
**Elastomeric seismic-protection
isolators —**

**Part 3:
Applications for buildings —
Specifications**

*Appareils d'appuis structuraux en élastomère pour protection
sismique —*

Partie 3: Applications pour bâtiments — Spécifications



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Foreword

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

The procedures used to develop this document and those intended for its further maintenance are described in the ISO/IEC Directives, Part 1. In particular, the different approval criteria needed for the different types of ISO documents should be noted. This document was drafted in accordance with the editorial rules of the ISO/IEC Directives, Part 2 (see www.iso.org/directives).

Attention is drawn to the possibility that some of the elements of this document may be the subject of patent rights. ISO shall not be held responsible for identifying any or all such patent rights. Details of any patent rights identified during the development of the document will be in the Introduction and/or on the ISO list of patent declarations received (see www.iso.org/patents).

Any trade name used in this document is information given for the convenience of users and does not constitute an endorsement.

For an explanation of the voluntary nature of standards, the meaning of ISO specific terms and expressions related to conformity assessment, as well as information about ISO's adherence to the World Trade Organization (WTO) principles in the Technical Barriers to Trade (TBT) see www.iso.org/iso/foreword.html.

This document was prepared by Technical Committee ISO/TC 45, *Rubber and rubber products*, Subcommittee SC 4, *Products (other than hoses)*.

This third edition cancels and replaces the second edition (ISO 22762-3:2010), which has been technically revised.

The main changes compared to the previous edition are as follows:

- the definitions of some symbols in [Clause 4](#) have been changed;
- a column stipulating the minimum number of test pieces has been added to [Table 4](#);
- a new subclause ([6.9](#)) has been added.

A list of all parts in the ISO 22762 series can be found on the ISO website.

Any feedback or questions on this document should be directed to the user's national standards body. A complete listing of these bodies can be found at www.iso.org/members.html.

Introduction

ISO 22762 series includes two parts related to specifications for isolators, i.e. ISO 22762-2 for bridges and ISO 22762-3 for buildings. This is because the isolator requirements for bridges and buildings are quite different, although the basic concept of the two products is similar. Therefore, ISO 22762-2 and the relevant clauses in ISO 22762-1 are used when ISO 22762 (all parts) is applied to the design of bridge isolators whereas ISO 22762-3 and the relevant clauses of ISO 22762-1 are used when it is applied to building isolators.

The main differences to be noted between isolators for bridges and isolators for buildings are the following.

- a) Isolators for bridges are mainly rectangular in shape and those for buildings are circular in shape.
- b) Isolators for bridges are designed to be used for both rotation and horizontal displacement, while isolators for buildings are designed for horizontal displacement only.
- c) Isolators for bridges are designed to perform on a daily basis to accommodate length changes of bridges caused by temperature changes as well as during earthquakes, while isolators for buildings are designed to perform only during earthquakes.
- d) Isolators for bridges are designed to withstand dynamic loads caused by vehicles on a daily basis as well as earthquakes, while isolators for buildings are mainly designed to withstand dynamic loads caused by earthquakes only.

For structures other than buildings and bridges (e.g. tanks), the structural engineer uses either ISO 22762-2 or ISO 22762-3, depending on the requirements of the structure.

Elastomeric seismic-protection isolators —

Part 3:

Applications for buildings — Specifications

1 Scope

This document specifies minimum requirements and test methods for elastomeric seismic isolators used for buildings and the rubber material used in the manufacture of such isolators.

It is applicable to elastomeric seismic isolators used to provide buildings with protection from earthquake damage. The isolators covered consist of alternate elastomeric layers and reinforcing steel plates. They are placed between a superstructure and its substructure to provide both flexibility for decoupling structural systems from ground motion, and damping capability to reduce displacement at the isolation interface and the transmission of energy from the ground into the structure at the isolation frequency.

2 Normative references

The following documents are referred to in the text in such a way that some or all of their content constitutes requirements of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

ISO 630 (all parts), *Structural steels*

ISO 22762-1:2018, *Elastomeric seismic-protection isolators — Part 1: Test methods*

3 Terms and definitions

For the purposes of this document, the following terms and definitions apply.

ISO and IEC maintain terminological databases for use in standardization at the following addresses:

— ISO Online browsing platform: available at <http://www.iso.org/obp/>

— IEC Electropedia: available at <http://www.electropedia.org/>

3.1

breaking

rupture of *elastomeric isolator* (3.8) due to compression- (or tension-) shear loading

3.2

buckling

state when *elastomeric isolators* (3.8) lose their stability under compression-shear loading

3.3

compressive properties of elastomeric isolator

K_v

compressive stiffness for all types of rubber bearings

3.4

cover rubber

rubber wrapped around the outside of inner rubber and reinforcing steel plates before or after curing of elastomeric isolators for the purposes of protecting the inner rubber from deterioration due to oxygen, ozone and other natural elements and protecting the reinforcing plates from corrosion

3.5

design compressive stress

long-term compressive force on the *elastomeric isolator* (3.8) imposed by the structure

3.6

effective loaded area

area sustaining vertical load in *elastomeric isolator* (3.8), which corresponds to the area of reinforcing steel plates

3.7

effective width

<rectangular elastomeric isolator> the smaller of the two side lengths of inner rubber to which direction shear displacement is not restricted

3.8

elastomeric isolator

rubber bearing, for seismic isolation of buildings, bridges and other structures, which consists of multi-layered vulcanized rubber sheets and reinforcing steel plates

EXAMPLE High-damping rubber bearings, linear natural rubber bearings and lead rubber bearings.

3.9

first shape factor

ratio of effectively loaded area to free deformation area of one inner rubber layer between steel plates

3.10

high-damping rubber bearing

HDR

elastomeric isolator with relatively high damping properties obtained by special compounding of the rubber and the use of additives

3.11

inner rubber

rubber between multi-layered steel plates inside an elastomeric isolator *elastomeric isolator* (3.8)

3.12

lead rubber bearing

LRB

elastomeric isolator (3.8) whose *inner rubber* (3.11) with a lead plug or lead plugs press fitted into a hole or holes of the isolator body to achieve damping properties

3.13

linear natural rubber bearing

LNR

elastomeric isolator (3.8) with linear shear force-deflection characteristics and relatively low damping properties, fabricated using natural rubber

Note 1 to entry: Any bearing with relatively low damping can be treated as an LNR bearing for the purposes of isolator testing.

3.14

maximum compressive stress

peak stress acting briefly on *elastomeric isolators* (3.8) in compressive direction during an earthquake

3.15**nominal compressive stress**

long-term stress acting on *elastomeric isolators* (3.8) in compressive direction as recommended by the manufacturer for the isolator, including the safety margin

3.16**roll-out**

instability of an isolator with either dowelled or recessed connection under shear displacement

3.17**routine test**

test for quality control of the production isolators during and after manufacturing

3.18**second shape factor**

<circular elastomeric isolator> ratio of the diameter of the *inner rubber* (3.11) to the total thickness of the inner rubber

3.19**second shape factor**

<rectangular or square elastomeric isolator> ratio of the effective width of the *inner rubber* (3.11) to the total thickness of the inner rubber

3.20**shear properties of elastomeric isolators**

comprehensive term that covers characteristics determined from isolator tests:

- shear stiffness, K_h , for LNR;
- shear stiffness, K_h , and equivalent damping ratio, h_{eq} , for HDR and LRB;
- post-yield stiffness, K_d , and characteristic strength, Q_d , for LRB

3.21**standard value**

value of isolator property defined by manufacturer based on the results of type test

3.22**structural engineer**

engineer who is in charge of designing the structure for base-isolated bridges or buildings and is responsible for specifying the requirements for *elastomeric isolators* (3.8)

3.23**type test**

test for verification either of material properties and isolator performances during development of the product or that project design parameters are achieved

3.24**ultimate properties**

properties at either buckling, breaking, or roll-out of an isolator under compression-shear loading

3.25**ultimate property diagram****UPD**

diagram giving the interaction curve of compressive stress and buckling strain or breaking strain of an elastomeric isolator

4 Symbols

For the purposes of this document, the symbols given in [Table 1](#) apply.

Table 1 — Symbols and descriptions

Symbol	Description
A	effective plan area; plan area of elastomeric isolator, excluding cover rubber portion
A_b	effective area of bolt
A_e	overlap area between the top and bottom elastomer area of isolator
A_{free}	load-free area of isolator
A_{load}	loaded area of isolator
A_p	area of the lead plug for a lead rubber bearing
a	side length of square elastomeric isolator, excluding cover rubber thickness, or length in longitudinal direction of rectangular isolator, excluding cover rubber thickness
a_e	length of the shorter side of the rectangular isolator, including cover rubber thickness
a'	length in longitudinal direction of the rectangular isolator, including cover rubber thickness
B	effective width for bending of flange
b	length in transverse direction of the rectangular isolator, excluding cover rubber thickness
b'	length in transverse direction of the rectangular isolator, including cover rubber thickness
c	distance from centre of bolt hole to effective flange section
D'	outer diameter of circular isolator, including cover rubber
D_f	diameter of flange
d_i	inner diameter of reinforcing steel plate
d_k	diameter of bolt hole
d_0	outer diameter of reinforcing steel plate
E_{ap}	apparent Young's modulus of bonded rubber layer
E_c	apparent Young's modulus corrected, if necessary, by allowing for compressibility
E_c^s	apparent Young's modulus corrected for bulk compressibility depending on its shape factor (S_1)
E_∞	bulk modulus of rubber
E_0	Young's modulus of rubber
F_u	tensile force on isolator by uplift
G	shear modulus
$G_{\text{eq}}(\gamma)$	equivalent linear shear modulus at shear strain
H	height of elastomeric isolator, including mounting flange
H_n	height of elastomeric isolator, excluding mounting flange
h_{eq}	equivalent damping ratio
$h_{\text{eq}}(\gamma)$	equivalent damping ratio as a function of shear strain
K_d	post-yield stiffness (tangential stiffness after yielding of lead plug) of lead rubber bearing
K_h	shear stiffness
K_i	initial shear stiffness
K_p	shear stiffness of lead plug inserted in lead rubber bearing
K_r	shear stiffness of lead rubber bearing before inserting lead plug
K_t	tangential shear stiffness
K_v	compressive stiffness
L_f	length of one side of a rectangular flange
M	resistance to rotation
M_f	moment acting on bolt
M_r	moment acting on isolator
n	number of rubber layers
n_b	number of fixing bolts

Table 1 (continued)

Symbol	Description
P	compressive force
P_0	design compressive force in absence of seismic action effects
$P_{\max}$	maximum compressive force including seismic action effects
$P_{\min}$	minimum compressive force including seismic actions effects
P_{Tb}	tensile force at break of isolator
Q	shear force
Q_b	shear force at break
Q_{buk}	shear force at buckling
Q_d	characteristic strength
S_1	first shape factor
S_2	second shape factor
T	temperature
T_0	standard temperature, 23 °C or 27 °C; where specified tolerance is ± 2 °C, T_0 is standard laboratory temperature
T_r	total rubber thickness, given by $T_r = n \times t_r$
t_r	thickness of one rubber layer
t_{r1}, t_{r2}	thickness of rubber layer laminated on each side of plate
t_s	thickness of one reinforcing steel plate
t_0	thickness of outside cover rubber
$U(\gamma)$	function giving ratio of characteristic strength to maximum shear force of a loop
V	uplift force
v	loading velocity
W_d	energy dissipated per cycle
X	shear displacement
X_0	design shear displacement
X_b	shear displacement at break
X_{buk}	shear displacement at buckling
X_s	shear displacement due to quasi-static shear movement
$X_{\max}$	maximum shear displacement
X_d	shear displacement due to dynamic shear movement
Y	compressive displacement
Z	section modulus of flange
α	coefficient of linear thermal expansion
γ	shear strain
γ_0	design shear strain
γ_a	upper limit of the total of design strains on elastomeric isolators
γ_b	shear strain at break
γ_c	local shear strain due to compressive force
γ_d	shear strain due to dynamic shear movement
$\gamma_{\max}$	maximum design shear strain during earthquake
γ_r	local shear strain due to rotation
γ_s	shear strain due to quasi-static shear movement
γ_u	ultimate shear strain
δ_H	horizontal offset of isolator

Table 1 (continued)

