
**Hydrometry — Measurement of liquid
flow in open channels using current-
meters or floats**

*Hydrométrie — Mesurage du débit des liquides dans les canaux
découverts au moyen de débitmètres ou de flotteurs*

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Foreword

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

International Standards are drafted in accordance with the rules given in the ISO/IEC Directives, Part 2.

The main task of technical committees is to prepare International Standards. Draft International Standards adopted by the technical committees are circulated to the member bodies for voting. Publication as an International Standard requires approval by at least 75 % of the member bodies casting a vote.

Attention is drawn to the possibility that some of the elements of this document may be the subject of patent rights. ISO shall not be held responsible for identifying any or all such patent rights.

ISO 748 was prepared by Technical Committee ISO/TC 113, *Hydrometry*, Subcommittee SC 1, *Velocity area methods*.

This fourth edition cancels and replaces the third edition (ISO 748:1997), which has been technically revised.

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Hydrometry — Measurement of liquid flow in open channels using current-meters or floats

1 Scope

This International Standard specifies methods for determining the velocity and cross-sectional area of water flowing in open channels without ice cover, and for computing the discharge therefrom.

It covers methods of employing current-meters or floats to measure the velocities. It should be noted that although, in some cases, these measurements are intended to determine the stage-discharge relation of a gauging station, this International Standard deals only with single measurements of the discharge; the continuous recording of discharges over a period of time is covered in ISO 1100-1 and ISO 1100-2.

NOTE The methods for determining the velocity and cross-sectional area of water flowing in open channels with ice cover are specified in ISO 9196.

2 Normative references

The following referenced documents are indispensable for the application of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

ISO 772, *Hydrometric determinations — Vocabulary and symbols*

ISO 1088, *Hydrometry — Velocity-area methods using current-meters — Collection and processing of data for determination of uncertainties in flow measurement*

ISO 2537, *Hydrometry — Rotating-element current-meters*

ISO 3455, *Hydrometry — Calibration of current-meters in straight open tanks*

ISO/TS 15768, *Measurement of liquid velocity in open channels — Design, selection and use of electromagnetic current meters*

3 Terms and definitions

For the purposes of this document, the terms and definitions given in ISO 772 apply.

4 Principle of the methods of measurements

4.1 The principle of these methods consists of determining velocity and cross-sectional area. A measuring site is chosen conforming to the specified requirements (see Clause 5); the width, depending on its magnitude, is measured either by means of steel tape or by some other surveying method, and the depth is measured at a number of points (known as verticals) across the width, sufficient to determine the shape and area of the cross-section (see Clause 6).

Velocity observations using current-meters are made at each vertical preferably at the same time as measurement of depth, especially in the case of unstable beds (see 7.1.5).

Velocity observations can also be made using surface floats or velocity-rods (see 7.2).

4.2 The discharge is computed either arithmetically or graphically by summing the products of the velocity and corresponding area for a series of observations in a cross-section. If unit width discharge is required, it is generally computed from the individual observations at each measurement vertical.

5 Selection and demarcation of site

5.1 Selection of site

The site selected should comply as far as possible with the following requirements.

- a) The channel at the measuring site should be straight and of uniform cross-section and slope in order to minimize abnormal velocity distribution. When the length of the channel is restricted, it is recommended for current-meter measurements that the straight length upstream should be at least twice that downstream.
- b) Flow directions for all points on any vertical across the width should be parallel to one another and at right angles to the measurement section.
- c) The bed and margins of the channels should be stable and well defined at all stages of flow in order to facilitate accurate measurement of the cross-section and ensure uniformity of conditions during and between discharge measurements.
- d) The curves of the distribution of velocities should be regular in the vertical and horizontal planes of measurement.
- e) Conditions at the section and in its vicinity should also be such as to preclude changes taking place in the velocity distribution during the period of measurement.
- f) Sites displaying vortices, reverse flow or dead water should be avoided.
- g) The measurement section should be clearly visible across its width and unobstructed by trees, aquatic growth or other obstacles.
- h) Measurement of flow from bridges can be a convenient and sometimes safer way of sampling width, depth and velocity. When gauging from a bridge with divide piers, each section of the channel should be measured separately. Particular care should be taken in determining the velocity distribution when bridge apertures are surcharged or obstructed.
- i) The depth of water at the section should be sufficient at all stages to provide for the effective immersion of the current-meter or float, whichever is to be used.
- j) If the site is to be established as a permanent station, it should be easily accessible at all times with all necessary measurement equipment.
- k) The section should be sited away from pumps, sluices and outfalls, if their operation during a measurement is likely to create unsteady flow conditions.
- l) Sites where there is converging or diverging flow should be avoided.
- m) In those instances where it is necessary to make measurements in the vicinity of a bridge, it is preferable that the measuring site be upstream of the bridge. However, in certain cases and where accumulation of ice, logs or debris is liable to occur, it is acceptable that the measuring site be downstream of the bridge.

- n) The measurement of flow under ice cover is dealt with in ISO 9196. For streams subject to formation of ice cover, the requirements of measurement specified in this International Standard can be used during the free water season.
- o) It may, under certain conditions of river flow or level, prove necessary to carry out current-meter measurements on sections other than the original chosen location. This is quite acceptable if there are no substantial unmeasured losses or gains to the river in the intervening reach and so long as all flow measurements can be related to any stage value recorded at the principal reference section.

5.2 Demarcation of site

5.2.1 If the site is to be established as a permanent station or likely to be used frequently for future measurement, it should be provided with means for demarcation of the cross-section and for determination of stage. Where the site is used only once, or infrequently, and there are no means of determining stage values on site, care should be taken to ensure that the water level and/or flow do not change significantly during the measurement period.

5.2.2 The position of each cross-section, normal to the mean direction of flow, shall be defined on the two banks by clearly visible and readily identifiable markers. Where a site is subject to considerable snow cover, the section line-markers may be referenced to other objects such as rock cairns.

5.2.3 The stage shall be read from a gauge at intervals throughout the period of measurement and the gauge datum shall be related by precise levelling to a standard datum.

5.2.4 An auxiliary gauge on the opposite bank shall be installed where there is likelihood of a difference in the level of water surface between the two banks. This is particularly important in the case of very wide rivers. The mean of the measurements taken from the two gauges shall be used as the mean level of the water surface and as a base for the cross-sectional profile of the stream.

6 Measurement of cross-sectional area

6.1 General

The cross-sectional profile of the open channel at the gauging-site shall be determined at a sufficient number of points to establish the shape of the bed.

The location of each point is determined by measuring its horizontal distance to a fixed reference point on one bank of the channel, in line with the cross-section. This in turn allows calculation of the area of individual segments separated by successive verticals where velocities are measured.

6.2 Measurement of width

6.2.1 Measurement of the width of the channel and the width of the individual segments may be obtained by measuring the horizontal distance from or to a fixed reference point which shall be in the same plane as the cross-section at the measuring site.

6.2.2 Where the width of the channel permits, these horizontal distances shall be measured by direct means, for example a graduated tape or suitable marked wire, care being taken to apply the necessary corrections given in Annex A. The intervals between the verticals, i.e. the widths of the segments, shall be similarly measured.

6.2.3 Where the channel is too wide for the above methods of measurement, and a boat is used, the horizontal distance may be determined by optical or electronic distance-meters, by the use of a differential Global Positioning System, or by one of the surveying methods given in Annex B.

6.3 Measurement of depth

6.3.1 Measurement of depth shall be made at intervals close enough to define the cross-sectional profile accurately. The number of points at which depth shall be measured should be the same as the number of points at which velocity is measured (see 7.1.3).

6.3.2 The depth shall be measured by employing either sounding-rods or sounding-lines or other suitable devices. Where the channel is of sufficient depth, an echo-sounder may be used. If the velocity is high and the channel is sufficiently deep, it is preferable to use an echo-sounder or other device which will not require large corrections. Difficulty may be experienced when attempting to measure depth at times of high velocity. Annex C of this document offers alternative methods.

