, t) = \Delta T_{o, \max} \left\{ \sum_{n=1}^{\infty} Y_n(x) \int_0^b f(x') Y_n(x') dx' \right\} \cdot \left\{ \sum_{j=1}^{\infty} \frac{2}{a^2} \frac{\mu_j^2 j_0 \left(\mu_j \frac{r}{a} \right)}{(\mu_j^2 + L_r^2) j_0^2(\mu_j)} \int_0^a r' g(r') j_0 \left(\mu_j \frac{r'}{a} \right) dr' \right\} \\ \times \int_{t_1}^{t_2} \exp \left\{ -\alpha \left(\frac{\mu_j^2}{a^2} + \frac{\beta_n^2}{b^2} \right) (t - t') \right\} \Psi(t') dt' \quad (\text{C.2})$$

$$Y_n(x) = \frac{\left\{ 2 \left(\beta_n^2 + L_2^2 \right)^{1/2} \right\} \left\{ \beta_n \cos \left(\frac{x \beta_n}{b} \right) + L_1 \sin \left(\frac{x \beta_n}{b} \right) \right\}}{b^{1/2} \left\{ (\beta_n^2 + L_1^2)(\beta_n^2 + L_2^2 + L_2) + L_1(\beta_n^2 + L_2^2) \right\}^{1/2}} \\ \tan \beta_n = \frac{\beta_n (L_1 + L_2)}{\beta_n^2 - L_1 L_2} \quad (\text{C.3})$$

$$\mu_j J_1(\mu_j) - L_r J_0(\mu_j) = 0 \quad (\text{C.4})$$

where

the distribution of a heat pulse is expressed by $f(x)g(r)\Psi(t)$ ($0 \leq x \leq b, 0 \leq r \leq a, t_1 \leq t \leq t_2$);

L_1, L_2 , and L_r are Biot numbers of specimen (front, rear and side) surfaces;

a and b are the diameter and thickness of a specimen, respectively;

μ_j and β_n are roots of Equations (C.3) and (C.4), respectively;

$\Delta T_{0, \max}$ is the maximum temperature rise of a specimen at $L = 0$ (adiabatic condition).

These relations show that thermal diffusivity, non-approximated Biot numbers, pulse width and non-uniformity of pulse can be, in principle, calculated under the assumption of axial symmetry from one transient temperature curve observed in the specified area on a specimen.

The actual data analysis procedures may be carried out on the basis of the Marquart (non-linear regression) method, as shown with the nonlinear operational form of Equation (C.2), the algorithm of data analysis, and some measurement results in [23].

In order to avoid ambiguous estimations, the centroid of pulse t_g is at first determined using a sufficiently thin metal foil, then nonuniformity of a pulse is estimated using suitable functions with one of specimens at room temperature, where heat losses are negligibly small. As the centroid position t_g and nonuniformity of laser pulses are usually assumed to be constant during experiments, thermal diffusivity, Biot numbers and $\Delta T_{0, \max}$ (or the corresponding value in a transient radiance curve) can be precisely determined simultaneously under the predetermined parameters including the observed temperature area (diameters). The procedures are also applicable to measure thermal diffusivity of thin films, such as those not covered by this regulation, because the laser heating and observed temperature area may be flexibly controlled and specified on a specimen so as to satisfy Equation (C.2), if the conditions are axial symmetry.

C.4 Equiareal method

The thermal diffusivity value should be determined when the integrated areas from t_1 to t_2 are equal under the observed transient temperature curve and under the analytical solution of the thermal diffusion equation under the initial and boundary conditions corresponding to the measurement condition [5, 24].

The amplitude of the analytical solution is normalized to the observed transient temperature curve at the maximum temperature if measurements are made under the ideal condition with no heat losses under uniform heating.

Under the general boundary condition with heat losses, the amplitude of the analytical solution is normalized by the asymptotic exponential function of the corresponding analytical solution.

As described in B.3, the equiareal method takes the effect of radiative heat losses from the beginning, since the observed temperature response curve is fitted by Josell's equation [Equation (B.2)] which is the solution under the heat-loss boundary condition [14, 16].