Symbol	Description
δ_v	difference in isolator height measured between two points at opposite extremes of the isolator
ε	compressive strain of rubber
ε_{cr}	creep strain
ε_T	tensile strain of isolator
ε_{Tb}	tensile-break strain of isolator
ε_{Ty}	tensile-yield strain of isolator
ζ	ratio of total height of rubber and steel layers to total rubber height
θ	rotation angle of isolator about the diameter of a circular bearing or about an axis through a rectangular bearing
θ_a	rotation angle of isolator in the longitudinal direction (a)
θ_b	rotation angle of isolator in the transverse direction (b)
λ	correction factor for calculation of stress in reinforcing steel plates
η	correction factor for calculation of critical stress
κ	correction factor for apparent Young's modulus according to hardness
$\Sigma\gamma$	total local shear strain
ρ_R	safety factor for roll-out
ρ_T	safety factor for tensile force
σ	compressive stress in isolator
σ_0	design compressive stress
σ_B	tensile stress in bolt
σ_b	bending stress in flange
σ_{bf}	allowable bending stress in steel
σ_{cr}	critical stress in isolator
σ_f	allowable tensile stress in steel
σ_{max}	maximum compressive stress
σ_{min}	minimum compressive stress
σ_{nom}	for building: nominal long-term compressive stress recommended by manufacturer
σ_s	tensile stress in reinforcing steel plate
σ_{sa}	allowable tensile stress in steel plate
σ_{sy}	yield stress of steel for flanges and reinforcing steel plates
σ_{su}	tensile strength of steel for flanges and reinforcing steel plates
σ_t	tensile stress
σ_{te}	allowable tensile stress in isolator
τ_B	shear stress in bolt
τ_f	allowable shear stress in steel
ϕ	factor for computation of buckling stability
ξ	factor for computation of critical stress

5 Classification

5.1 General

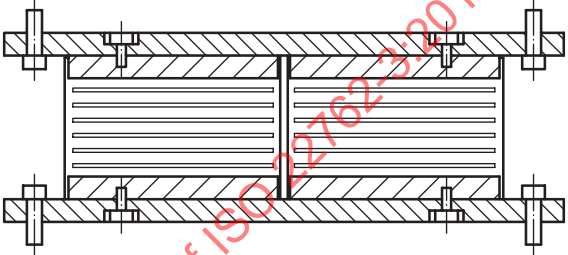
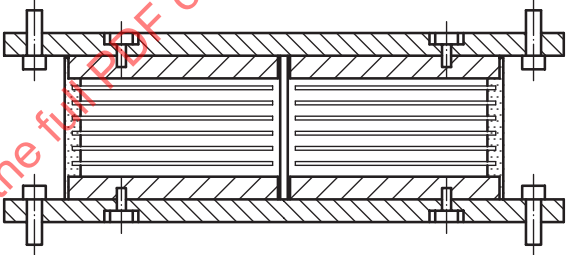
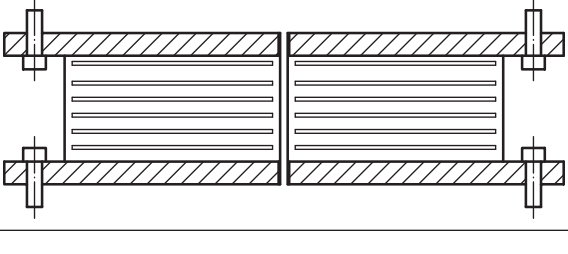
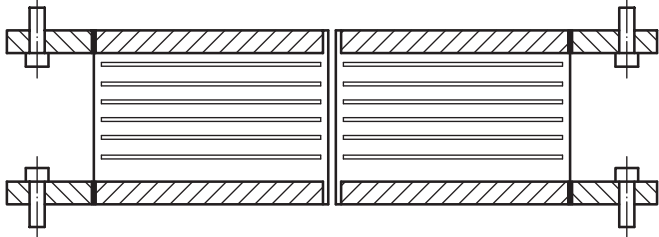
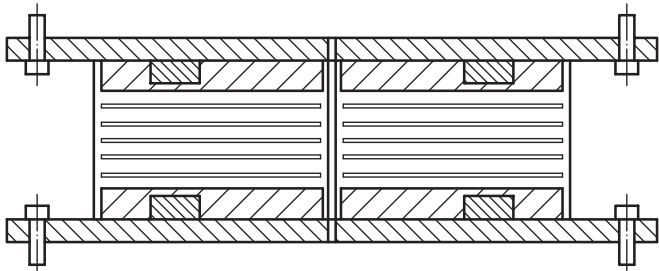
Elastomeric isolators are classified by construction, their ultimate properties and tolerances on their performance.

5.2 Classification by construction

Elastomeric isolators are classified by construction, as shown in [Table 2](#).

Other methods not listed in [Table 2](#) may be used to fix flanges to the laminated rubber, if the resulting construction has adequate strength to resist the shear forces and bending moments due to shear deflection. Furthermore, such constructions shall be capable of resisting tension if the elastomeric isolator is designed for uplift.

Table 2 — Classification by construction

Type	Construction	Illustration
Type I	Mounting flanges are bolted to connecting flanges, which are bonded to the laminated rubber. Cover rubber is added before curing of isolator.	
	Mounting flanges are bolted to connecting flanges, which are bonded to the laminated rubber. Cover rubber is added after curing of isolator.	
Type II	Mounting flanges are directly bonded to the laminated rubber.	
Type III	Isolators without mounting flanges, connected to base by either recess rings or dowell pins.	 Recess connection
		 Dowell connection

5.3 Classification by tolerance on shear properties

Elastomeric isolators are classified by tolerance on shear properties, as shown in [Table 3](#).

Table 3 — Classification by tolerance of shear properties

Class	Individual	Global
S-A	±15 %	±10 %
S-B	±25 %	±20 %

6 Requirement

6.1 General

Elastomeric isolators for buildings and the materials used in manufacture shall meet the requirements specified in this clause. For test items (see [Table 4](#)) that have no specific required values, the manufacturer shall define the values and inform the purchaser prior to production.

The standard temperature for determining the properties of elastomeric isolators is 23 °C or 27 °C in accordance with prevailing International Standards. However, it is advisable to establish a range of working temperatures taking into consideration actual environmental temperatures and possible changes in temperatures at the work site where the elastomeric isolators are installed.

Table 4 — Test pieces for type testing

Properties	Test item	Test piece	
		Scale	Minimum number
Compressive properties	Compressive stiffness	Full-scale only	3
Shear properties ^a	Shear stiffness	Full-scale only	3
	Equivalent damping ratio		
	Post-yield stiffness (for LRB)		
	Characteristic strength (for LRB)		
Tensile properties	Tensile fracture strength	Scale B	3
	Tensile yield strength		
Dependency of shear properties	Shear strain dependency ^a	Full-scale only	3
	Compressive stress dependency ^a	Full-scale only	3
	Frequency dependency	Scale A, STD, SBS	3
	Repeated loading dependency ^a	Scale B	3
	Temperature dependency	Scale A, STD, SBS	3
Dependency of compressive properties	Shear strain dependency	Scale B	3
	Compressive stress dependency		3
Ultimate properties	Shear displacement capacity ^b	Scale B	3
Durability	Ageing	Scale A, STD, SBS	2
	Creep	Scale A	2
Scale A: Scaling such that, for a circular bearing, diameter ≥ 150 mm, for a rectangular bearing, side length ≥ 100 mm and, for both types, rubber layer thickness $\geq 1,5$ mm and thickness of reinforcing steel plates $\geq 0,5$ mm. Scale B: Scaling such that, for a circular bearing, diameter ≥ 500 mm, for a rectangular bearing, side length ≥ 500 mm and, for both types, rubber layer thickness $\geq 1,5$ mm and thickness of reinforcing steel plates $\geq 0,5$ mm. Minimum scale factor 0,5. Scale C: Scaling such that, for a circular bearing, diameter ≥ 600 mm, for a rectangular bearing, side length ≥ 500 mm, and both types, rubber layer thickness $\geq 1,5$ mm and thickness of reinforcing steel plates $\geq 0,5$ mm., second shape factor is 7 or more (for pure breaking). STD: Standard test piece [see Tables 10 and 11 of ISO 22762-1:2018]. SBS: Shear-block test piece specified in ISO 22762-1:2018, 5.8.3 With LRB, SBS shall only be used for ageing tests. ^a If double-shear test configuration used, 3 tests involving 3 test-pieces shall be performed. The test pieces shall be paired such that the properties of individual test-pieces can be obtained. ^b If double-shear test configuration used, 2 tests shall be performed.			

Some of these properties may be determined using one of the standard test pieces detailed in Tables 10 and 11 in ISO 22762-1:2018. The standard test pieces are used for non-specific product tests, such as testing in the development of new materials and products.

6.2 Type tests and routine tests

6.2.1 Testing to be carried out on elastomeric isolators is classified into “type tests” and “routine tests”.

6.2.2 Type tests shall be conducted either to ensure that project design parameters have been achieved (in which case the test results shall be submitted to the structural engineer for review prior to production) or to verify isolator performance and material properties during development of the product. The test

piece for each type test shall be full-scale or one of the options specified in [Table 4](#). The test piece shall not have been subjected to any previous test programme. The tests shall be performed on test pieces not subjected to any scragging, unless the production isolators are to be supplied after scragging. In that case, the test pieces shall be subjected to the same scragging procedure as the production isolators.

6.2.3 Previous type test results may be substituted, provided the following conditions are met.

- a) Isolators are fabricated in a similar manner and from the same compound and adhesive.
- b) All corresponding external and internal dimensions are within 10 % of each other. Flange plates are excluded.
- c) First and second shape factors are equal to or larger than those in previous tests.
- d) The test conditions, such as maximum and minimum vertical load applied in the ultimate property test (see [6.5.7](#)), are more severe.

Routine tests are carried out during production for quality control. Sampling is allowed for routine testing for projects with agreement between structural engineer and manufacturer. Sampling shall be conducted randomly and cover not less than 20 % of the production of any isolator design. For a given project, tests shall cover not less than four test pieces for each size and not less than 20 test pieces in total.

If isolators are supplied after scragging, the routine test shall be performed on scragged isolators.

6.3 Functional requirements

Elastomeric isolators for buildings are designed and manufactured to have the performance characteristics required so that they deform in all directions with the proper stiffness (with damping, if required) during an earthquake.

In the application of elastomeric isolators, attention shall be paid to the following points.

- a) The isolators shall be installed horizontally between the structure and foundation.
- b) Once installed, the isolators shall not be subjected to a constant shear force.
- c) When isolators are to be installed under relatively flexible columns, the rotation at the top of the isolator caused by bending deformation shall be carefully considered.
- d) Exposed steel surfaces, such as the surfaces of mounting flanges, shall be properly painted or galvanized to prevent rusting.
- e) Proper maintenance shall be carried out on installed isolators to prevent any abnormalities such as distortion, cracks or rust occurring.
- f) Fire protection of the isolators may be required.
- g) The seismic gap shall be maintained at all times.

6.4 Design compressive force and design shear displacement

6.4.1 The design stress and strain of an isolator are defined by the following relationships with the design force and the displacement.

$$\sigma_0 = \frac{P_0}{A}, \sigma_{\max} = \frac{P_{\max}}{A}, \sigma_{\min} = \frac{P_{\min}}{A}$$

$$\gamma_0 = \frac{X_0}{T_r}, \gamma_{\max} = \frac{X_{\max}}{T_r}$$

6.4.2 The design compressive forces, P_0 , and maximum and minimum compressive forces, respectively $P_{\max}$ and $P_{\min}$, and the design shear displacements X_0 and the maximum shear displacement $X_{\max}$ for an isolator shall be provided by the structural engineer. If the P_0 , $P_{\max}$, $P_{\min}$, X_0 and $X_{\max}$ are not known at the time of type testing, the design stress and design strain to be used for testing can be determined as follows:

$$\sigma_0 = \sigma_{\text{nom}}, \sigma_{\max} = 2\sigma_{\text{nom}}$$

where σ_{nom} , $\sigma_{\min}$, γ_0 and $\gamma_{\max}$ are determined by the manufacturer.

6.5 Performance requirements

6.5.1 General

The isolators shall be tested and the results recorded using the specified test methods. They shall satisfy all of the requirements listed below. The test items are summarized in [Table 5](#), which indicates those type tests that are optional, where a material test piece may substitute an isolator, and the tests to be performed as routine tests. The standard value obtained from the tests shall be reported. Double-shear configuration testing (see ISO 22762-1:2018, 6.2.2.2) can be employed with the approval of the structural engineer.

Table 5 — Tests on isolators

Property	Test item	Test method	Routine test	Type test
Compressive properties	Compressive stiffness	ISO 22762-1:2018, 6.2.1, method 2	X	X
Shear properties	Shear stiffness Equivalent damping ratio Post-yield stiffness (for LRB) Characteristic strength (for LRB)	ISO 22762-1:2018, 6.2.2	X	X
Tensile properties	Tensile fracture strength Tensile yield strength	ISO 22762-1:2018, 6.5	N/A	Opt.
Dependency of shear properties	Shear strain dependency	ISO 22762-1:2018, 6.3.1	N/A	X
	Compressive stress dependency	ISO 22762-1:2018, 6.3.2	N/A	X
	Frequency dependency	ISO 22762-1:2018, 6.3.3	N/A	X(m)
	Repeated loading dependency	ISO 22762-1:2018, 6.3.4	N/A	X
	Temperature dependency	ISO 22762-1:2018, 6.3.5 5.8	N/A	X(m)
Dependency of compressive properties	Shear strain dependency	ISO 22762-1:2018, 6.3.6	N/A	Opt.
	Compressive stress dependency	ISO 22762-1:2018, 6.3.7	N/A	Opt.
Shear displacement capacity	Breaking strain, buckling strain	ISO 22762-1: 2018, 6.4	N/A	X
	Roll-out strain			
	Ultimate property diagram (UPD)	ISO 22762-3:2018, Annex B	N/A	Opt.
Durability	Property change	ISO 22762-1:2018, 6.6.1	N/A	X(m)
	Creep	ISO 22762-1:2018, 6.6.2	N/A	X
X: Test to be conducted with isolators. X(m): Test can be conducted either with isolators or with shear-block test pieces. N/A: Not applicable. Opt.: Optional; the structural engineer can request that any optional test has to be carried out.				