6.3.3 When a sounding-rod or sounding-line is used, it is desirable that at least two readings be taken at each point and the mean value adopted for calculations, unless the difference between the two values is more than 5 %, in which case two further readings shall be taken. If these are within 5 %, they shall be accepted for the measurement and the two earlier readings discarded. If they are again different by more than 5 %, no further readings shall be taken but the average of all four readings shall be adopted for the measurement, noting that the accuracy of this measurement is reduced.

When an echo-sounder is used, the average of several readings shall always be taken at each point. Regular calibrations of the instrument shall be carried out under the same conditions of salinity and temperature as those of the water to be measured.

Where it is impracticable to take more than one reading of the depth, the uncertainty in measurement may be increased (see Clause 9).

6.3.4 Where measurements of the depths are made separately from the velocity measurements and the water level is not steady, the water level shall be observed at the time of each measurement of the depth. When this is not possible, the water level shall be observed at sufficient intervals for the value of the level at the time of each determination of depth to be obtained by interpolation.

6.3.5 When, during the determination of discharge, the bed profile changes appreciably, depth measurements should be carried out by taking one depth reading at each point at the beginning and one at the end of the velocity measurement at each vertical, and the mean value of these two measurements shall be taken as the effective depth. Care should be exercised when taking repeated soundings to avoid disturbance of the bed.

6.3.6 Inaccuracies in soundings are most likely to occur owing to:

- a) the departure from the vertical of the sounding rod or line, particularly in deep water, when the velocity is high;
- b) the penetration of the bed by the sounding weight or rod;
- c) the nature of the bed when an echo-sounder is used.

Errors due to a) may be minimized by the use, where practicable, of an echo-sounder, or pressure-measuring device. The effect of drag on a sounding line may be reduced by using a streamlined lead weight at the end of a fine wire. A correction shall be applied to the wetted length of wire if the wire is not normal to the water-surface. It is recommended that the angle of departure from the vertical of the sounding line should not be greater than 30° in view of the inaccuracies involved. Two alternative methods of applying the correction are given in Annex C.

Errors due to b) may be reduced by fitting a base plate to the lower end of the sounding-rod, or by fastening a disk to the end of the sounding line, provided they will not cause additional scour of fine bed material due to high velocities.

Errors due to c) may be reduced by selecting an echo-sounder frequency that most adequately depicts the bed-water interface.

6.3.7 In certain cases, for example floods, it may be impossible to determine an adequate profile of cross-section during the measurement. For those cases, the full profile shall be determined by surveying methods, either before or after the measurement. However, it should be recognized that this method is subject to errors due to possible erosion or deposition in the cross-section between the time the profile is determined and the time of discharge measurement.

7 Measurement of velocity

7.1 Measurement of velocity using current-meters

7.1.1 Rotating-element current-meters

Rotating-element current-meters shall be manufactured, calibrated and maintained according to ISO 2537 and ISO 3455. They should be used only within their calibrated range and fitted on suspension equipment similar to that used during calibration.

In the vicinity of the minimum speed of response, the uncertainty in determining the velocity is high. Care should be exercised when measuring velocities near the minimum speed of response.

For high velocities, the propeller, in the case of propeller-type current-meters, or the reduction ratio where available, shall be chosen in order that the maximum speed of rotation can be correctly measured by the revolution counter.

No rotating-element current-meter shall be selected for use where the depth at the point of measurement is less than four times the diameter of the impeller that is to be used, or of the body of the meter itself, whichever is the greater. No part of the meter shall break the surface of the water. An exception to this is the case where the cross-section is very shallow at one side but is the best available.

7.1.2 Electromagnetic current-meters

Electromagnetic current-meters are acceptable for making measurements of point velocity. These current-meters have the advantage that they have no moving parts and thereby eliminate uncertainty due to friction and resistance. They should be calibrated throughout the range of velocity for which they are to be used, and should meet accuracy requirements similar to rotating-element current-meters. They should not be used outside the range of calibration. Electromagnetic current-meters may be capable of operation in shallower depths than rotating element current-meters and of detecting and measuring flow reversal.

No electromagnetic current-meter should be selected for use where the depth at the point of measurement is less than three times the vertical dimension of the probe (see ISO/TS 15768). An exception to this is the case where the cross-section is very shallow at one side but is the best available.

7.1.3 Measurement procedure

Velocity observations are normally made at the same time as measurements of the depth. This method shall be particularly used in the case of unstable beds. Where, however, the two measurements are made at different times, the velocity observations shall be taken at a sufficient number of places, and the horizontal distance between observations shall be measured as described in 6.2.2 and 6.2.3.

In judging the specific number n of verticals in small channels (< 5 m) that are to be defined for the purpose of determining flow at a particular location, the following criteria shall be applied. These criteria shall be the minimum requirement and only practical constraints of time, costs, or on site conditions should result in a reduction of these numbers.

- Channel width $< 0,5$ m $n = 5$ to 6
- Channel width $> 0,5$ m and < 1 m $n = 6$ to 7

- Channel width > 1 m and < 3 m $n = 7$ to 12
- Channel width > 3 m and < 5 m $n = 13$ to 16
- Channel width > 5 m $n \geq 22$

For channel widths > 5 m, the number of verticals shall be chosen so that the discharge in each segment is less than 5 % of the total, insofar as possible, and that in no case should exceed 10 %.

In all instances, measurements of depth made at the water's edge are additional to the above. The first and last verticals should be as close as practically possible to the water's edge.

It is further recommended that the location of the verticals be selected after a previous cross-section survey.

The current-meter shall be held in the desired position in each vertical by means of a wading-rod in the case of shallow channels, or by suspending it from a cable or rod in the case of deeper channels. The current-meter shall be held so that it is not affected by any disturbances of flow.

Current-meter counters or velocity indicators with a digital display of low resolution should not be used at low velocities, e.g. less than 0,15 m/s.

When the orientation of the current-meter can be controlled, e.g. when wading gauging with rods, the meter should be held at right angles to the measuring cross-section. Where oblique flow occurs, or the cross-section is not at right angles to the direction of flow (see 7.1.4) and the meter is suspended, it will align itself with the direction of flow. In such cases, the meter shall be allowed to adjust to the flow before readings are started.

Care should be taken to ensure that the current-meter observations are not affected by random surface-waves and wind.

When a number of points in a vertical are to be measured, a number of current-meters fixed to the same rod or cable can be used to measure corresponding velocities simultaneously whilst ensuring that there is no mutual interference.

If there is any appreciable deflection of the cable on which the meter is suspended, a correction shall be applied for the depth of the measuring-point. No generally applicable correction factor can be given, but it shall be determined by the user for the particular instrument and conditions of measurement (see Annex C).

NOTE The selection and use of appropriate suspension equipment is described in ISO 3454 and ISO 4375.

The velocity at each selected point shall be observed by exposing the current-meter for a minimum of 30 s.

Where the velocity is subject to periodic pulsations in excess of 30 s, the exposure time should be increased accordingly (see ISO 1088).

The current-meter shall be removed from the water or brought to the surface at intervals for visual examination, usually when passing from one vertical to another.

A spin test, where appropriate, should be performed before and after each discharge measurement to ensure that the mechanism of the current-meter operates freely (see ISO 2537).

In channels where the flow is unsteady, it is possible to correct for the variations in the total discharge during the period of the measurement not only by observing the change in stage, but also by continuously measuring the velocity at some conveniently chosen point in the main current.

7.1.4 Oblique flow

If oblique flow is unavoidable, the angle of the direction of the flow to the perpendicular to the cross-section shall be measured and the measured velocity adjusted. Special instruments have been developed for measuring the angle and velocity at a point simultaneously. Where, however, these are not available and

there is insignificant wind, the angle of flow throughout the vertical can be assumed to be the same as that observed on the surface. This angle can be measured with appropriate equipment provided that the operator is located above the measurement vertical. If the channel is very deep or if the local bed profile is changing rapidly, this assumption shall not be accepted without confirmation.

If the measured angle between the flow direction and the perpendicular to the cross-section is θ the velocity used for the computation of flow discharge shall be:

$$v_{\text{corrected}} = v_{\text{measured}} \cos \theta \quad (1)$$

NOTE Some current-meters are equipped to measure the normal component of velocity directly when held perpendicular to the measurement cross-section in oblique flow. This correction would not be applied in such cases.