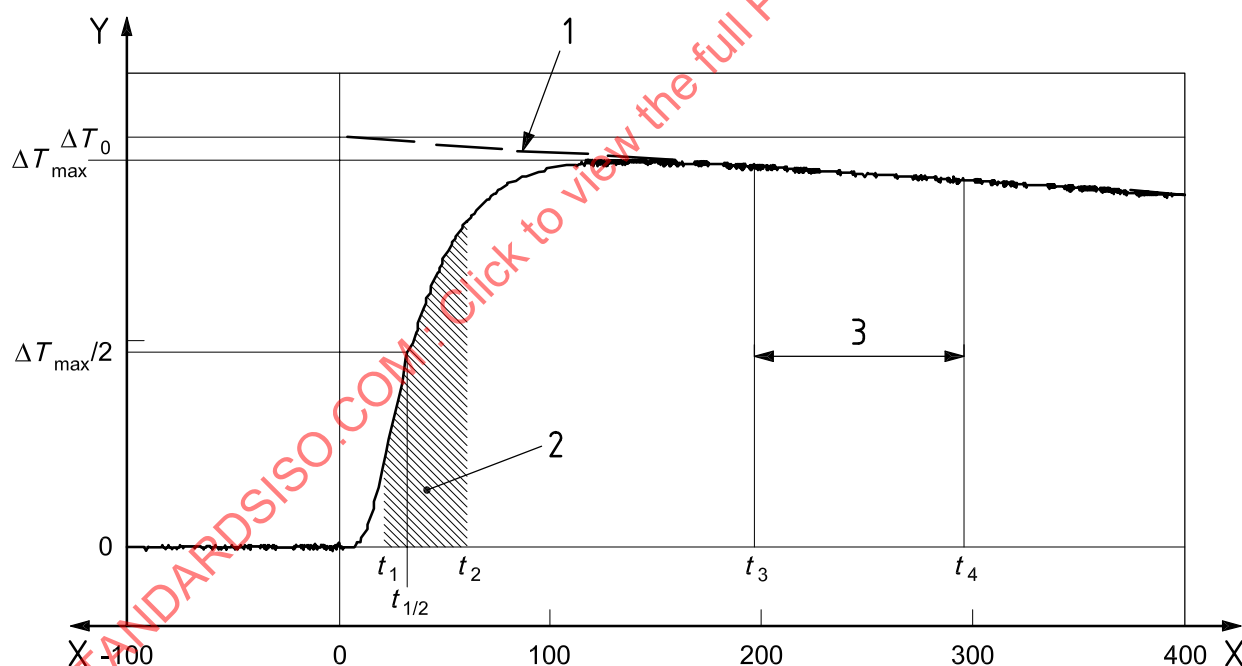
The equiareal method calculates thermal diffusivity from the transient temperature curve obtained by the laser flash measurement. In contrast to the half-rise-time method, the entire set of the experimental data is fitted by the theoretical curve based on Cape and Lehman's analysis [14] corrected by Josell et al. [16], which considers the radiative-heat-loss effect exactly. Both thermal diffusivity and Biot number are simultaneously determined by this equiareal method as shown in Figure C.1.

If $t > \tau_0$, the terms of order higher than 2nd can be neglected compared with the 1st term in Equation (B.2). Thus, the specimen temperature converges to the steady-state temperature before the light pulse heating expressed by the following single exponential equation:

$$T(t) = \Delta T \cdot A_0 \exp\left(-X_0^2 \frac{t}{\tau_0}\right) \quad (\text{C.5})$$

Consequently, the temperature rise decreases exponentially with the characteristic cooling time of $\tau_c = \tau_0 / X_0^2$. The data analysis procedure to determine thermal diffusivity values by the equiareal method is shown in Figure 2. First, τ_c is determined by a least-squares fit over the cooling region " $t > \tau_0$ " of the observed temperature response curve. Then, if either the thermal diffusivity or Biot number is determined, the other is simultaneously fixed. Thus, the thermal diffusivity is determined when the normalized area under Equation (B.2), as a function of t with the parameter τ_0 for the fixed region ($t_1 < t < t_2$), is equal to the area under the observed temperature response curve for the same time region [5].

One advantage of the equiareal method is that the quality of experimental data can be checked by observing the discrepancy between the experimental data and the theoretical curve. Data of poor quality, such as those affected by nonuniform heating, by drift of steady-state temperature, or by a temperature detection system of slow response time, can be screened out immediately. Thus, only the experimental data of good quality are chosen and the thermal diffusivity values with smaller uncertainty are obtained.