6.5.2 Compressive properties

6.5.2.1 General requirements

The compressive stiffness, K_v , shall be within ± 30 % of the design value.

6.5.2.2 Test piece

The test piece shall be a full-scale isolator for the type test and a production isolator for the routine test.

6.5.2.3 Test condition

As specified in ISO 22762-1:2018, 6.2.1.5.2, method 2, cyclic loading with the design compressive stress $\sigma_0 \pm 30$ % shall be carried out for three cycles.

The compressive stiffness, K_v , shall be computed from the third cycle.

The standard test temperature, T_0 , is 23 °C or 27 °C. If the test is carried out at a different temperature, the result shall be corrected to the value of the property at T_0 by an appropriate method.

6.5.3 Shear properties

6.5.3.1 General requirements

The following properties shall be within the specified range of design value corresponding to the adopted tolerance class specified in 5.3.

The test items specified for each type of isolator are shown in Table 6 (see Annex F). The properties measured for LRB may be selected from either L-1 or L-2, as given in Table 6 below.

Table 6 — Shear property test items

Isolator type	Test item	
LNR	Shear stiffness, K_h	
HDR	Shear stiffness, K_h , equivalent damping ratio, h_{eq}	
LRB	L-1	Shear stiffness K_h , equivalent damping ratio h_{eq}
	L-2	Post-yield stiffness K_d , characteristic strength Q_d

6.5.3.2 Test piece

The test piece shall be a full-scale isolator for the type test and a production isolator for the routine test.

6.5.3.3 Test conditions

6.5.3.3.1 The test piece shall be loaded with the design compressive stress, σ_0 .

6.5.3.3.2 The cyclic loading of the design shear strain, γ_0 , or of the shear strain which corresponds to $\gamma = 100\%$ shall be carried out for three cycles.

6.5.3.3.3 The required properties shall be computed from the third cycle.

If the test is performed at a frequency different from the design isolation frequency, the result shall be corrected to the design frequency or to 0,5 Hz by an appropriate method.

The standard test temperature is 23 °C or 27 °C. If the test is carried out at a different temperature, the result shall be corrected to the value of the property at T_0 by an appropriate method.

6.5.4 Tensile properties

6.5.4.1 General requirements

The tensile properties shall be within the specified range.

6.5.4.2 Test piece

The test piece shall be a full-scale isolator or a scale model, as specified in Table 4.

6.5.4.3 Test conditions

The test conditions shall be as specified in 6.5 of ISO 22762-1:2018.

6.5.5 Dependencies of shear properties

6.5.5.1 Shear strain dependency

6.5.5.1.1 General requirements

The change in each property over the range of test shear strains with respect to the value of the property at the design shear strain, γ_0 (or another reference strain, if employed in the shear property test in 6.5.3), shall be within the specified range.

6.5.5.1.2 Test piece

The test piece shall be a full-scale isolator.

6.5.5.1.3 Test conditions

The shear properties shall be determined at strains between 50 % and the maximum shear strain, $\gamma_{\max}$, at strain intervals of 50 %; the interval between the last two test strains shall be at least 50 %. The change in the property, normalized using the value corresponding to the design strain, shall be determined. Tests can also be performed at 10 % and 20 % shear strain.

6.5.5.2 Compressive stress dependency

6.5.5.2.1 General requirements

As the compressive stress varies, the change in the shear properties with respect to the value of the property at the design stress, σ_0 , shall be within the specified range (see Annex D).

The test piece shall be a full-scale isolator.

6.5.5.2.2 Test conditions

The shear strain amplitude shall be γ_0 .

The shear properties shall be determined at 0, $0,5\sigma_0$, $1,0\sigma_0$, $1,5\sigma_0$, $2,0\sigma_0$ and the maximum tensile stress, if applicable, and the change in the property, normalized using the value corresponding to the design strain, shall be determined.

6.5.5.3 Frequency dependency

6.5.5.3.1 General requirements

The frequency dependency shall be within the specified range.

6.5.5.3.2 Test piece

The test piece shall be a full-scale isolator, a scale model, a standard test piece or a shear-block test piece, as specified in Table 4.

6.5.5.3.3 Test conditions

The shear strain amplitude shall be γ_0 .

Other test conditions shall be as specified in 6.3.3 of ISO 22762-1:2018.

6.5.5.4 Repeated loading dependency

6.5.5.4.1 General requirements

The repeated loading dependency shall be within the specified range.

6.5.5.4.2 Test piece

The test piece shall be a full-scale isolator or a scale model, as specified in [Table 4](#).

6.5.5.4.3 Test conditions

The shear strain amplitude shall be γ_0 .

Other test conditions shall be as specified in 6.3.4 of ISO 22762-1:2018.

6.5.5.5 Temperature dependency

6.5.5.5.1 General requirements

The temperature dependency shall be within the specified range.

6.5.5.5.2 Test piece

The test piece shall be a full-scale isolator, a scale model, a standard test piece, or a shear-block test piece, as specified in [Table 4](#).

6.5.5.5.3 Test conditions

The shear strain amplitude shall be γ_0 .

Other test conditions shall be as specified in 6.3.5 of ISO 22762-1:2018.

6.5.6 Dependencies of compressive properties

6.5.6.1 Shear strain dependency

6.5.6.1.1 General requirements

The shear strain dependency of the compressive properties shall be within the specified range.

6.5.6.1.2 Test piece

The test piece shall be a full-scale isolator or a scale model, as specified in [Table 4](#).

6.5.6.1.3 Test conditions

The test conditions shall be as specified in 6.3.6 of ISO 22762-1:2018.

6.5.6.2 Compressive stress dependency

6.5.6.2.1 General requirements

The compressive stress dependency of the compressive properties shall be within the specified range.

6.5.6.2.2 Test piece

The test piece shall be a full-scale isolator or a scale model, as specified in [Table 4](#).

6.5.6.2.3 Test conditions

The shear strain amplitude shall be γ_0 .

Other test conditions shall be as specified in 6.3.7 of ISO 22762-1:2018.

6.5.7 Shear displacement capacity

6.5.7.1 General requirements

The isolator shall be loaded to the maximum shear displacement under both the maximum and the minimum axial loads. The isolator shall not suffer any failure, such as instability, breaking or roll-out during the test. The variation in axial load used depends on the isolator type (see [5.2](#)) and shall be as specified in [Table 7](#).

Table 7 — Axial stress for each isolator type

Isolator type	Axial stress used in test
Type I, Type II	Maximum stress $\sigma_{\max}$ Minimum stress $\sigma_{\min}$ (when in tension)
Type III	Maximum stress $\sigma_{\max}$ Minimum stress $\sigma_{\min}$

6.5.7.2 Test piece

The test piece shall be a full-scale isolator or a scale model, as specified in [Table 4](#).

6.5.7.3 Test conditions

The test conditions shall be as specified in 6.4 of ISO 22762-1:2018. For Type I and Type II isolators, a test at $P_{\min}$ can be carried out using the procedure given in 6.5 of ISO 22762-1:2018, the shear strain applied shall be $\gamma_{\max}$ and the isolator shall not fail at a load of less than $P_{\min}$.

6.5.8 Durability

6.5.8.1 Change in properties on ageing

6.5.8.1.1 General requirements

The change on ageing in the shear properties, K_h , and, if required, h_{eq} , shall be within the specified range.

6.5.8.1.2 Test piece

The test piece shall be a full-scale isolator, a scale model, a standard test piece or a shear-block test piece, as specified in [Table 4](#). If production isolators are to be supplied after scragging, the test pieces shall be subjected to the same scragging procedure as the production isolators, and the durability test carried out directly after scragging.

6.5.8.2 Creep

6.5.8.2.1 General requirements

The total creep strain [see ISO 22762-1:2018, 6.6.2.6 b) for definition] shall be less than 10 % after 60 years.

6.5.8.2.2 Test piece

The test piece shall be a full-scale isolator or a scale model, as specified in [Table 4](#).

6.6 Rubber material requirements

6.6.1 General

The rubber materials used in the manufacture of elastomeric isolators shall be tested as required in [Table 8](#). The standard value obtained from the tests shall be reported. The test results shall be properly recorded to verify that the specified requirements are satisfied. Recommended minimum values for inner rubber material are given in [Annex C](#). The frequency of each required test shall be determined in accordance with the manufacturer's quality control.

6.6.2 Tensile properties

The following are general requirements for testing tensile properties.

- a) Tensile strength: not less than design value.
- b) Elongation at break: not less than design value.
- c) Other recommended minimum values are given in [Annex C](#).

6.6.3 Properties after ageing in air

6.6.3.1 General requirements

The following are general requirements for testing tensile properties.

- a) Change in tensile strength: within ± 25 %.
- b) Change in elongation at break: maximum -50 %.

EXAMPLE Original 600 %, elongation at break after ageing not less than 300 %.

Table 8 — Test items for rubber material

Property	Test items	Test method in ISO 22762-1:2018	Routine test		Type test	
			Inner rubber	Cover rubber	Inner rubber	Cover rubber
Tensile properties	Tensile strength	5.3	X	X	X	X
	Elongation at break		X	X	X	X
	100 % modulus		Opt.	Opt.	X	X
Air ageing properties	Tensile strength	5.4	Opt.	Opt.	X	X
	Elongation at break		Opt.	Opt.	X	X
	100 % modulus		N/A	N/A	X	X
Hardness	Hardness	5.5	Opt.	Opt.	Opt.	Opt.
Adhesion properties	90° peel strength	5.6	Opt.	N/A	X	X
Shear properties	Shear modulus	5.8	Opt.	N/A	X	N/A
	Damping ratio		Opt.	N/A	X	N/A
	Temperature dependency of shear modulus and damping ratio		N/A	N/A	Opt.	N/A
	Fracture strain	5.9	N/A	N/A	Opt.	N/A
	Fracture stress		N/A	N/A	Opt.	N/A
Brittleness point	Brittleness temperature	5.10	N/A	N/A	Opt.	X ^a
Ozone resistance	Observation of cracks	5.11	N/A	X	N/A	X
Low-temperature crystallization	Hardness	5.12	N/A	N/A	X ^b	X ^b
X: Test to be carried out. N/A: Not applicable. Opt.: Optional; the structural engineer can request that any optional test had to be carried out. ^a Test is required for service temperatures below 0 °C. ^b Test is required unless elastomer is not susceptible to crystallization in range of service temperatures (see ISO 22762-1:2018, 5.12).						

6.6.3.2 Test conditions

6.6.3.2.1 The recommended conditions for natural rubber- and chloroprene-based isolators are

- natural rubber: 70 °C for seven days, and
- chloroprene rubber: 100 °C for 72 h.

6.6.3.2.2 Other conditions can be used by agreement between the structural engineer and the manufacturer. Test conditions and requirements for other elastomers shall be recommended by the manufacturer and agreed to by the structural engineer.

6.6.4 Hardness

6.6.4.1 The design value of IRHD shall be ±5.

6.6.4.2 Hardness may be used as a quality control test and for other purposes when a relationship has been established with the appropriate shear modulus. Hardness should not be used for primary design purposes.

6.6.5 Ozone resistance

The following conditions shall be met when testing the ozone resistance of an elastomeric isolator.

- a) Test conditions: 50 pphm (50 mPa), 20 % elongation, 40 °C for 96 h.
- b) There shall be no cracks on cover rubber.

6.6.6 Other properties

Properties other than the ones listed above shall be determined by the test methods listed in [Table 5](#). Each test result shall be within the tolerances specified prior to testing.

6.7 Dimensional requirements

Typical dimensions of elastomeric isolators are given in [Table 9](#) as a guide for the design of elastomeric isolators. Sizes other than those given in [Table 9](#) are permissible as long as the remaining requirements are satisfied.

Table 9 — Typical dimensions of elastomeric isolators

Dimensions <i>a</i> or <i>d</i> ₀ mm	Thickness mm		Second shape factor <i>S</i> ₂	Inner diameter <i>d</i> _i mm			
	Rubber layer <i>t</i> _r				Steel plate <i>T</i> _s		
	min.	max.	min.	min.	max.		
400	2,0	5,0	2,0	3,0	<i>d</i> ₀ 6		
450	2,0	5,5		3,0			
500	2,5	6,0		3,0			
550	2,5	7,0		3,0			
600	3,0	7,5		3,0			
650	3,0	8,0		3,0			
700	3,5	9,0		3,0			
750	3,5	9,5	2,5	3,0		<i>d</i> ₀ 5	
800	4,0	10,0		3,0			
850	4,0	10,5		3,5			
900	4,5	11,0		3,5			
950	4,5	11,0		3,5			
1 000	4,5	11,0	3,0	3,5	<i>d</i> ₀ 5		
1 050	5,0	11,0		3,5			
1 100	5,5	11,0		3,5			
1 150	5,5	12,0		3,5			
1 200	6,0	12,0		4,0			
1 250	6,0	13,0		4,0			
1 300	6,5	13,0	4,0	4,0			<i>d</i> ₀ 5
1 350	6,5	14,0		4,0			
1 400	7,0	14,0		4,0			
1 450	7,0	15,0		4,0			
1 500	7,0	15,0		4,0			

NOTE 1 d_0 , a , d_i are the dimensions of the reinforcing steel plate.