7.1.5 Determination of the mean velocity in a vertical

7.1.5.1 Choice and classification

The choice of the method for determining velocity depends on certain factors. These are: time available, width and depth of the channel, bed conditions in the measuring section and the upstream reach, rate of variation of level, degree of accuracy desired and equipment used.

These methods are classified as follows:

- a) velocity distribution method (see 7.1.5.2);
- b) reduced point methods (see 7.1.5.3);
- c) integration method (see 7.1.5.4).

7.1.5.2 Velocity distribution method

Using this method, the values of the velocity are obtained from observations at a number of points in each vertical between the surface of the water and the bed of the channel. The number and spacing of the points should be so chosen as to define accurately the velocity distribution in each vertical with a difference in readings between two adjacent points of not more than 20 % with respect to the higher value. The location of the top and the bottom readings should be chosen, taking into account the specification under 7.1.1 and 7.1.2 (see also ISO 1088).

The velocity observations at each position are then plotted graphically and the unit width discharge or mean velocity determined by planimeter, digitizer or equivalent method. The mean velocity in the vertical may also be obtained by dividing the unit width discharge by the total depth.

NOTE 1 This method may not be suitable for routine discharge measurements because the apparent gain in precision may be offset by errors resulting from change of stage during the long period of time needed for making the measurement.

NOTE 2 Although this clause deals primarily with the determination of mean velocity in the vertical, it may be necessary to apply the same principle to the determination of mean velocity close to the vertical side or wall of a channel. The velocity curve can be extrapolated from the last measuring point to the bed or vertical side of the channel by calculating v_x from Equation (2):

$$v_x = v_a \left(\frac{x}{a} \right)^{1/m} \quad (2)$$

where

v_x is the open point velocity in the extrapolated zone at a distance x from the bed or vertical side;

v_a is the velocity at the last measuring point at a distance a from the bed or vertical side;

m is an exponent.

The mean velocity, $\bar{v}$, between the bottom (or a vertical side) of the channel and the nearest point of measurement (where the measured velocity is v_a) can be calculated directly from Equation (3):

$$\bar{v} = \left(\frac{m}{m+1} \right) v_a \quad (3)$$

Generally, m lies between 5 and 7 but it may vary over a wider range depending on the hydraulic resistance. The value $m = 4$ applies to coarse beds or vertical sides while $m = 10$ is characteristic of smooth beds or vertical sides.

m is obtained as follows:

$$m = \frac{C_{\text{ver}}}{\sqrt{g}} \left(\frac{2\sqrt{g}}{\sqrt{g} + C_{\text{ver}}} + 0,3 \right) \quad (4)$$

where

g is the acceleration due to gravity (m/s^2);

C_{ver} is Chezy's coefficient on a vertical ($\text{m}^{0.5}/\text{s}$).

NOTE 3 An alternative method of obtaining the velocity in the region below the last measuring-point is based on the assumption that the velocity for some distance up from the bed of the channel is proportional to the logarithm of the distance X from that boundary. If the observed velocities at points approaching the bed are plotted against $\log X$, then the best-fitting straight line through these points can be extended to the boundary. The velocities close to the boundary can then be read from the graph.

7.1.5.3 Reduced point methods

7.1.5.3.1 General

These methods, less strict than methods exploring the entire field of velocity, are used frequently because they require less time than the velocity-distribution method (7.1.5.2). They are based, however, on theoretical velocity profiles.

It is recommended that for a new gauging section the accuracy of the selected method be assessed by comparing the results of preliminary gaugings with those obtained from the velocity distribution method.

7.1.5.3.2 One-point method

Velocity observations shall be made on each vertical by exposing the current-meter at 0,6 of the depth below the surface. The value observed shall be taken as the mean velocity in the vertical.

7.1.5.3.3 Two-point method

Velocity observations shall be made on each vertical by exposing the current-meter at 0,2 and 0,8 of the depth below the surface. The average of the two values shall be taken as the mean velocity in the vertical.

7.1.5.3.4 Three-point method

Velocity observations shall be made on each vertical by exposing the current-meter at 0,2, 0,6 and 0,8 of the depth below the surface. The 0,6 measurement may be weighted and the mean velocity $\bar{v}$ obtained from Equation (5):

$$\bar{v} = 0,25(v_{0,2} + 2v_{0,6} + v_{0,8}) \quad (5)$$

7.1.5.3.5 Five-point method

Velocity measurements are made by exposing the current-meter on each vertical at 0,2, 0,6 and 0,8 of the depth below the surface and as near as possible to the surface and the bed. The mean velocity $\bar{v}$ may be determined from a graphical plot of the velocity profile with a planimeter, or from Equation (6).

$$\bar{v} = 0,1(v_{\text{surface}} + 3v_{0,2} + 3v_{0,6} + 2v_{0,8} + v_{\text{bed}}) \quad (6)$$

7.1.5.3.6 Six-point method

Velocity observations are made by exposing the current-meter on each vertical at 0,2, 0,4, 0,6 and 0,8 of the depth below the surface and as near as possible to the surface and the bed (see 7.1.5.3.7.2). The velocity observations at each point are plotted in graphical form and the mean velocity or unit width discharge determined with the aid of a planimeter. Alternatively, the mean velocity $\bar{v}$ may be found algebraically from Equation (7).

$$\bar{v} = 0,1(v_{\text{surface}} + 2v_{0,2} + 2v_{0,4} + 2v_{0,6} + 2v_{0,8} + v_{\text{bed}}) \quad (7)$$

7.1.5.3.7 Surface one-point method

7.1.5.3.7.1 In flashy or other conditions where the above methods are not feasible, velocity shall be measured at one point just below the surface. The depth of submergence of the current-meter shall be uniform over all the verticals; care shall be taken to ensure that the current-meter observations are not affected by random surface-waves and wind. This 'surface' velocity may be converted to the mean velocity in the vertical by multiplying it by a predetermined coefficient specific to the section and to the discharge.

The coefficient shall be computed for all stages by correlating the velocity at the surface with the velocity at 0,6 of the depth or, where greater accuracy is desired, with the mean velocity obtained by one of the other methods previously described.

It may be noted for guidance that in general, the coefficient varies between 0,84 and 0,90 depending upon the shape of the velocity profile; the higher values between 0,88 and 0,90 are usually obtained when the bed is smooth.

7.1.5.3.7.2 The use of current-meters near to the surface, or to the bed of the channel, shall be in accordance with the manufacturer's instructions (see also 7.1.1 and 7.1.2).

7.1.5.3.8 Alternate sampling methods

Alternative sampling methods for determining the mean velocity in the vertical may be utilized under exceptional circumstances, e.g. high velocity, rapidly changing stage or floating debris provided the method applied can be demonstrated by experiment to give results of similar accuracy to those listed above.

7.1.5.4 Integration method

In this method, the current-meter is lowered and raised through the entire depth on each vertical at a uniform rate. The speed at which the meter is lowered or raised should not be more than 5 % of the mean water velocity and should not in any event exceed 0,04 m/s. Two complete cycles should be made on each vertical and if the results differ by more than 10 %, the operation (two complete cycles) should be repeated until results within this limit are obtained.

The integration method gives good results if the time of measurement allowed is sufficiently long (60 s to 100 s). The technique can be, but is not normally, used in depths of less than 1 m.

With a propeller-type current-meter, the average velocity can then be read from the instrument calibration as equivalent to the average number of revolutions (being derived as the total number of revolutions divided by the total time taken for the measurement in that vertical). Uncertainties introduced by using meters with more than one calibration equation should be avoided.

By using a current-meter that measures velocity directly, such as the electromagnetic current-meter, the mean velocity in the vertical can be obtained by direct reading of the instrument.

When a sounding rod or weight is used, it will not be possible to measure the velocity throughout the entire vertical; a zone may, for example, remain unmeasured near the channel bed. An estimate of the unit width discharge of this zone can be obtained from:

$$q_u = \frac{2v_m h_f}{3} \quad (8)$$

where

q_u is the unit width discharge below the measured zone;

v_m is the mean velocity for the measured part of the vertical;

h_f is the depth of the unmeasured zone.