Key

X: time (ms)

Y: normalised temperature rise

1 exponential function

2 equal area method

3 least-square fit

Figure C.1 — Principle of the equiareal method to calculate thermal diffusivity from a transient temperature curve observed by the laser flash method

Annex D (informative)

Other error factors

D.1 Effect of nonuniform heating

There have been several investigations to analyze heat diffusion and temperature response after nonuniform pulse heating [25-27]. McKay and Schriempf^[25] gave a general analytical solution of temperature distribution within the specimen after the front face was heated by a laser beam of arbitrary energy distribution.

D.1.1 Observation of spatial energy distribution of pulse laser beam

It is desirable that the spatial energy distribution of pulse laser is quantitatively measured with a beam profile measurement instrument such as a CCD camera [28]. If those instruments are not available, the beam profile can be checked with a sheet of laser-beam foot print paper.

When the temperature profile is axially symmetric, axial energy distribution of the laser beam can be measured using a laser power meter while changing the aperture size of the field stop before the power meter. The diameter of the aperture size should be typically from 2 mm to the specimen diameter (10 mm standard) by steps of 2 mm.

The energy transmitting through the aperture of diameter ϕ is the integration of the energy distribution $q(z)$ of the laser beam as follows:

$$\begin{aligned} Q(\phi) &= \int_0^\phi q(z) \cdot 2\pi z dz = q_0 \int_0^\phi \left[1 + c_1 J_0\left(\mu_1 \frac{z}{r}\right) \right] \cdot 2\pi z dz \\ &= q_0 \left(\pi \phi^2 + c_1 \int_0^\phi J_0\left(\mu_1 \frac{z}{r}\right) \cdot 2\pi z dz \right) \end{aligned} \quad (D.1)$$

$$c_1 = \frac{Q(\phi)/q_0 - \pi \phi^2}{\int_0^\phi J_0\left(\mu_1 \frac{z}{r}\right) \cdot 2\pi z dz} \quad (D.2)$$

where μ_1 is the first positive root of $J_1(x) = 0$ and $J_1(x)$ is the first-order Bessel function.

When the aperture diameter is equal to the specimen diameter,

$$Q(r) = \pi r^2 q_0 = Q \quad (D.3)$$

where Q is the total energy of the pulse incident on the specimen.

The temperature distribution along the rear face of the specimen by the function $T(z, t)$, where $0 < z < r$ and $t > 0$. Then $T(z, t)$ is expressed as:

$$T(z, t) = \Delta T \cdot \left[1 + \sum_{j=1}^{\infty} c_j J_0\left(\mu_j \frac{z}{r}\right) \cdot \exp\left(-\left(\frac{\pi \mu_j}{\rho}\right)^2 \cdot \frac{t}{\tau_0}\right) \right] \cdot \left[1 + 2 \sum_{n=1}^{\infty} (-1)^n \exp\left(-(\pi n)^2 \frac{t}{\tau_0}\right) \right] \quad (D.4)$$

where

$$\Delta T = Q/C;$$

Q is the total energy absorbed by the specimen;

C is the heat capacity of the specimen;

$$\rho = \pi/(2p);$$

$p = d/(2r)$ is the thickness to diameter ratio of the specimen;

$\tau_0 = d^2/\alpha$ is the characteristic time of heat diffusion across the specimen;