NOTE 2 The inside diameter of lead rubber bearings is $\leq \frac{d_0}{4}$, $\leq \frac{a}{4}$.

NOTE 3 a is the side length of square elastomeric isolators.

NOTE 4 The stability of isolators is increased by making S_2 larger and the diameter of the inner hole smaller (see [Annex E](#)).

6.8 Requirements on steel used for flanges and reinforcing plates

Steel plates used for flanges, end and inner plates shall meet the strength requirements specified in [Table 10](#).

ISO 630(all parts) or any other International Standard where yield strength and fracture strength are specified, shall be used, as long as the steel specified satisfies the requirements given in [Table 10](#) or is approved by the structural engineer.

Table 10 — Hot- and cold-rolled sheet and strip for flanges and reinforcing steel plates

Designation	Yield stress σ_{sy} N/mm ²			Tensile strength σ_{su} N/mm ²
	Thickness of steel plate t mm			
	$t \leq 16$	$16 < t \leq 40$	$40 < t$	
SS400	$\sigma_{sy} \geq 245$	$\sigma_{sy} \geq 235$	$\sigma_{sy} \geq 215$	$400 \leq \sigma_{su} \leq 510$
SM490A	$\sigma_{sy} \geq 325$	$\sigma_{sy} \geq 315$	$\sigma_{sy} \geq 295$	$490 \leq \sigma_{su} \leq 610$

6.9 Requirement on lead material for LRB

Purity of lead material for the plug of LRB shall be 99,99 % or more.

7 Design rules

7.1 General

The elastomeric isolators shall be designed to meet the relevant provisions of this clause, in the serviceability limit state determined from the design compressive force, the restraint of wind force and the ultimate limit state caused by an earthquake.

In the serviceability limit state, the design shall be such that the isolators will not suffer damage that would affect their proper functioning, or incur excessive maintenance costs during their intended life.

In the ultimate limit state, the strength and stability of the isolators shall be adequate to withstand the ultimate design forces and movements of the structure (see [Annex D](#)).

7.2 Shape factor

7.2.1 First shape factor

7.2.1.1 The first shape factor, S_1 , of a rubber layer is defined as the ratio of the effective loaded area, A_{load} , to the free surface area, A_{free} , as in [Formula \(1\)](#):

$$S_1 = \frac{A_{load}}{A_{free}} \quad (1)$$

a) For isolators without holes.

$$\text{Circular isolators: } S_1 = \frac{d_0}{4t_r} \quad (2)$$

$$\text{Square isolators: } S_1 = \frac{a}{4t_r} \quad (3)$$

b) For isolators with holes.

$$\text{Circular isolators: } S_1 = \frac{d_0 - d_i}{4t_r} \quad (4)$$

$$\text{Square isolators: } S_1 = \frac{4a^2 - \pi d_i^2}{4t_r (4a + \pi d_i)} \quad (5)$$

7.2.1.2 If the holes are adequately plugged with rubber or lead, the isolator can be treated as having no holes.

7.2.2 Second shape factor

The second shape factor, S_2 , is defined as the ratio of the effective width to the total thickness of the inner rubber, as in a) and b) [Formulae (6) and (7)] below.

a) For circular isolators, S_2 is expressed as Formula (6):

$$S_2 = \frac{d_0}{T_r} \quad (6)$$

b) For square isolators, S_2 is expressed as Formula (7):

$$S_2 = \frac{a}{T_r} \quad (7)$$

7.3 Compression and shear properties

7.3.1 Compressive stiffness

7.3.1.1 The compressive stiffness, K_v , is given by Formula (8):

$$K_v = \frac{E_c \times A}{T_r} \quad (8)$$

where E_c is as given in Annex E.

7.3.1.2 The compressive displacement and compressive strain of an elastomeric isolator are given by Formulae (9) and (10):

$$Y = \frac{P}{K_v} \quad (9)$$

$$\varepsilon_c = \frac{Y}{T_r} \quad (10)$$

7.3.2 Shear stiffness and equivalent damping ratio

7.3.2.1 The shear stiffness is given by Formula (11):

$$K_h = G \frac{A}{T_r} \quad (11)$$

7.3.2.2 When the shear strain dependency on shear modulus is considered, the shear stiffness is given by Formula (12):

$$K_h = G_{eq}(\gamma) \times \frac{A}{T_r} \quad (12)$$

where $G_{eq}(\gamma)$ is determined as indicated in Annex E.

7.3.2.3 The shear modulus $G_{eq}(\gamma)$ for any γ shall be determined from the results of a cyclic dynamic-loading test, using either a full-scale or scale model isolator, under shear strain and under compressive stress, σ . If there is a significant difference between the compressive stress, σ , applied during the

measurement of $G_{eq}(\gamma)$ and the design stress, σ_0 , $G_{eq}(\gamma)$ shall be determined under design conditions, taking into account the effect of compressive stress. The following expression may be used to predict the stiffness under any compressive stress, σ , using $G_{eq}(\gamma)$ determined from a shear-block test piece:

$$K_h = G_{eq}(\gamma) \left\{ 1 - \left(\frac{\sigma}{\sigma_{cr}} \right)^2 \right\} \frac{A}{T_r} \quad (13)$$

where σ_{cr} is calculated using [Formula \(17\)](#).

7.3.2.4 The shear strain, γ , at a given displacement is calculated using [Formula \(14\)](#):

$$\gamma = \frac{X}{T_r} \quad (14)$$

where X is the horizontal displacement.

7.3.2.5 For LRB, K_h is related to K_d and Q_d as expressed in [Formula \(15\)](#):

$$K_h = \frac{K_d \times X + Q_d}{X} \quad (15)$$

7.3.2.6 The energy dissipated per cycle, W_d , is measured from the loop, and the equivalent damping ratio, h_{eq} , is given by [Formula \(16\)](#):

$$h_{eq} = \frac{1}{2\pi} \times \frac{W_d}{K_h \times X^2} \quad (16)$$

7.4 Ultimate properties

7.4.1 Stability at zero displacement

7.4.1.1 The critical stress, σ_{cr} , is defined as the compressive stress, at zero displacement, under which the isolator loses its stability. It is calculated using [Formula \(17\)](#):

$$\sigma_{cr} = \frac{\pi}{4} \times \xi \times S_2 \sqrt{E_b \times G} \quad (17)$$

where E_b is the apparent Young's modulus for bending and is given by [Formula \(18\)](#):

$$\frac{1}{E_b} = \frac{1}{E_0 (1 + \frac{2}{3} \kappa S_1^2)} + \frac{1}{E_\infty} \quad (18)$$

where (see [Table E.1](#) for values of κ)

G is the shear modulus at $\gamma = 100$ %;

ξ is a coefficient dependent on the cross-sectional shape of the isolator and is defined as:

$\xi = 1$ for circular sections;

$\xi = \frac{2}{\sqrt{3}}$ for square sections.

7.4.1.2 For lead rubber bearings, G represents the shear modulus of the rubber portion excluding the lead plug.

7.4.1.3 The isolator shall be designed with a safety factor ρ_c which meets the following requirement with respect to σ_{cr} and the design stress σ_0 :

$$\sigma_0 \leq \frac{1}{\rho_c} \sigma_{cr} \quad (19)$$

where the safety factor, ρ_c , shall be provided by the structural engineer.

7.4.2 Stability and failure under large shear displacements

The relationship between compressive stress and shear strain in the ultimate state shall be expressed, for an isolator, in the form of an ultimate property diagram (UPD) (see [Annex B](#) and [Annex C](#)). The structural engineer may request UPD.

7.4.3 Roll-out properties of isolators with recessed or dowelled connections (Type III)

7.4.3.1 The roll-out properties of isolators with either recessed or dowelled connections shall be checked.

7.4.3.2 The effect of a compressive force and a shear force on an isolator is shown in [Figure 1](#). At roll-out, the following relationship applies (see Reference [1]):

$$P \times (d - X) = Q \times H \quad (20)$$

(for a circular isolator)

For a square isolator, d is replaced by a .

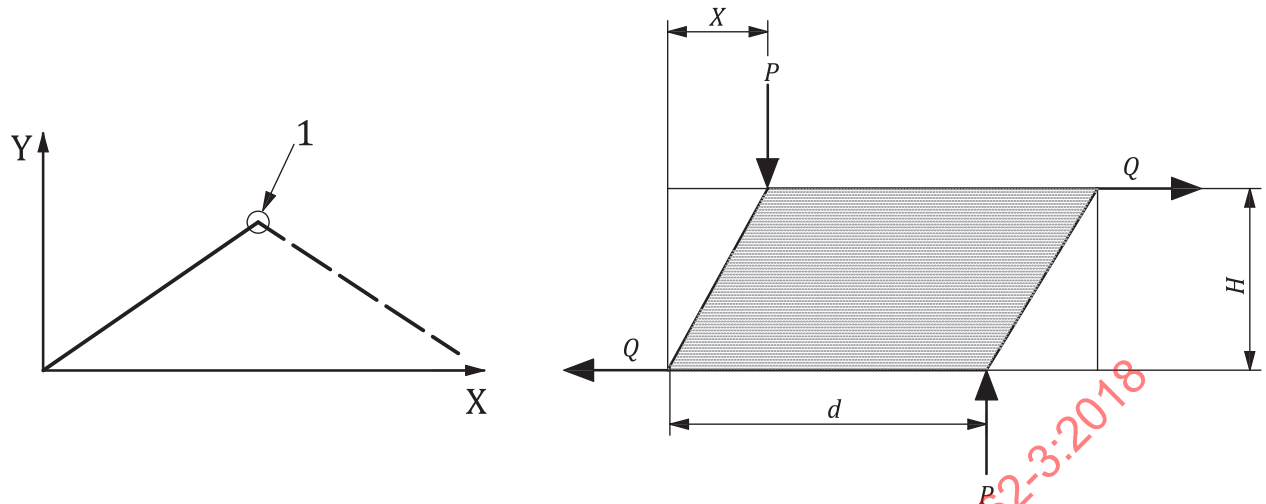
7.4.3.3 From the above relationship, an isolator with recessed or dowelled connections shall satisfy the following requirement with respect to minimum design compressive stress, σ_{min} , and maximum design strain, γ_{max} , including the safety factor, ρ_R :

$$\gamma_{max} \leq \frac{S_2 \times \sigma_{min}}{\zeta \times G + \sigma_{min}} \times \frac{1}{\rho_R} \quad (21)$$

where

$$\zeta = \frac{H}{T_r}$$

The safety factor, ρ_R , shall be provided by the structural engineer.

**Key**

X shear displacement

Y shear force

1 roll-out

Figure 1 — Roll-out properties of isolators with either recessed or dowelled connections**7.4.4 Tensile properties**

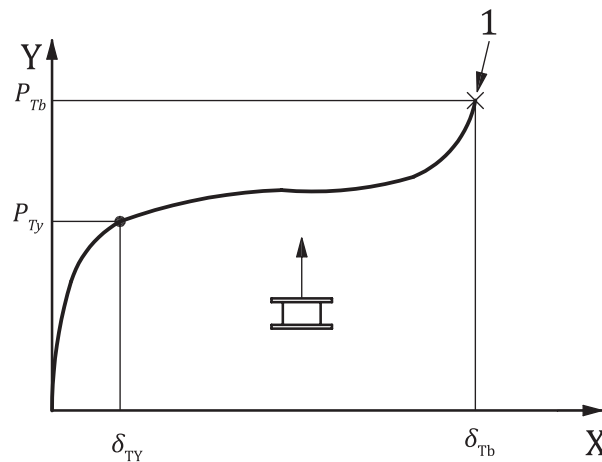
7.4.4.1 If the minimum force at maximum displacement, $X_{\max}$, is an uplift force, F_u , shall satisfy the following requirement:

$$F_u \leq F_{Ty} \times \frac{1}{\rho_T} \quad (22)$$

where ρ_T is a safety factor which shall be provided by the structural engineer.

7.4.4.2 The typical relationship between tensile force and tensile displacement for isolators is shown in [Figure 2](#).

7.4.4.3 The tensile force, P_{Ty} , of the design isolator, as indicated in [Figure 2](#), shall be determined from the force-displacement curve, as specified in 6.5 of ISO 22762-1:2018.



Key

- X tensile displacement
- Y tensile force
- 1 breaking point

Figure 2 — Tensile properties of elastomeric isolators

7.4.4.4 If the stress and strain are calculated from the tensile force and tensile displacement, the values obtained only represent mean values of the non-uniformly distributed stress and strain, which are significantly affected by flange bending.