Similarly, the unit width discharge for any unmeasured zone near the surface is obtained from:

$$q_s = \frac{v_m h_s}{0,9} \quad (9)$$

where

q_s is the unit width discharge above the measured zone;

v_m is the mean velocity for the measured part of the vertical;

h_s is the depth of the unmeasured zone.

As far as possible, the type of measuring equipment should be selected to minimize the depth of the unmeasured zones.

7.1.6 Errors and limitations

Estimates of the possible errors that may occur when using the various methods detailed in 7.1.5 are given in 9.3.3. It should be noted that these estimates are of possible random errors which may occur even when all the precautions noted earlier and below are observed. If the measurement is not made under these best conditions, additional uncertainty should be included when estimating the overall uncertainty of the measurement.

Errors may arise:

- a) if the flow is unsteady;
- b) if material in suspension interferes with the performance of the current-meter;
- c) if skew flow occurs, and the appropriate correction factors are not known accurately;
- d) if the current-meter is used for measurement of velocity outside the range established by the calibration;
- e) if the set-up for measurement (such as rods or cables suspending the current-meter, the boat, etc.) is different from that used during the calibration of the current-meter, in which case a systematic error may be introduced;
- f) if there is significant disturbance of the water surface by wind;

- g) if the current-meter is not held steadily in the correct place during the measurement, which is the case when gauging from a boat which is drifting (see Annex D), or when an oscillating transverse movement occurs. In the latter case, the resultant of the flow velocity and the transverse velocities gives rise to serious positive errors.

7.2 Measurement of velocity using floats

7.2.1 General

This method shall only be used when it is impossible to employ a current-meter because of access difficulties, excessive velocities and depths, the presence of material in suspension, where velocities are too low for current-meter measurement or in cases of reconnaissance.

7.2.2 Selection of site

Three cross-sections shall be selected along the reach of the channel as described in Clause 5, at the beginning, midway and at the end of the reach. The cross-sections shall be far enough apart for the time which the floats take to pass from one cross-section to the next to be measured accurately. The midway cross-section shall be used only for the purpose of checking the velocity measurement between the cross-sections at the beginning and at the end of the reach. A minimum duration of float movement of 20 s is recommended.

7.2.3 Measuring procedure

The float shall be released far enough above the upper cross-section to attain a constant velocity before reaching the first cross-section. The time at which the float passes each of the three cross-sections is then noted. This procedure shall be repeated with the floats at various distances from the bank of the river. The distances of the float from the bank as it passes each cross-section may be determined by suitable optical means, for example, a theodolite.

It is also possible to use the double stopwatch method described in Annex F. This allows the determination of the velocity of the float and the position of its path in the section in a single operation and without the need for special or surveying equipment.

Increasing the number of floats used to determine the velocity in each segment will improve the accuracy of the measurement.

The width of the channel shall be divided into a certain number of segments of equal width. If, however, the channel is very irregular, each segment shall have approximately the same discharge. The number of segments shall not be less than three, but where possible a minimum of five shall be used, the actual number of segments depending on the time available for these observations at the particular stage of the river.

7.2.4 Types of float

7.2.4.1 General

The velocity of the water in each segment can be determined by

- a) surface floats,
- b) double floats,
- c) other types of floats.

NOTE Separately flowing blocks of ice, provided they are small, can be used as surface floats during ice drifting.

The coefficients for obtaining the mean velocity from the measurements for the various types of floats are given in 7.2.5.

7.2.4.2 Surface floats

These may be used during floods when velocity measurements are to be made quickly. They shall not be used when their movement is likely to be affected by winds.

7.2.4.3 Double floats

These may be used for measurements of velocities in deep rivers. The sub-surface body may be positioned at 0,6 of the depth below the surface, or at other depths to obtain direct velocity measurements at these depths.

7.2.4.4 Other types of floats

Other methods of obtaining the mean velocity in each segment may be used if the bed profile is regular over the measuring reach:

a) Sub-surface floats

These may be used for measurement of velocities in very deep rivers. The length of the sub-surface float, sometimes called the multiple float, which consists of separate elements suitably attached together to permit flexibility and supported by a surface float, shall be approximately equal to the water depth, but the float shall in no case touch the bottom.

b) Velocity-rods

These may be used for measurement of velocities in the case of artificial or other regular channels where the cross-section is uniform, the bed is free from weeds, and the depth of the water is constant. The velocity-rod (sometimes called a float-rod) shall be at least 0,95 of the depth of the channel but shall not touch the bottom.

7.2.5 Determination of velocity

7.2.5.1 Method

The float velocity shall be determined by dividing the distance between the cross-sections by the time taken by the float to travel this distance. Several measurements of the float velocities shall be taken and the mean of these measurements shall be multiplied by the appropriate coefficient to obtain the mean velocity in the segment. The coefficient derived from current-meter measurements at the site at a stage as near as possible to that during the float measurement may be used for converting the float velocity to mean velocity.

7.2.5.2 Surface floats

Where it is not possible to check the coefficient directly, it may be assumed for guidance that, in general, the coefficient of the surface float varies between 0,84 and 0,90 depending upon the shape of the velocity profile. The higher values are usually obtained when the bed is smooth, but values outside this range may occur under certain circumstances.

7.2.5.3 Double floats

Where it is not possible to check the coefficient directly, it may be accepted for guidance that when the sub-surface body is situated at 0,6 of the depth, the coefficient is approximately equal to 1,0 and at 0,5 of the depth, the coefficient is approximately equal to 0,96.

7.2.5.4 Other types of floats

Where a direct check on the coefficient is not possible, it may be assumed that the coefficient of the sub-surface floats and velocity-rods varies in general over the range 0,8 to 1,0.

7.2.6 Main sources of error

Errors may occur during the measurement of discharge by floats and the main sources are listed below. They shall be taken into consideration when estimating the overall error as given in Clause 9.

Errors may arise:

- a) if the coefficient from which the mean velocity is obtained from the float velocity is not known accurately;
- b) if too few segments are used for the velocity distribution;
- c) if a sub-surface float or velocity-rod is used and the depth of the channel is not uniform throughout the measuring reach;
- d) if the float does not travel in the centre of the panel due to oblique currents;
- e) if there is wind, but it should be noted that this error is generally negligible in comparison with others listed above, unless a surface float is used.

8 Computation of discharge

8.1 General

The method of determination of the mean velocity or unit width discharge in each vertical has been dealt with in 7.1 and 7.2. In these subclauses, the method of determination of discharge from current-meter measurements and float measurements is presented. These methods have been classed as the graphical method (8.2) and the arithmetic method (8.3), the latter being particularly useful for computations carried out in the field. The methods given in 8.4 to 8.7 are applicable for special circumstances.

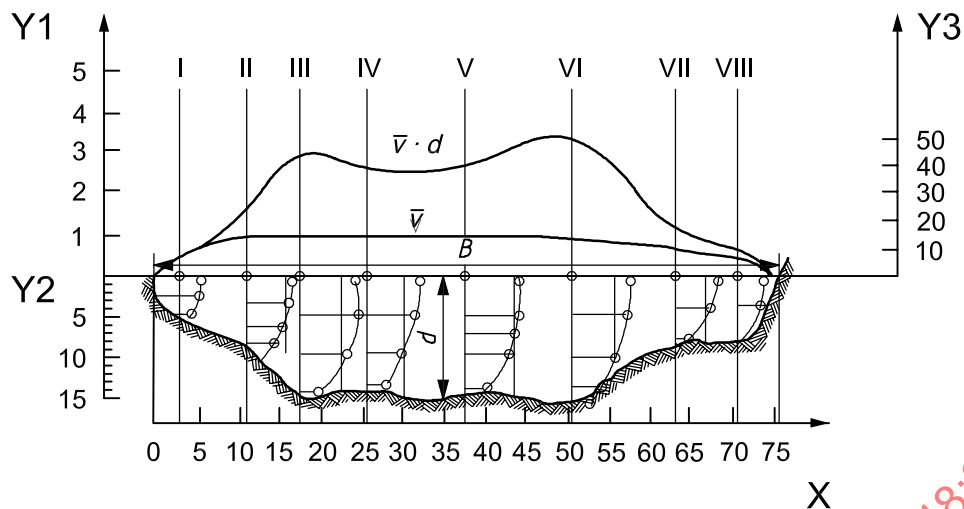
8.2 Graphical method

8.2.1 Depth-velocity-integration

The velocity readings recorded for each vertical are plotted against depth as shown in Figure 1. The area contained by the velocity curve produced for each vertical gives the discharge for unit width of the corresponding section. Where necessary, velocity curves can be extrapolated to the surface and bed using the methods described in notes at the end of 7.1.5.2. The values of unit-width discharges $\bar{v} \cdot d$ are then plotted on the upper part of the diagram and joined to form a continuous curve. The area enclosed between this curve and the line representing the water surface gives the total discharge through the section.