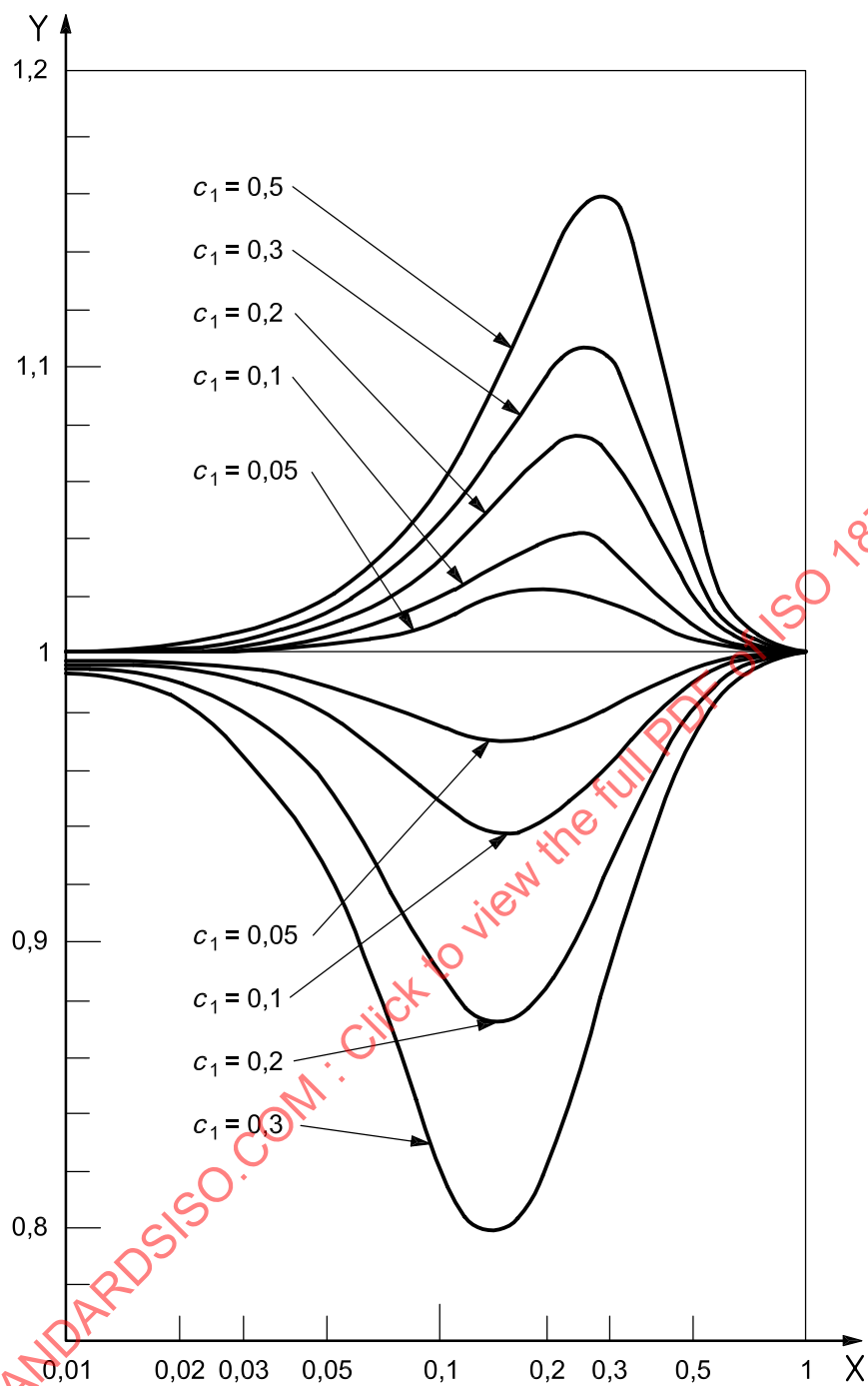
α is the thermal diffusivity of the specimen.

The nonuniform heating effect is expressed by the first parenthesis and the second parenthesis corresponds to the normal solution under the uniform heating.

D.1.2 Evaluation of nonuniform heating effect

The temperature response of any combination of p and c_1 can be calculated from Equation (D.4), and the apparent thermal diffusivity values, α , can be calculated by the half-rise-time method. Figure D.1 shows the calculated apparent thermal diffusivity values, when temperature is measured at the center of the specimen as a function of thickness to diameter ratio p with a parameter c_1 .

When the coefficient c_1 is positive, the beam has a hot center and when the coefficient c_1 is negative, the beam has a cold center. All curves have a maximum ($c_1 > 0$) or minimum ($c_1 < 0$) between $p = 0,15$ and $p = 0,3$, where the nonuniform heating effect is largest under irradiation of the laser beam of the same profile.



Key

X: ratio of thickness to diameter (in log scale), p

Y: apparent thermal diffusivity (normalised)

Figure D.1 — Calculated apparent thermal diffusivity when temperature is measured at the centre of the specimen as a function of “ p ” with a parameter “ c_1 ”