7.5 Reinforcing steel plates

The reinforcing steel plates in elastomeric isolators shall be designed to satisfy the following requirement:

$$\sigma_s = 2\lambda \times \frac{P_{\max} \times t_r}{A \times t_r} \leq \sigma_{sa} \quad (23)$$

where λ is as given in [Annex A](#), and σ_{sa} is specified by the structural engineer.

7.6 Connections

Connections, including fixing bolts and flanges, shall be designed for maximum and minimum compressive load and maximum shear displacement during an earthquake. The strength calculation shall be carried out by an appropriate method, such as that given in [Annex H](#).

8 Manufacturing tolerances

8.1 General

Dimensional tolerances for elastomeric isolators for buildings shall be as specified below in this subclause.

Product dimensions shall be specified at a standard laboratory temperature of T_0 [$= (23 \text{ or } 27)^\circ\text{C} \pm 5^\circ\text{C}$]. Measurements made at a different temperature shall be corrected to a standard laboratory temperature. Dimensions shall be measured at least 24 h after curing of bearing. The cooling time shall be defined

according to the product size and shall be based on measurement of the internal temperature of the product or another appropriate method.

Larger bearings may need more than 24 h after curing.

8.2 Measuring instruments

The following can be used as measuring instruments:

- a) vernier calipers;
- b) calipers;
- c) height gauge;
- d) limit gauge, to be calibrated with a gauge certified to match the upper and lower tolerance limits;
- e) straight rule;
- f) other instruments, such as a tape measure.

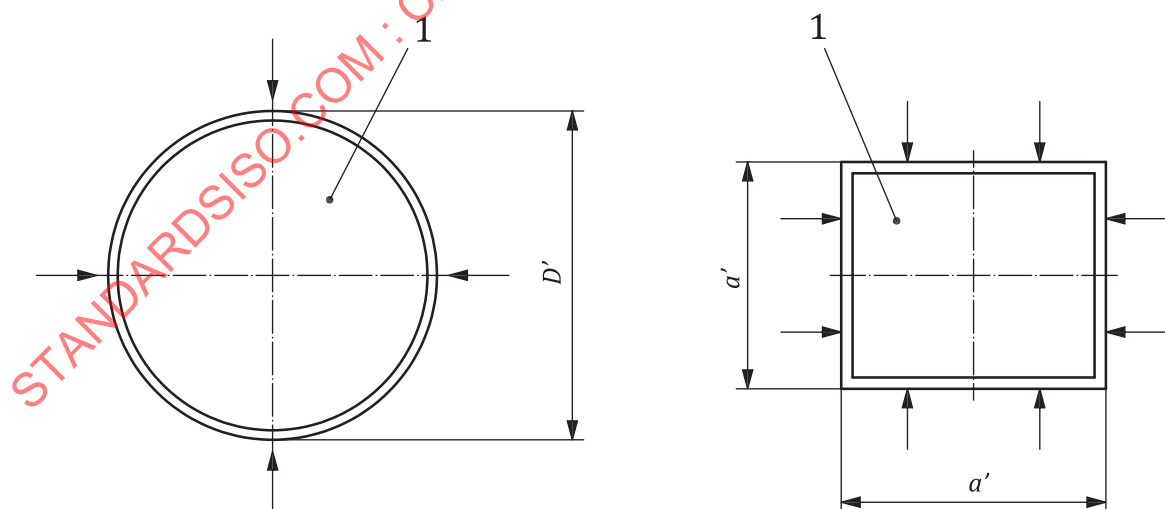
8.3 Plan dimensions

8.3.1 Measurement method

The measurement method to determine the plan dimensions of circular and rectangular isolators shall be as follows.

- a) For circular isolators: the plan dimensions shall be determined by measuring the diameter at two different locations.
- b) For rectangular isolators: the plan dimensions shall be measured at two positions on each side.

Examples of measurement points are as given in [Figure 3](#) below.



Key

1 reinforcing steel plate

NOTE The measurement points are indicated by arrows.

Figure 3 — Example of plan dimension measurement positions

8.3.2 Tolerances

Tolerances on the diameter D' and side length a' are specified for Type I, Type II and dowelled Type III isolators in [Table 11](#) according to the nominal dimensions of the product.

For recessed Type III isolators, the tolerance shall be ± 2 mm, or $\pm 0,4$ % of the plan dimension, whichever is greater.

Table 11 — Tolerances on plan dimensions of isolators

Nominal plan dimensions (D' , a') mm		Tolerance
Above	Maximum	
—	500	± 5 mm
500	1 500	± 1 %
1 500	—	± 15 mm

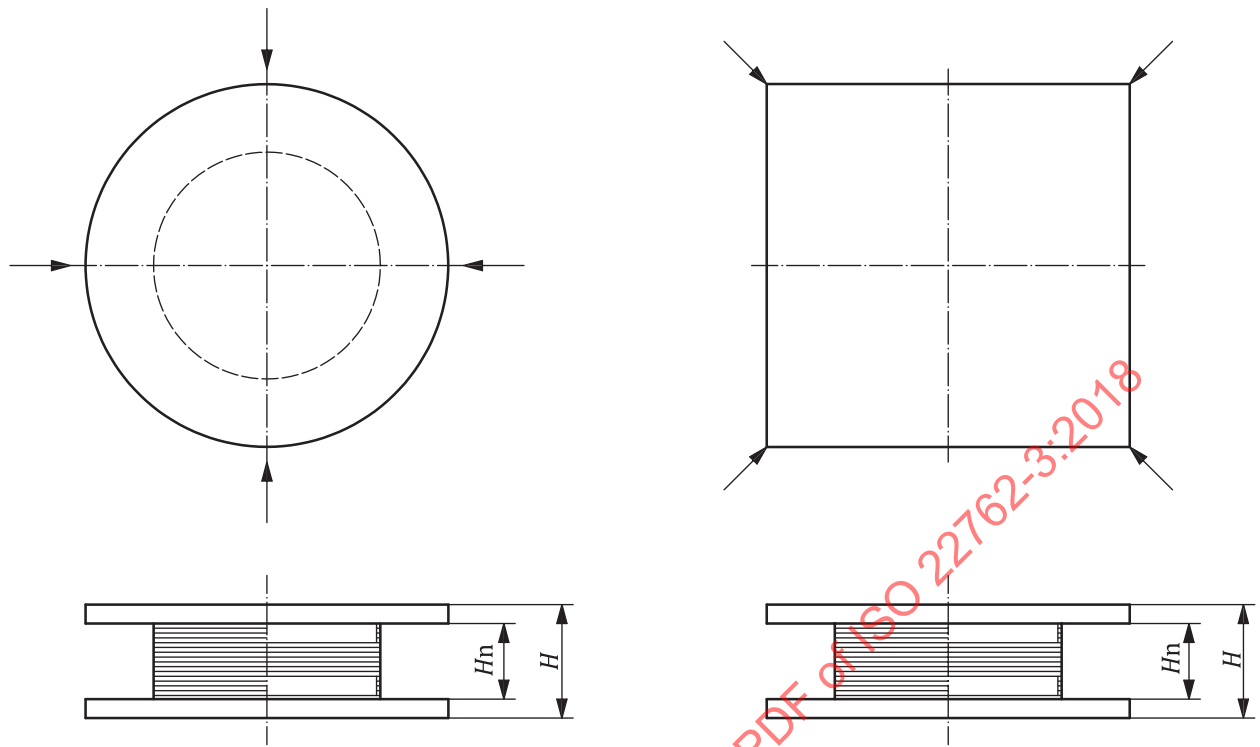
8.4 Product height

8.4.1 Measurement method

The method to measure the height of circular and rectangular isolators shall be as follows.

- For circular isolators: the height shall be measured at the four points where two straight lines at right angles to each other which pass through the centre of the circular cross-section intersect the outer circumference (see [Figure 4](#)).
- For rectangular isolators: the height (H or H_0) shall be measured at each of the four corners (see [Figure 4](#)).

The product height shall be taken as the arithmetic mean of the four measured values.



NOTE The measurement points are indicated by arrows.

Figure 4 — Height measurement positions

8.4.2 Tolerances

The tolerance on the product height shall be $\pm 1,5\%$ or $\pm 6,0$ mm, whichever is smaller.

8.5 Flatness

8.5.1 Measurement method

The flatness is the maximum difference in height at four points on the circumference of the isolator (see Figure 5). The measurement positions shall be the same as those for product height (H or H_n) measurements.

$$\text{Flatness } \psi = \left| \frac{\delta_v}{D_f} \right| \text{ or } \left| \frac{\delta_v}{D'} \right| \quad (24)$$

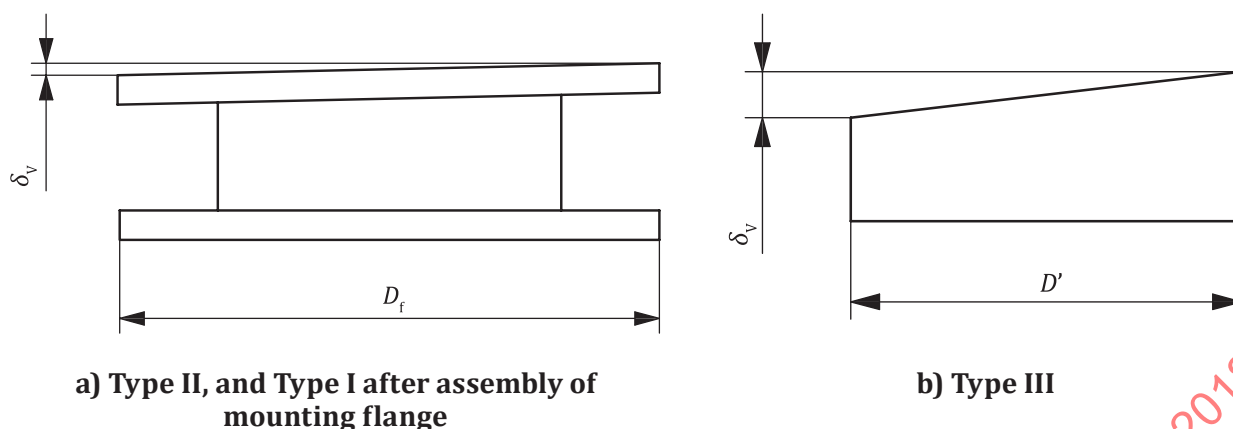


Figure 5 — Measurement of flatness

8.5.2 Tolerances

The tolerance on the flatness of isolators shall be as follows:

$$|\Psi| \leq \pm 0,25 \% \quad (25)$$

and

$$|\delta_v| \leq 3,0 \text{ mm} \quad (26)$$

8.6 Horizontal offset

For the measurement method, the horizontal offset is measured between the top and bottom edges of the product at two positions (see Figure 6). For rectangular isolators, the positions shall be on adjacent sides, and for circular isolators, on orthogonal diameters.

The horizontal offset, δ_H , of elastomeric isolators shall be as follows:

$\delta_H \leq 5,0 \text{ (mm)}$ or $2,5 \% \text{ of } H$, whichever is smaller.

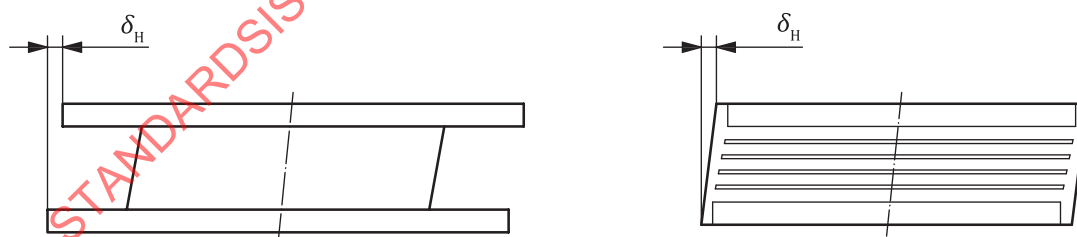


Figure 6 — Measurement of horizontal offset

8.7 Plan dimensions of flanges

The tolerances on the plan dimensions of flanges shall be as specified in [Table 12](#). Plan demensions of flanges is shown in Figure 7 below.