In the case of velocity measurements by the integration or reduced point methods, the unit-width discharge at each vertical is obtained directly as the product of the mean velocity $\bar{v}$ and the corresponding depth d .

When velocity measurements are not carried out on the same verticals on which the depth measurements are made, the $\bar{v}$ curve shall be plotted across the width of the stream and the value of $\bar{v}$ corresponding to the verticals where depth measurements are made shall be taken for plotting the $\bar{v} \cdot d$ curve.

**Key**

- X distance (m)
 Y1 mean velocity (m/s)
 Y2 depth (m)
 Y3 unit width discharge (m²/s)

Figure 1 — Computation of discharge from current-meter measurements — Depth-velocity integration method

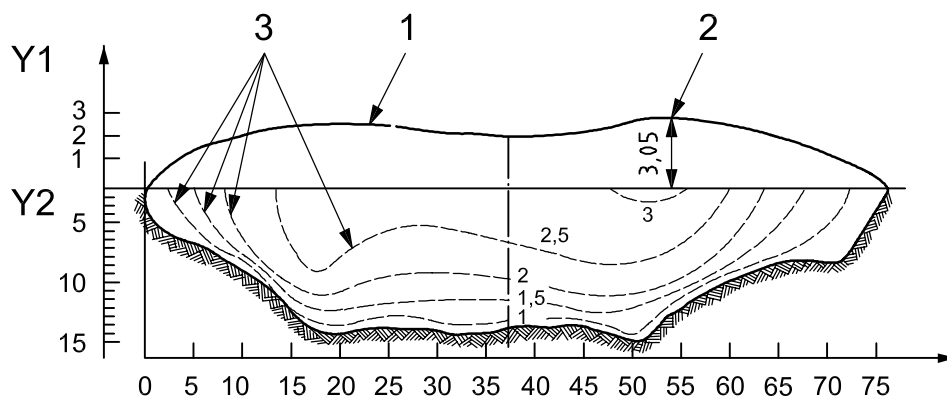
$$Q = \sum v_i d_i \Delta B \quad (10)$$

where

- Q is the total discharge;
 v is the average velocity in segment;
 d_i is the depth of segment;
 ΔB is the incremental width.

8.2.2 Velocity-area integration method (velocity-contour method)

Based on the velocity-distribution curves of the verticals, a velocity-distribution diagram for the cross-section [see Figure 2 a)] shall be prepared showing lines of equal velocity. Starting from the maximum, the areas enclosed by the successive equal-velocity curves and the water surface shall be measured by a planimeter and shall be plotted in another diagram [as shown in Figure 2 b)] with the ordinate indicating the velocity and the abscissa indicating the corresponding area enclosed by the respective velocity curve. The area enclosed by the velocity-area curve represents the discharge of the cross-section.

**Key**

X distance (m)

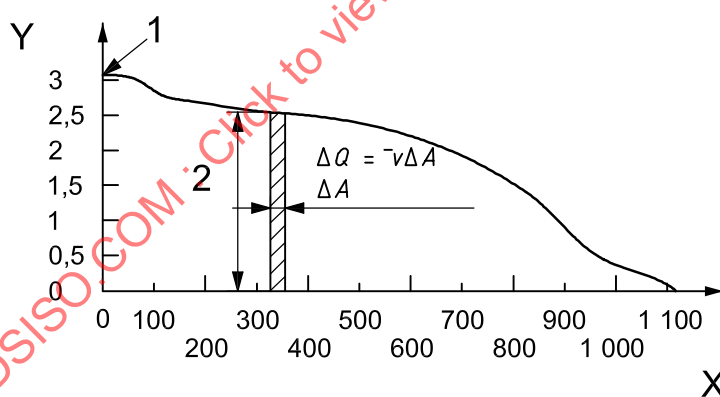
Y1 surface velocity (m/s)

Y2 depth (m)

1 surface velocity distribution curve

2 maximum velocity

3 lines of equal velocity (m/s)

a) Velocity contours in a section**Key**X area (m²)

Y velocity (m/s)

1 maximum velocity

2 mean velocity, $\bar{v}$, (m/s)

$$Q = \sum \bar{v}_i \Delta A_i$$

b) Total flow**Figure 2 — Computation of discharge from current-meter measurements — Velocity-area integration method**

8.3 Arithmetic methods

8.3.1 Mean-section method

The cross-section is regarded as being made up of a number of segments, each bounded by two adjacent verticals (see Figure 3).

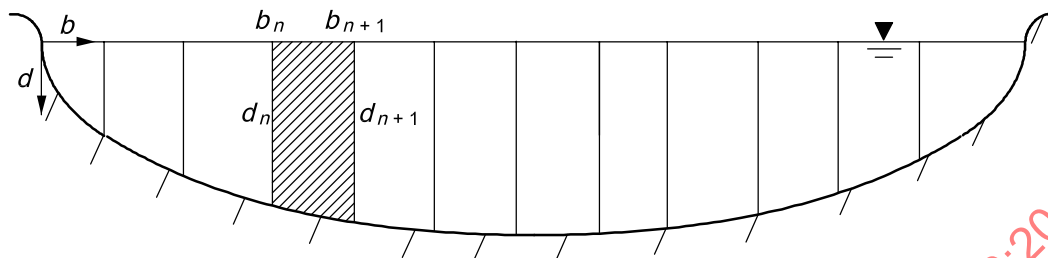


Figure 3 — Diagram illustrating the mean section method

The flow in the shaded panel is calculated as follows:

$$q = (b_{n+1} - b_n) \left(\frac{d_{n+1} + d_n}{2} \right) \left(\frac{\bar{v}_{n+1} + \bar{v}_n}{2} \right) \quad (11)$$

where $\bar{v}$ is the average velocity in each vertical.

NOTE The additional discharge in the segments between the bank and the first vertical, and between the last vertical and the other bank, can be estimated from the above equation, on the assumption that the velocity at the banks is zero. If, however, this discharge is a significant proportion of the total flow, then the equation given in Note 2 of 7.1.5.2 can be used to obtain the mean velocity in the region of the bank.

The total flow is equal to the sum of the discharge in each panel, thus:

$$Q = \sum (b_{n+1} - b_n) \left(\frac{d_{n+1} + d_n}{2} \right) \left(\frac{\bar{v}_{n+1} + \bar{v}_n}{2} \right) \quad (12)$$

8.3.2 Mid-section method

The cross-section is regarded as being made up of a number of segments, each containing a vertical (see Figure 4).

The discharge in each segment shall be computed by multiplying $\bar{v} \cdot d$ by the corresponding width measured along the water-surface line. This width shall be taken to be the sum of half the width from the adjacent vertical to the vertical for which $\bar{v} \cdot d$ has been calculated plus half the width from this vertical to the corresponding adjacent vertical on the other side. The value for $\bar{v} \cdot d$ in the two half-widths next to the banks may be taken as zero.

For this reason, the first and last verticals of a measurement should be as close to the banks as possible if the mid-section method of calculation is used.

Where the bed is uneven, and time and cost allows, determining the depth at points midway between the annotated verticals shown in Figure 4 may provide a more accurate determination of the area of each panel.