Table 12 — Tolerances on flange diameter and side length

Dimensions in millimetres

Thickness		D_f (or L_f) < 1 000	$1\ 000 \leq D_f$ (or L_f) < 3 150	$3\ 150 \leq D_f$ (or L_f) < 6 000
Above	Maximum			
6	27	$\pm 2,0$	$\pm 2,5$	$\pm 3,0$
27	50	$\pm 2,5$	$\pm 3,0$	$\pm 3,5$
50	100	$\pm 3,5$	$\pm 4,0$	$\pm 4,5$

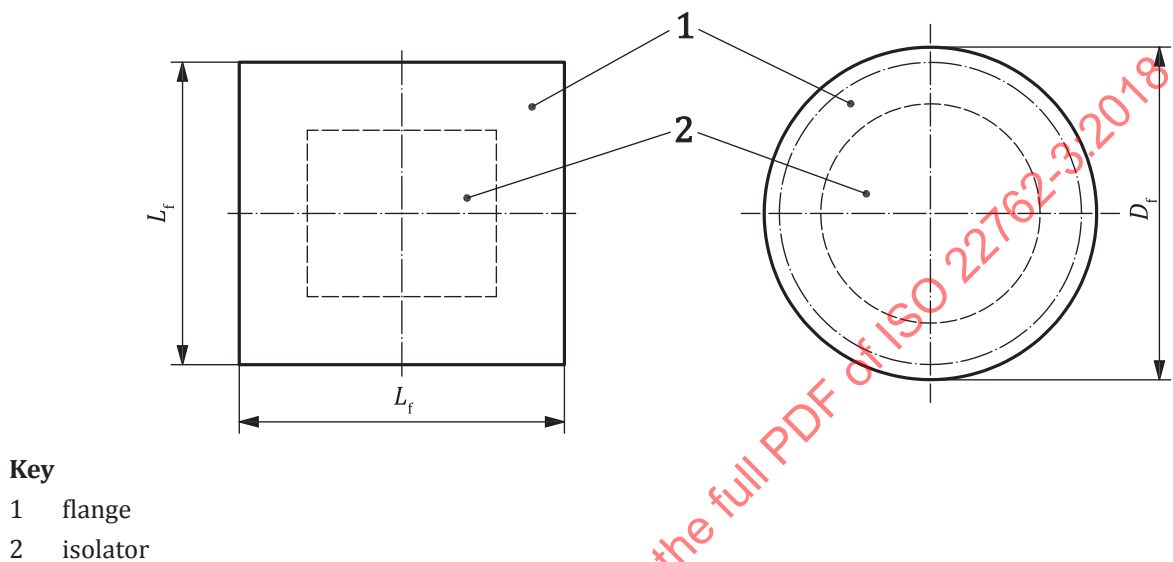


Figure 7 — Measurement of plan dimensions of flanges

8.8 Flange thickness

The tolerances on flange thickness shall be as specified in [Table 13](#).

Table 13 — Tolerances on thickness of flange (connecting plate for Type I)

Dimensions in millimetres

Nominal dimension		D_f (or L_f) < 1 600	$1\ 600 \leq D_f$ (or L_f) < 2 000
Above	Maximum		
16,0	25,0	$\pm 0,65$	$\pm 0,75$
25,0	40,0	$\pm 0,70$	$\pm 0,80$
40,0	63,0	$\pm 0,80$	$\pm 0,95$
63,0	100,0	$\pm 0,90$	$\pm 1,10$

8.9 Tolerances on positions of flange bolt holes

The tolerances on the positions of flange bolt holes, including the positions of tapped holes on the connecting plate, shall be as specified in [Table 14](#).

Table 14 — Tolerances on positions of flange bolt holes

Dimensions in millimetres

Nominal dimension		Tolerance
Above	Maximum	
400	1 000	±0,8
1 000	2 000	±1,2
2 000	—	±2,0

9 Marking and labelling

9.1 General

Marking and labelling are required for the purpose of identification of a product and its properties and to ensure traceability of the product's history after installation. Therefore, marking and labelling are considered to be very important for quality control of a product.

9.2 Information to be provided

The following information shall be provided for the marking and labelling of elastomeric isolators.

- a) The manufacturer's name or corporate emblem.
- b) The type of elastomeric isolator. Types of elastomeric isolator shall be identified as in [Table 15](#).

Table 15 — Identification of elastomeric isolators according to types and designations

Type	Designation
Linear natural rubber bearing	LNR
High-damping rubber bearing	HDR
Lead rubber bearing	LRB

- c) The serial number or manufacturing number.
- d) The size (optional).

EXAMPLE 1 Cross-sectional area circular and diameter 800 mm: size code D-800.

EXAMPLE 2 Cross-sectional area square and side length 800 mm × 800 mm: size code 800 × 800 or S-800.

9.3 Additional requirements

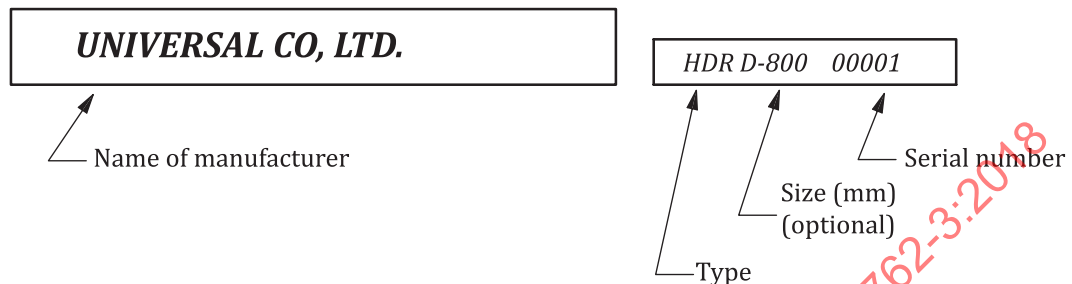
Additional requirements for marking and labelling include the following.

- a) Marking shall be on lateral surfaces.
- b) Marking shall be water-resistant and abrasion-resistant.
- c) Marking shall be large enough to be easily identified. The size of the characters shall be larger than 5 mm in width and height.

9.4 Marking and labelling examples

Marking may be on one line as in Example 1 or on two lines as in Example 2 shown in this subclause.

EXAMPLE 1



EXAMPLE 2



10 Test methods

Test methods prescribed in this clause shall be in accordance with ISO 22762-1.

11 Quality assurance

A quality assurance programme to ensure consistent manufacturing of the isolators, including, but not limited to, preparation of reinforcing steel plates, uniformity of the thickness of the reinforcing steel plates and uniformity of the vulcanized rubber layers, shall be proposed by the manufacturer and approved by the structural engineer.

Annex A (normative)

Tensile stress in reinforcing steel plate

A.1 Method for checking strength of reinforcing steel plate

The tensile stress in the reinforcing steel plates shall satisfy [Formula \(A.1\)](#):

$$\sigma_s = 2\lambda \times \frac{P_{\max} \times t_r}{A \times t_r} \leq \sigma_{sa} \quad (\text{A.1})$$

where λ is a correction factor, including a safety margin, obtained from experimental data as follows:

- a) for plates without holes: $\lambda = 1,0$;
- b) for plates with holes ($A_p/A = 0,03$ to $0,1$): $\lambda = 1,5$.

A.2 Verification of [Formula \(A.1\)](#) by compressive failure testing of isolators

A.2.1 General

The test described in this clause was carried out to verify the applicability of [Formula \(A.1\)](#).

A.2.2 Test pieces

The test pieces used are described in [Table A.1](#). The test pieces were square, measuring 240 mm × 240 mm, the thickness of one rubber layer being 5,0 mm and the test pieces having six layers of laminated rubber. The thickness of the reinforcing steel plate was 2,3 mm made of SS400 mild steel (see [6.8](#)). One isolator had no hole in the steel plate (RB-1), whereas the other had four holes of diameter 34,5 mm which were plugged with lead cores (RB-2). Two isolators for each type (with/without hole) were subjected to the testing.

Table A.1 — Dimensional characteristics of test pieces

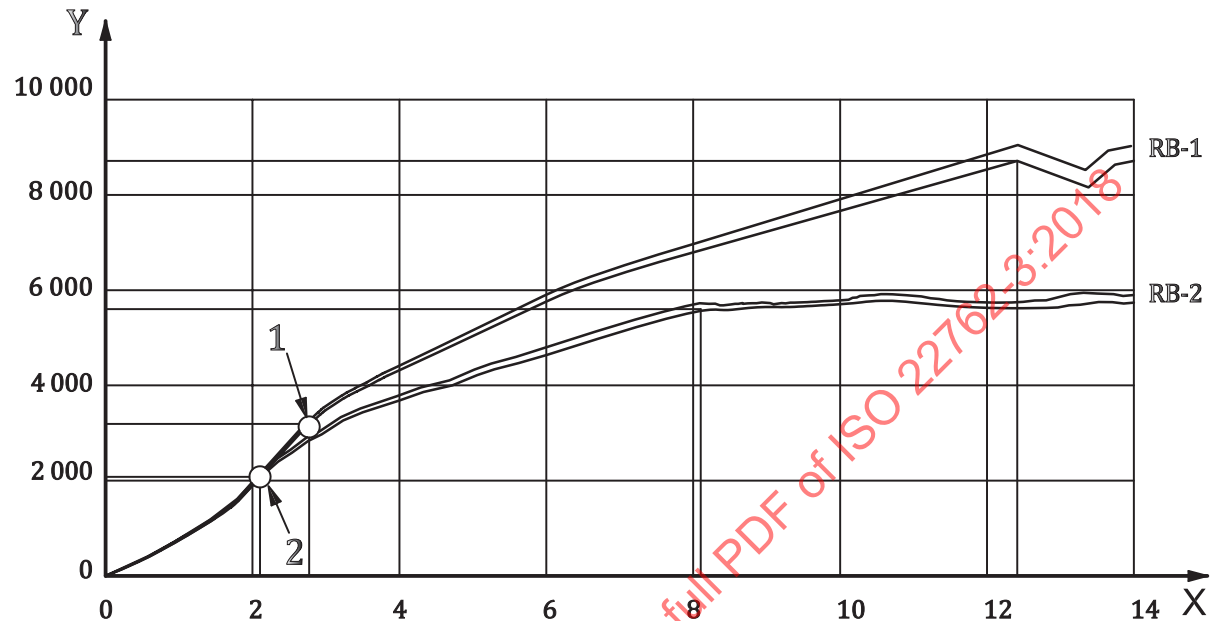
	RB-1	RB-2
Type	LNR	LRB
Plan dimension ($a \times a$), mm	240 × 240	
Hole diameter, d , mm	0	4 × 34,5
Thickness of one rubber layer, t_r , mm	5	
Number of layers	6	
Reinforcing plate thickness, t_s , mm	2,3	

A.2.3 Test conditions

Isolators were subjected to compressive loading until failure was indicated by the force-deflection curve. The horizontal displacement was maintained at zero during testing. The compressive loading rate was 32 kN/s.

A.2.4 Test results

A.2.4.1 Figure A.1 shows the plots of the force-deflection curve obtained during testing. The yield point of the plate was determined as the point on the curve where the second-order derivative of the curve was zero.



Key

- X compressive deflection, δ , expressed in millimetres
- Y compressive force, P , expressed in kilonewtons
- 1 yield point of plate for RB-1
- 2 yield point of plate for RB-2

Figure A.1 — Compressive force-deflection curve for isolator

A.2.4.2 The tensile stresses in the plates calculated from the compressive force at the observed yield point using [Formula \(A.1\)](#) are summarized in Table A.2.

Table A.2 — Summary of test results

	RB-1	RB-2	RB-1/RB-2
A Compressive force, P , at yield point, expressed in kN	3 200	2 100	0,66
B Compressive stress, σ , at yield point, expressed in N/mm ²	55,6	36,5	0,66
C Yield stress in plate, expressed in N/mm ² , computed from P and Formula (A.1)	241,6	237,9	1,016
D Design yield stress of plate, expressed in N/mm ²	235	235	—

A.2.4.3 Comparing the values of C and D in Table A.2, the applicability of [Formula \(A.1\)](#) can be seen to be verified.

For further details, see Reference [1].

Annex B **(normative)**

Determination of ultimate property diagram based on experimental results

B.1 Test piece

A scale model isolator may be used for the test. The model shall have a minimum layer thickness of 2 mm and a minimum diameter of 250 mm. The thickness of the reinforcing steel plates need not be scaled down if the scaled thickness is $<0,5$ mm.

B.2 Testing machine

A combined compression and shear testing machine shall be used.

The compressive load shall be controlled to maintain a constant load.

The vertical (compressive) load, horizontal load and horizontal displacement shall be measured using equipment with sufficient accuracy.

The load-deflection curve shall be recorded during testing.

B.3 Testing parameters

B.3.1 Compressive load

Different compressive loads corresponding to compressive stresses of 0 , σ , $0,5\sigma$ and $2,5\sigma$, where σ is the nominal compressive stress recommended by the manufacturer, shall be used.

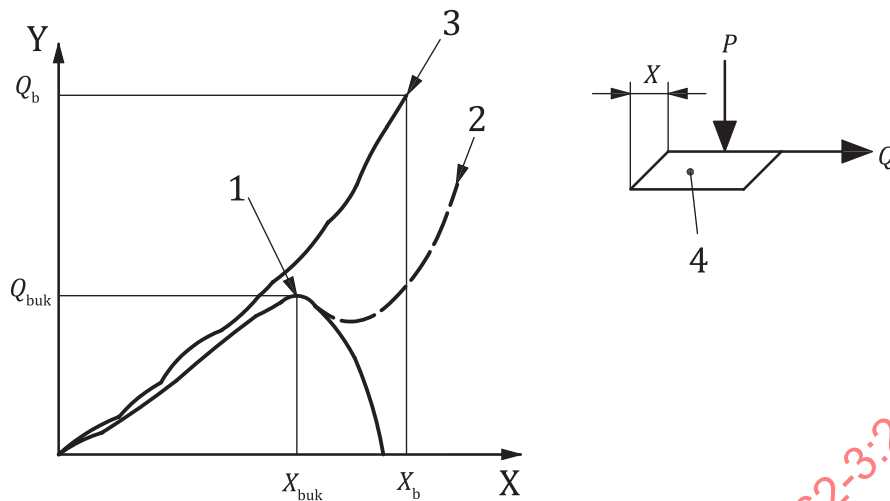
In order to obtain a more accurate load-deflection curve, loadings corresponding to compressive stresses of $1,5\sigma$ and $2,5\sigma$ are also recommended.

B.3.2 Compression-shear testing

Subject the isolator to static monotonic loading until breaking, buckling or roll-out occurs under the compressive stresses specified in [B.3.1](#). The horizontal displacement and load at break (X_b and Q_b), at buckling (X_{buk} and Q_{buk}) or at roll-out (X_{r0} and Q_{r0}) shall be determined from the result. If buckling, breaking or roll-out do not occur, the maximum displacement shall be considered as the ultimate property. Example of compressive-shear load test result to determine ultimate property is shown in Figure B.1.

B.3.3 Test temperature

The ambient temperature during the test is not specified but is required to be maintained at around 23 °C.

**Key**X shear deflection, X Y shear force, Q

1 buckling point

2 break

3 breaking point

4 rubber bearing

 P compressive load X_{buk} shear deflection at buckling point Q_{buk} shear force at buckling point X_b shear deflection at breaking point Q_b shear force at breaking point**Figure B.1 — Determination of ultimate properties****B.4 Interpretation of results**

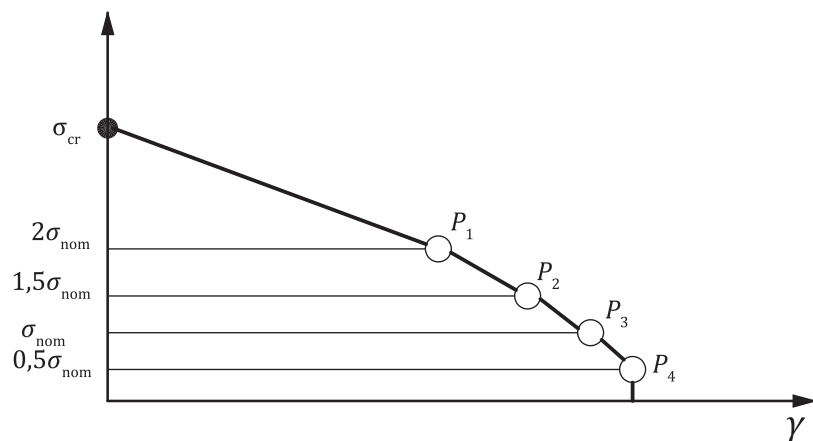
B.4.1 Plot the ultimate shear strain obtained in [B.3](#) against the compressive stress, as shown in [Figure B.2](#) (points P_1 , P_2 , P_3 and P_4).

B.4.2 Draw a curve through the plotted points. The compressive stress at zero shear strain (the critical stress, σ_{cr}) may be determined using [Formula \(B.1\)](#):

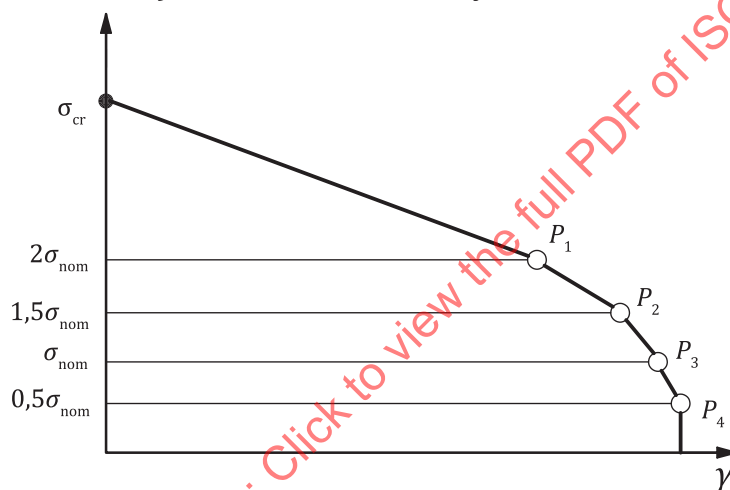
$$\sigma_{cr} = \frac{\pi}{4} \times \xi \times S_2 \sqrt{E_b \times G} \quad (\text{B.1})$$

(see [7.4.1](#))

B.4.3 The area enclosed by the curve and the X- and Y-axes on the graph shall be considered the stable range of the isolator under compressive-shear loading.



a) Isolator with relatively small S_2



b) Isolator with relatively large S_2

Figure B.2 — Ultimate property diagrams (UPDs) obtained by experiment

Annex C (informative)

Minimum recommended physical properties of rubber material

Examples of rubber material properties of elastomeric isolators, low-damping rubber bearings and high-damping rubber bearings, are shown in [Tables C.1](#) and [C.2](#).

Table C.1 — Properties of inner rubber materials for linear natural rubber bearings

Property	Test item	Unit	Shear modulus MPa (see ISO 22762-1:2018, 5.8)							Test method in ISO 22762-1:2018
			0,30	0,35	0,40	0,45	0,60	0,80	1,0	
Tensile properties	Tensile strength	MPa	≥12,0	≥14,0	≥14,0	≥15,0	≥15,0	≥20,0	≥20,0	5.3
	Elongation at break	%	≥650	≥600	≥600	≥600	≥500	≥500	≥500	
Hardness	Hardness	IRHD	30 ± 5	35 ± 5	35 ± 5	40 ± 5	45 ± 5	50 ± 5	65 ± 5	5.5
Adhesion properties	90° peel strength	N/mm	≥6	≥6	≥6	≥6	≥6	≥6	≥6	5.6
	Failure mode	—	Rubber failure	Rubber failure	Rubber failure	Rubber failure	Rubber failure	Rubber failure	Rubber failure	
Brittleness temperature	Brittleness temperature	°C	≤-40	≤-40	≤-40	≤-40	≤-40	≤-40	≤-40	5.10

Table C.2 — Properties of inner rubber materials for high-damping rubber bearings

Property	Test item	Unit	Shear modulus MPa (see ISO 22762-1:2018, 5.8)			Test method in ISO 22762-1:2018
			0,40	0,60	0,80	
Tensile properties	Tensile strength	MPa	≥8,0	≥8,0	≥10,0	5.3
	Elongation at break	%	≥650	≥650	≥650	
Hardness	Hardness	IRHD	(60 to 70) ± 5	(60 to 70) ± 5	(60 to 70) ± 5	5.5
Brittleness temperature	Brittleness temperature	°C	≤-40	≤-40	≤-40	5.10

NOTE The shear modulus is that for 100 % strain.

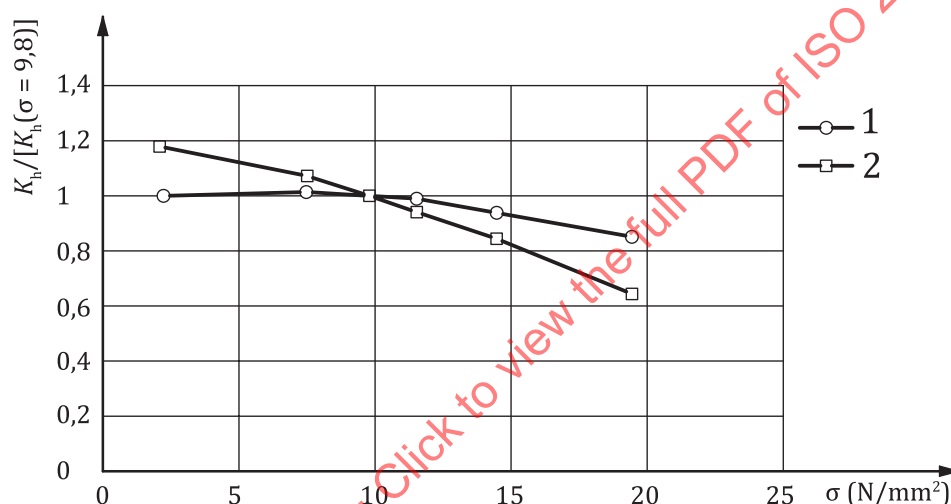
Annex D

(informative)

Effect of inner-hole diameter and second shape factor on shear properties

D.1 Effect of inner-hole diameter on compressive-stress dependency of shear stiffness

The inner-hole diameter of an isolator has a significant effect on the compressive stress dependency of the shear stiffness. The larger the inner-hole diameter, the larger the dependency, as shown in [Figure D.1](#), the data for which were obtained using test pieces with the properties given in [Table D.1](#).



Key

- 1 G 4,0-40
- 2 G 4,0-120

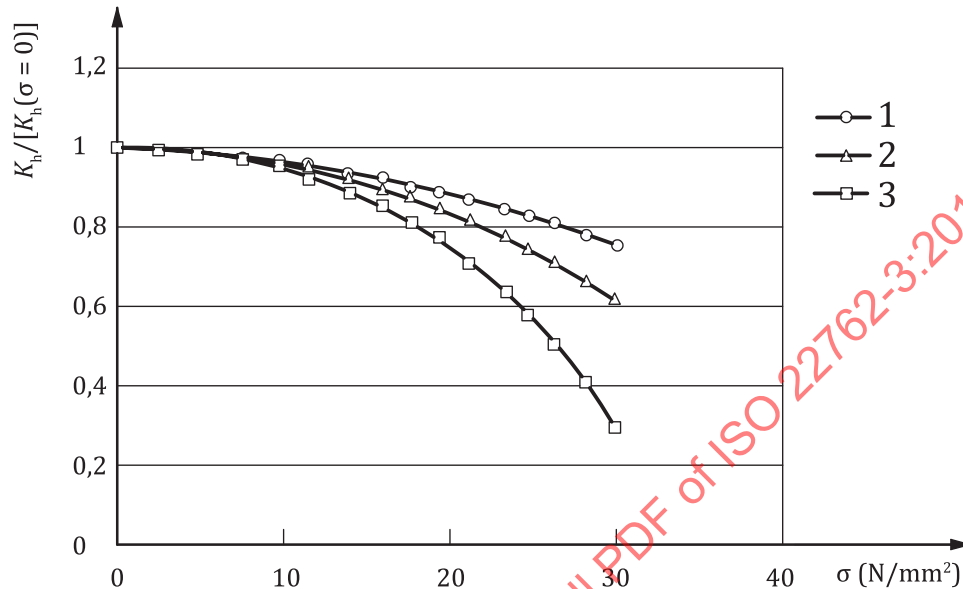
Figure D.1 — Compressive-stress dependency of shear stiffness of isolators with different inner-hole diameters

Table D.1 — Test pieces used

Property	Unit	G4,0-40	G4,0-120
G	MPa	0,39	0,39
d_o	mm	800	800
d_i	mm	40	120
d_i/d_o	—	0,05	0,15
t_r	mm	6,5	6,5
n_r	—	25	25
S_1	—	29,2	26,2
S_2	—	4,9	4,9

D.2 Effect of second shape factor on compressive-stress dependency of shear stiffness

The smaller the second shape factor, the larger the compressive stress dependency of the shear stiffness, as shown in [Figure D.2](#).



Key

1 $S_2 = 5,0$

2 $S_2 = 4,0$

3 $S_2 = 3,0$

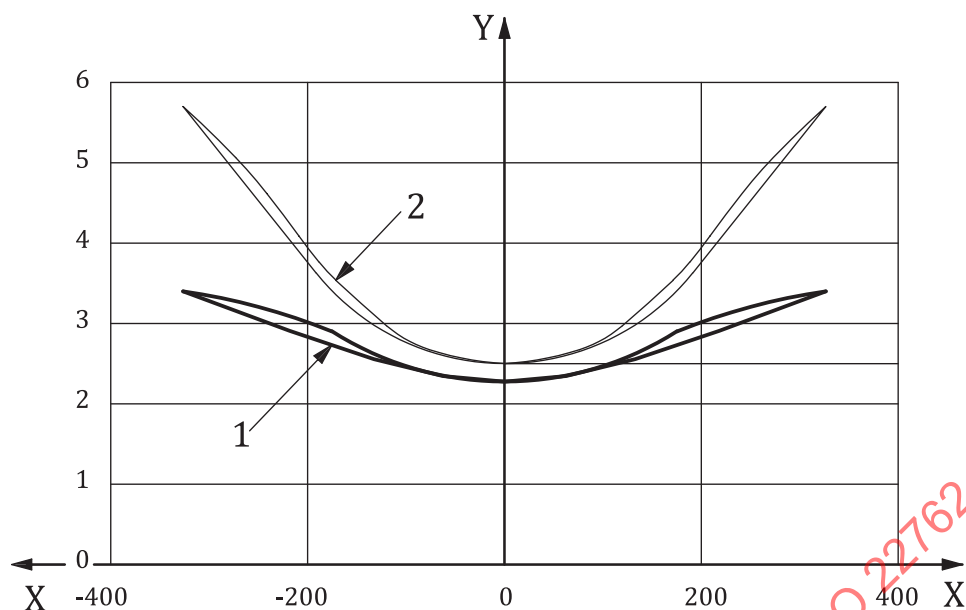
Test piece: $S_1 = 35$, $d_o = 225$ mm, $d_i = 0$ mm.