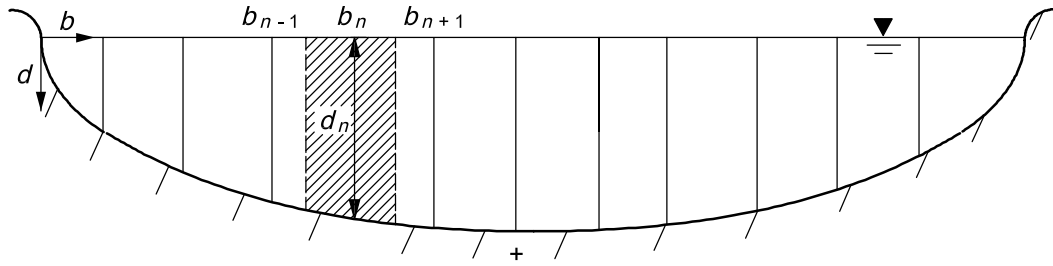


Figure 4 — Diagram illustrating the mid-section method

For this method, the flow in each panel is calculated as shown below:

$$q = \bar{v}_n d_n \left(\frac{b_{n+1} - b_{n-1}}{2} \right) \quad (13)$$

where again $\bar{v}$ is the average velocity in the vertical.

The computation is carried out at each vertical and the total discharge through the section is obtained by summing these partial discharges as follows:

$$Q = \sum \bar{v}_n d_n \left(\frac{b_{n+1} - b_{n-1}}{2} \right) \quad (14)$$

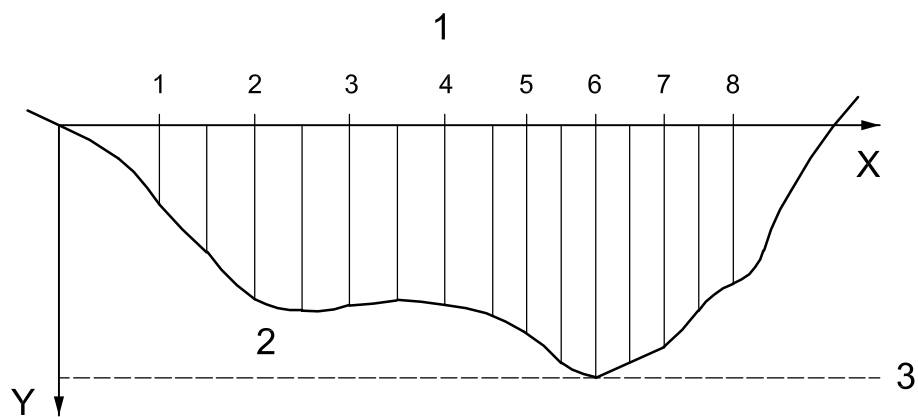
8.4 Independent vertical method

This method is useful for measuring streams with rapidly changing discharge. Several verticals are chosen and their distances measured from a fixed reference point [Figure 5 a)]. On each gauging, measurements of velocity and depth at all the chosen verticals are made, using one of the methods described above. The water level is measured at the beginning and end of the series of measurements on each vertical. For each segment, a separate stage discharge relation is prepared. Subsequently, the discharge of the river at a given stage can be determined by combining the discharges for each segment.

By employing this gauging technique over a period of time and if a sufficiently large range in flow has been covered, it will be possible to derive a relationship between stage and unit-width discharge for each vertical. A family of curves can then be constructed, each curve representing an independent stage/discharge relationship for the corresponding segment of channel width [Figure 5 b)]. This assumes that the channel geometry remains constant and that no change occurs in the position of a vertical relative to the reference point.

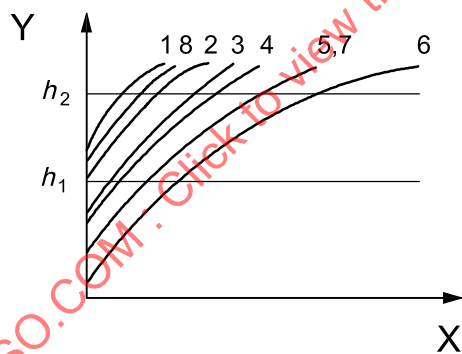
Then, for a given value of stage, total flow in the cross-section is obtained by using a mathematical method by summation of all segment discharges [Figure 5 c)]; or with a graphical method [Figure 5 d)] by plotting the unit-width discharge for all verticals and determining the area under this curve.

Total flow in the cross-section for any given value of stage can be obtained by either of these methods.



- Key**
- X channel width (m)
 - Y stage (m)
 - 1 verticals
 - 2 channel bed
 - 3 stage datum

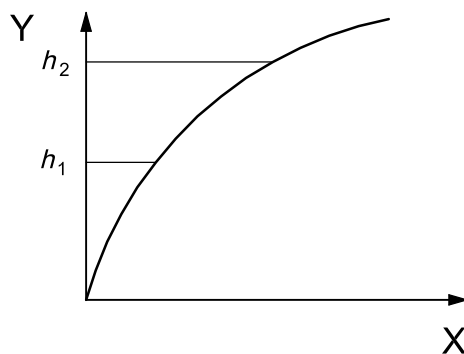
a) Verticals in cross-section



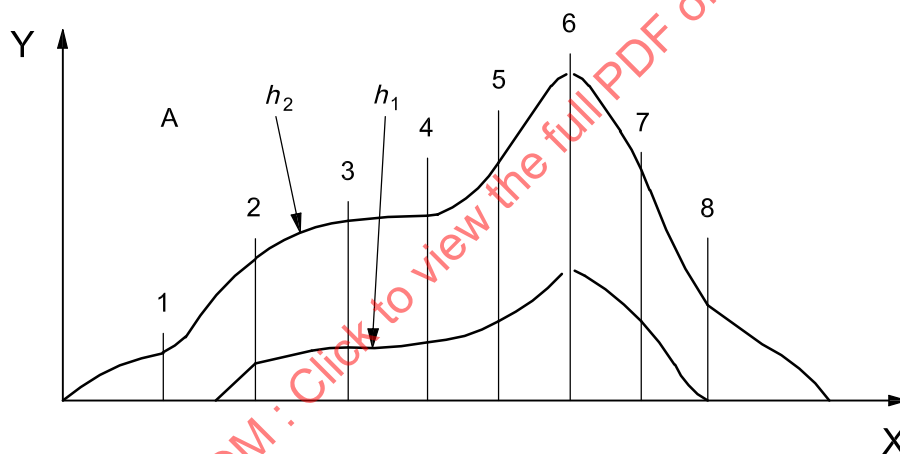
- Key**
- X discharge per unit (m^3/s)
 - Y stage (m)

b) Stage/discharge curves for individual verticals

Figure 5 — Computation of discharge from current-meter measurement — Independent vertical method *(continued)*

**Key**X total discharge (m^3/s)

Y stage (m)

c) Total discharge (mathematical method)**Key**

X distance (m)

Y discharge per unit width (m^3/s)A distribution of q for h_1 or h_2 **d) Graphical method**

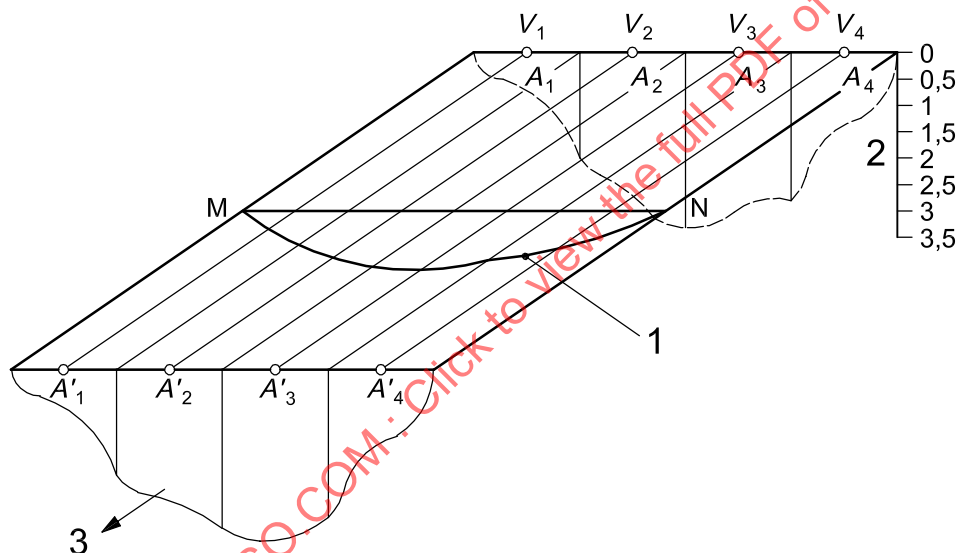
Figure 5 — Computation of discharge from current-meter measurement — Independent vertical method

8.5 Mean-section method — Horizontal planes

Instead of determining the mean velocity in each vertical, the mean velocities for a number of horizontal planes can be determined by a corresponding procedure to that given in 7.1.5.2. A similar method to that given in 8.3.1 can then be used to determine the discharge. The use of horizontal and vertical-plane computation is particularly suited to measurements in regular-shaped channels, as it enables a check to be made on the accuracy of the computation.