Figure D.2 — Compressive stress dependency of shear stiffness for various second shape factors

D.3 Effect of second shape factor on change in isolator height during compression-shear loading

As the inner-hole diameter becomes larger and/or the second shape factor smaller, the change in isolator height during compression-shear loading becomes larger.

[Figure D.3](#) shows the effect of inner-hole diameter on the change in isolator height during compression-shear loading.



Key

X shear displacement, expressed in millimetres

Y decrease in isolator height, expressed in millimetres

1 G 4,0-40

2 G 4,0-120

Test piece: same as that shown in [Table D.1](#).

Test conditions: $\sigma = 9,8 \text{ MPa}$, $\gamma = \pm 200 \text{ \%}$.

Figure D.3 — Effect of inner-hole diameter on the change in isolator height during compression-shear loading

Annex E (informative)

Determination of compressive properties of elastomeric isolators

E.1 The compressive (vertical) stiffness of an elastomeric isolator, K_v , is given by [Formula \(E.1\)](#):

$$K_v = \frac{A \times E_c}{n_r \times t_r} \quad (\text{E.1})$$

where

A is the cross-sectional area of the rubber bearing;

$n_r \times t_r$ is (number of layers) $\times$ (thickness of one layer), i.e. the total rubber height;

E_c is the apparent Young's modulus, corrected for the bulk modulus (compressibility).

E.2 E_c is calculated using [Formula \(E.2\)](#):

$$E_c = \left(\frac{1}{E_{ap}} + \frac{1}{E_\infty} \right)^{-1} \quad (\text{E.2})$$

E.3 Various formulae can be used to determine E_{ap} such as in [E.3.1](#) and [E.3.2](#).

E.3.1 Formula 1 (see References [\[1\]](#) and [\[2\]](#)):

$$E_{ap} = E_0 \times (1 + 2\kappa S_1^2) \quad (\text{E.3})$$

where

E_0 is Young's modulus of rubber (E_0 may be approximated as $3G$, where G is the shear modulus of rubber);

E_∞ is the bulk modulus of rubber;

κ is a correction factor;

S_1 is the first shape factor $\left(S_1 = \frac{d_o}{4t_r} \right)$;

d_o is the outer diameter of the isolator;

t_r is the thickness of one layer of rubber.

Examples of constants for several natural rubber compounds are given in [Table E.1](#). In practice, manufacturers apply their own constants for the design of isolators.

Table E.1 — Examples of values of the constant κ used in the design of elastomeric isolators

IRHD	E_0 MPa	G MPa	κ	E_∞ MPa
30	0,92	0,30	0,93	$1,00 \times 10^3$
40	1,50	0,45	0,85	$1,00 \times 10^3$
50	2,20	0,64	0,73	$1,03 \times 10^3$
60	5,34	1,06	0,57	$1,15 \times 10^3$
70	7,34	1,72	0,53	$1,27 \times 10^3$
NOTE See Reference [2].				

E.3.2 Formula 2:

$$E_{ap} = 3G_{eq}(\gamma) \times (1 + 2S_1^2) \quad (E.4)$$

where $G_{eq}(\gamma)$ is the shear modulus at the average shear strain γ produced by the compressive load.

γ may be estimated from the expression:

$$\gamma = \sqrt{6}S_1\varepsilon \quad (E.5)$$

where ε is the compressive strain on the rubber layer.

Neither of the formulae proposed here consider the non-linearity introduced when ε becomes greater than about 0,1.

E.4 E_0 and E_∞ may be determined by experiment, as follows:

$$\frac{1}{E_c} = \frac{1}{E_0} \times \frac{1}{1 + 2\kappa S_1^2} + \frac{1}{E_\infty} \quad (E.6)$$

When the compressive stiffness of isolators with various values of S_1 is measured and E_c is derived, $\frac{1}{E_c}$

and $\frac{1}{1 + 2\kappa S_1^2}$ can be plotted as shown in [Figure E.1](#).

The best straight line is fitted to the plotted points. The slope a of the curve and its intercept b with the Y-axis give $\frac{1}{E_0}$ and $\frac{1}{E_\infty}$. Any correction factor, κ , may be selected, as long as it does not affect the accuracy of the approximated line.

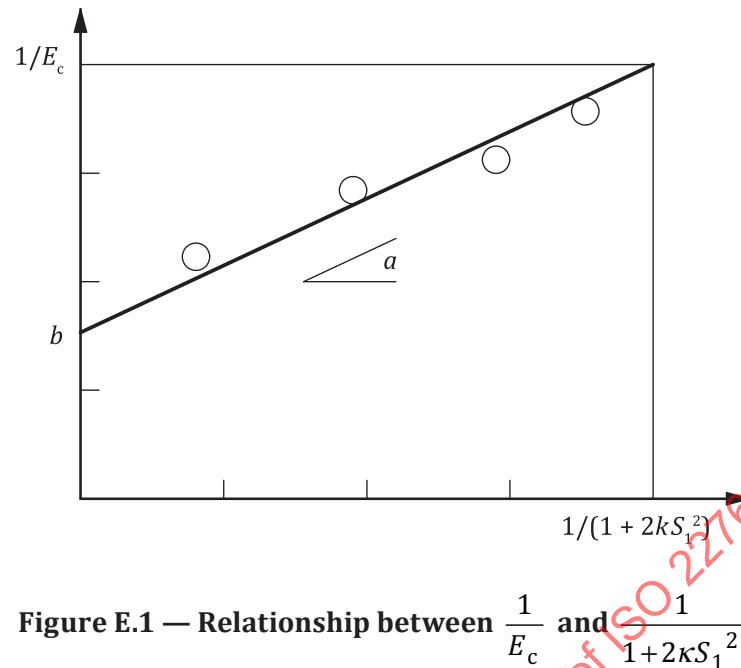


Figure E.1 — Relationship between $\frac{1}{E_c}$ and $\frac{1}{1 + 2\kappa S_1^2}$

For isolators with an unplugged central hole, formulae for the compressive stiffness are given in Reference [1]. Expressions for compressive stiffness based on shape factor, S_1 , modified to take account of a hole, might not give reliable results.

Annex F (informative)

Determination of shear properties of elastomeric isolators

F.1 Shear properties of linear natural rubber bearings

The shear stiffness, K_h , of LNR can be calculated from [Formula \(F.1\)](#):

$$K_h = G \frac{A}{T_r} \quad (\text{F.1})$$

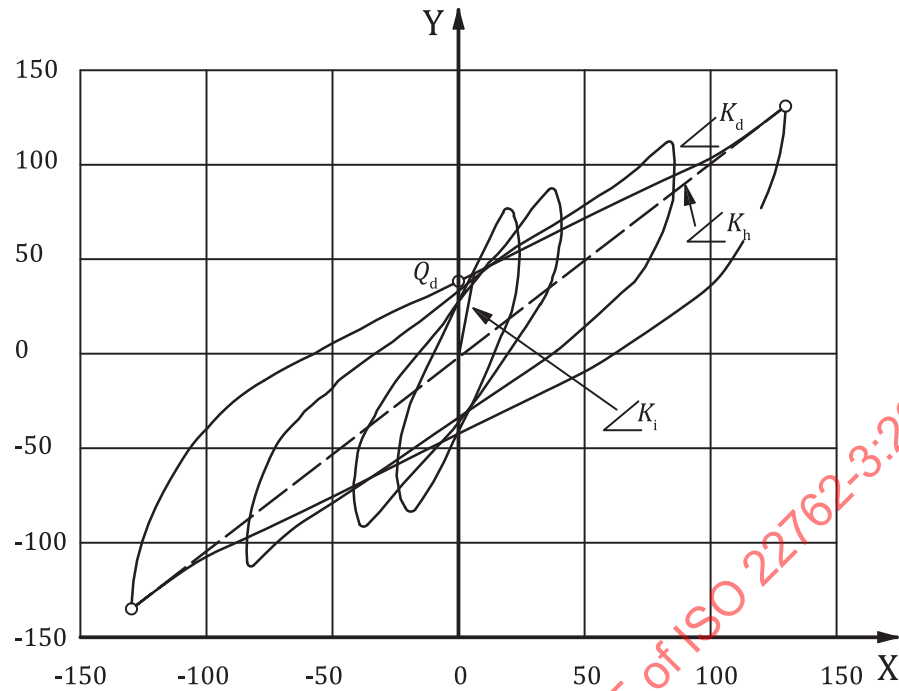
Alternatively, the tangential stiffness, K_t can be taken as a representative shear property of LNR. K_t can be determined as indicated in ISO 22762-1:2018, Annex E.

F.2 Shear properties of high-damping rubber bearings

F.2.1 A typical force-displacement curve for high-damping rubber bearings is shown in [Figure F.1](#). The shear stiffness, K_h , or the equivalent of this shear stiffness, which is defined as the secant slope from peak to peak of the loop, is dependent on the deflection of the elastomeric isolator. The shear stiffness, K_h , can be calculated from [Formula \(F.2\)](#):

$$K_h = G_{eq}(\gamma) \times \frac{A}{T_r} \quad (\text{F.2})$$

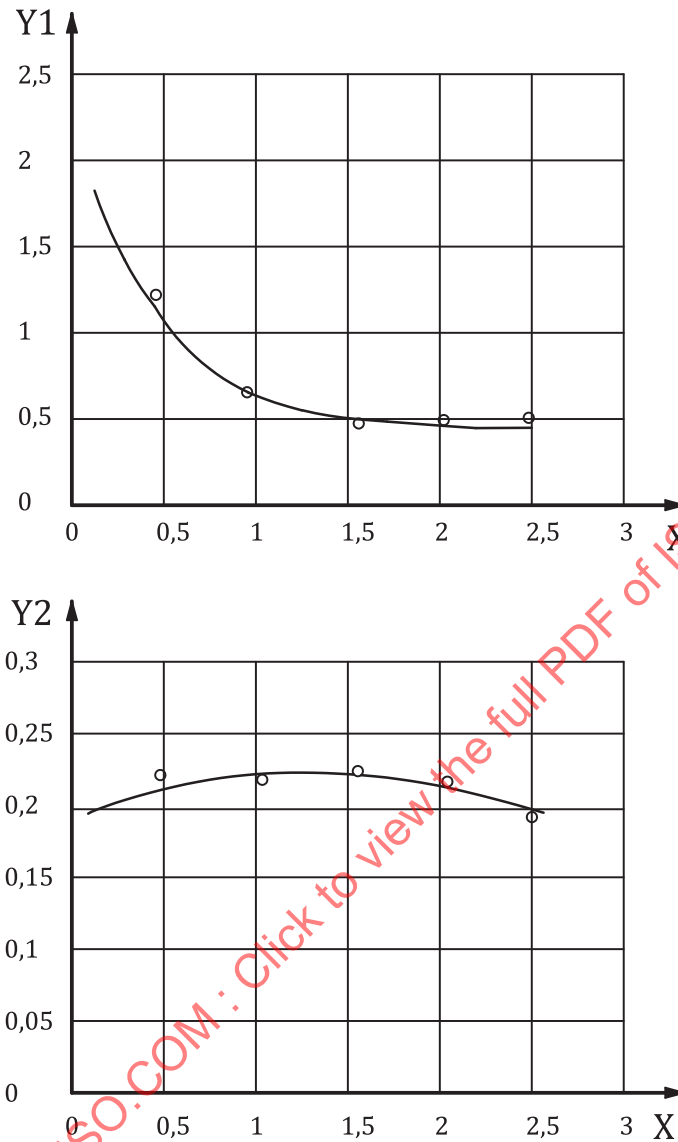
where $G_{eq}(\gamma)$ is the apparent shear modulus, derived from experimental data, expressed as a function of the shear strain γ .

**Key**

- X shear displacement, X , expressed in millimetres
 Y shear force, Q , expressed in kilonewtons

Figure F.1 — Shear force vs. displacement curve for high-damping rubber bearing

F.2.2 Figure F.2 shows an example of the strain dependence of the apparent shear modulus and damping ratio for a high-damping rubber.



Key

- X shear strain, γ
- Y1 shear modulus, $G_{eq}(\gamma)$ (MPa)
- Y2 equivalent damping ratio, $h_{eq}(\gamma)$

Figure F.2 — Examples of strain dependence of $G_{eq}(\gamma)$ and $h_{eq}(\gamma)$ for high-damping rubber bearing

F.2.3 $G_{eq}(\gamma)$ is expressed as a function of the shear strain, γ , such as a polynomial function as shown in Formula (F.3):

$$G_{eq}(\gamma) = a_0 + a_1 \times \gamma + a_2 \times \gamma^2 + a_3 \times \gamma^3 + a_4 \times \gamma^4 + a_5 \times \gamma^5 + L = \sum_{j=0}^n a_j \times \gamma^j \quad (F.3)$$