8.6 Determination of discharge from surface-float velocity measurements

If the upstream and downstream cross-sections are plotted as shown in Figure 6 a) and then divided into a suitable number of segments of equal width, the cross-sectional area of each of these segments can be determined. Halfway between the two cross-section lines, another line MN shall be drawn parallel to the cross-sectional lines. The starting and ending points of each float may then be plotted and joined by firm lines, while the surface-points separating the various panels of the two cross-sections may be joined by dotted lines. Where the firm lines cross the line MN, the corresponding mean velocity (float velocity multiplied by the appropriate coefficient - see Note 1 below) shall be plotted normal to MN and the end points of these velocity vectors joined to form a velocity-distribution curve [Figure 6 b)].

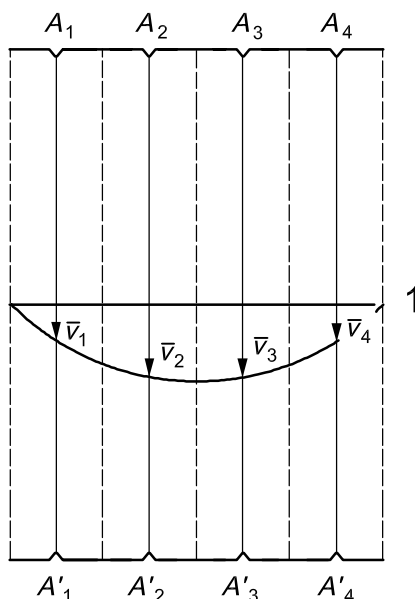


Key

- 1 surface velocity distribution
- 2 depth (m)
- 3 direction of flow

a) Measurement sections and float paths

Figure 6 — Computation of discharge from float measurements (continued)

**Key**

1 velocity (m/s)

b) Mean velocity-distribution curve from float measurements**Figure 6 — Computation of discharge from float measurements**

The mean area of corresponding segments of the upper and lower cross-sections, when multiplied by the mean velocity for this panel as shown by the velocity-distribution curve, represents the discharge through that segment. The summation of the discharges for all the segments is equal to the total discharge. The mean velocity in a panel may be determined by measuring, by means of a planimeter, the area under the velocity-distribution curve for the corresponding segment or, alternatively, an approximate value may be adopted equal to the reading of the velocity halfway across the panel.

$$Q = \sum_{i=1}^m \bar{v}_i \frac{A_i + A'_i}{2} \quad (15)$$

where

$\bar{v}_i$ is the mean velocity in the segment;

A_i is the area of upstream segment;

A'_i is the area of downstream segment.

NOTE 1 When it is impossible to obtain satisfactory movement of the floats across the whole width of the river, for instance if the floats move towards the centreline of the flow, an unadjusted discharge can be determined by measuring the mean of the surface velocities. This discharge has then to be multiplied by a coefficient determined from the results of current-meter measurements carried out simultaneously with float measurements at the level which approximates to that of the float measurements.

NOTE 2 Annex F presents a method for determining the discharge from a float measurement using two stop watches (see 7.2.3).

8.7 Determination of discharge for variations of water level

8.7.1 General

If the fluctuation of water level during the period of velocity measurement is less than 5 % of the mean depth or 0,05 m, whichever is the lesser dimension, the mean value shall be adopted for the computation of the discharge. If the fluctuation is more than this amount, then the discharge shall be computed as shown in 8.7.2 and the mean water level corresponding to this discharge computed as shown in 8.7.3.

8.7.2 Computation of discharge

The water level is plotted separately for each segment to form a series of steps as shown in Figure 7. Alternatively, the levels can be joined by a smooth curve. A curve of mean velocity multiplied by depth is then plotted above the water-surface line, the area enclosed representing the total discharge.

8.7.3 Computation of mean water level

The mean water level representative of the discharge measurement shall be computed from the equations:

$$\bar{z} = \frac{\sum q_i z_i}{Q} \quad (16)$$

$$q_i = b_i d_i \bar{v}_i \quad (17)$$

where

$\bar{z}$ is the weighted mean water level above the gauge datum;

q_i is the partial discharge in the i th segment;

z_i is the mean water level corresponding to the partial discharge q_i ;

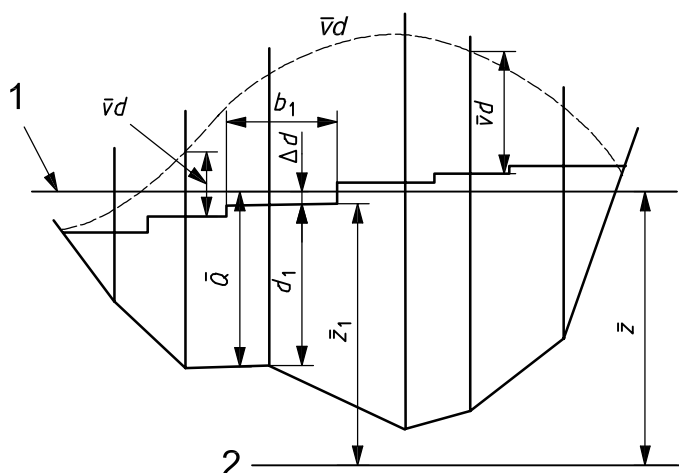
Q is the total discharge and equal to the sum of the partial discharges $\sum q_i$;

b_i is the width of the i th segment;

d_i is the depth of the i th segment;

$\bar{v}_i$ is the mean velocity in the i th segment.

The required measurements are illustrated in Figure 7.



Key

- 1 weighted mean water level above the gauge datum
- 2 gauge datum

Figure 7 — Computation of discharge and mean water level for variations of water level

9 Uncertainties in flow measurement

9.1 General

The uncertainty in a single measurement of discharge is dealt with in ISO 5168, to which reference should be made. Additional information is given in the GUM:1995¹⁾, especially Clauses 2 and 3. In these clauses, a general outline of the method of estimating this uncertainty under conditions of steady flow is given. In Annex E, the individual components of the uncertainty are examined and examples of these are given. It should not be assumed, however, that these are generally applicable and it should be stressed that the observations on which they are based did not include all kinds and sizes of rivers (see ISO 1088).

9.2 Definition of uncertainty

All measurements of a physical quantity are subject to uncertainties. These may be due to systematic errors (biases) in the equipment used for calibration and measurement, or to random scatter caused by, for example, a lack of sensitivity of the equipment used for the measurement. The result of a measurement thus is only an estimate of the true value of the measured quantity and therefore is complete only when accompanied by a statement of its uncertainty.

The discrepancy between the true and measured values is the measurement error. The measurement error, which cannot be known, causes an uncertainty about the correctness of the measurement result. The uncertainty is expressed quantitatively as a “parameter ... that characterizes the dispersion of the values that could reasonably be attributed to the measurand” (GUM:1995, 2.2.3). The GUM further states that the parameter may be, for example, a standard deviation or the half-length of an interval having a stated level of confidence, and that all sources of uncertainty, including those arising from systematic effects, contribute to the dispersion.

1) To be republished as ISO/IEC Guide 98-3.

The measurement error is a combination of component errors that arise during the performance of various elementary operations during the measurement process. For measurements of composite quantities that depend on several component quantities, the total error of the measurement is a combination of the errors in all component quantities. Determination of measurement uncertainty involves identification and characterization of all components of error, quantification of the corresponding uncertainties, and combination of the component uncertainties. The uncertainties are combined using the statistical rules for combining standard deviations, giving proper consideration to correlations among all of the various sources of measurement error in order to account for both systematic and random errors. The resulting uncertainty values are termed standard uncertainties; they correspond to one standard deviation of the probability distribution of measurement errors.

In some applications it is necessary to express the uncertainty of a measurement as a band or interval that may be expected to contain a specified fraction of the distribution of values that could reasonably be attributed to the measurand. Such an interval is obtained by multiplying the standard uncertainty by a factor, k , usually in the range 2 to 3, called the coverage factor. The fraction of the distribution contained by the interval is called the level of confidence. The relation between the level of confidence and the coverage factor depends on the probability distribution of measurement errors.

In this clause, uncertainties are given as standard uncertainties (one standard deviation) and are expressed as percentages of the measured values (relative or percentage uncertainties). (Note that the use of standard uncertainties is a change from previous editions of this International Standard, which used expanded uncertainties with a coverage factor of 2.) If expanded uncertainties are required, the standard normal (Gaussian) distribution is used to determine the coverage factor corresponding to a specified degree of confidence. In particular, expanded uncertainties with a coverage factor of 2 have an approximate level of confidence of 95 %. The expanded uncertainty with a coverage factor of 1 has an approximate level of confidence of 68 %.

9.3 Method of calculating the uncertainty in discharge by measurement of velocity by current-meter

9.3.1 General

The measurement method, briefly, consists of dividing the channel cross-section under consideration into segments by m verticals and measuring the width, depth and mean velocity (denoted by b_i , d_i and v_i , respectively) associated with each vertical i . The mean velocity v_i at each vertical is computed from point velocity measurements made at each of several depths on the vertical. The flow is computed as follows:

$$Q = F \sum b_i d_i v_i \quad (18)$$

where

Q is the flow (in cubic metres per second);

F is a factor, assumed to be unity, that relates the discrete sum over the finite number of verticals to the integral of the continuous function over the cross-section.

9.3.2 Contributory uncertainties

The relative (percentage) combined standard uncertainty in the measurement is given by Equation (19):

$$u(Q)^2 = u_m^2 + u_s^2 + \frac{\sum_{i=1}^m (b_i d_i \bar{v}_i)^2 (u_{b,i}^2 + u_{d,i}^2 + u_{v,i}^2)}{\left(\sum_{i=1}^m (b_i d_i \bar{v}_i) \right)^2} \quad (19)$$

where

- $u(Q)$ is the relative (percentage) combined standard uncertainty in discharge;
- $u_{b,i}, u_{d,i}, u_{\bar{v},i}$ are the relative (percentage) standard uncertainties in the width, depth and mean velocity measured at vertical i ;
- u_s is the uncertainty due to variable responsiveness of the current-meter (u_{cm}), width measurement instrument (u_{bm}) and depth sounding instrument (u_{ds}).

$$u_s = \sqrt{u_{cm}^2 + u_{bm}^2 + u_{ds}^2} \quad (20)$$

An estimated practical value of 1 % may be taken for this expression.

u_m is the uncertainty due to the limited number of verticals, and

m is the number of verticals.

The mean velocity $\bar{v}_i$ at vertical i is an estimate of the average of point measurements of velocity made at one or more depths in the vertical (see for example 7.1.5.3). The uncertainty in $\bar{v}_i$ is computed as follows:

$$u(\bar{v}_i)^2 = u_{p,i}^2 + \left(\frac{1}{n_i}\right)(u_{c,i}^2 + u_{e,i}^2) \quad (21)$$

where

- $u_{p,i}^2$ is the uncertainty in mean velocity $\bar{v}_i$ due to the limited number of depths at which velocity measurements are made at vertical i ;
- n_i is the number of depths in the vertical i at which velocity measurements are made;
- $u_{c,i}$ is the uncertainty in the velocity at a particular measuring point in vertical i due to lack of repeatability of the current-meter;
- $u_{e,i}$ is the uncertainty in point velocity at a particular depth in vertical i due to velocity fluctuations (pulsations) in the stream during the exposure time of the current-meter.

Combining Equations (19) and (21) yields:

$$u(Q)^2 = u_m^2 + u_s^2 + \frac{\sum_{i=1}^m (b_i d_i \bar{v}_i)^2 \left(u_{b,i}^2 + u_{d,i}^2 + u_{p,i}^2 \left(\frac{1}{n_i} \right) (u_{c,i}^2 + u_{e,i}^2) \right)}{\left(\sum_{i=1}^m (b_i d_i \bar{v}_i) \right)^2} \quad (22)$$

If the measurement verticals are placed so that the segment discharges ($b_i d_i \bar{v}_i$) are approximately equal and if the component uncertainties are equal from vertical to vertical, then Equation (22) simplifies to:

$$u(Q) = \left[u_m^2 + u_s^2 + \left(\frac{1}{m} \right) \left(u_b^2 + u_d^2 + u_p^2 + \left(\frac{1}{n} \right) (u_c^2 + u_e^2) \right) \right]^{1/2} \quad (23)$$

9.3.3 Example

It is required to estimate the uncertainty in a current-meter gauging from the following particulars:

Number of verticals used in the gauging	20
Number of points taken in the vertical (0,2 and 0,8)	2
Average velocity in measuring section	above 0,3 m/s
Exposure time of current-meter	3 min
Rating of current-meter	individual rating

Component uncertainties (percentages) can be obtained from information given in Annex E, which presents the results of investigations carried out since the publication of the first edition of this International Standard in 1968.

u_m	2,5	(Table E.6)
u_s	1,0	(see above)
u_b	0,5	(see E.2 line 1)
u_d	0,5	(see E.3 line 2)
u_p	3,5	(Table E.4)
u_c	1,0	(Table E.5)
u_e	3,0 (at 0,2 depth)	(Table E.3)
	3,0 (at 0,8 depth)	(Table E.3)

Therefore

$$u_e = \sqrt{3^2 + 3^2} = 4,2$$

9.3.4 Combined uncertainty

Therefore, from Equation (23):

$$u(Q) = \left[u_m^2 + u_s^2 + \left(\frac{1}{m} \right) (u_b^2 + u_d^2 + u_p^2 + \left(\frac{1}{n} \right) (u_c^2 + u_e^2)) \right]^{1/2}$$

$$u(Q) = \left[2,5^2 + 1,0^2 + \left(\frac{1}{20} \right) (0,5^2 + 0,5^2 + 3,5^2 + \left(\frac{1}{2} \right) (1,0^2 + 4,2^2)) \right]^{1/2}$$

giving

$$u(Q) = 2,89 \%$$

The expanded uncertainty at the 95 % confidence level, U_{95} , is obtained by applying a coverage factor of $k = 2$,

Thus:

$$\begin{aligned} U_{95}(Q) &= k \cdot u(Q) \\ &= 2 \times 2,89 \\ &= 5,78 \% \end{aligned}$$

Therefore

$$U_{95}(Q) = 6 \%$$

Now, if the measured flow is $Q \text{ m}^3/\text{s}$, the result of the measurement is expressed as:

$Q \text{ m}^3/\text{s} \pm 6 \%$ (expanded uncertainty, coverage factor $k = 2$, approximate level of confidence = 95 %).

9.4 Method of calculating the uncertainty in discharge by measurement of velocity using floats

9.4.1 General

Whilst there have been considerable investigations carried out into the uncertainties in current-meter gauging, little work has been performed into the uncertainties in float gauging. As a result, there is little guidance in the literature and little research reported to allow reliable recommendations to be made. The following analysis is therefore given as a guide until more information is available.

9.4.2 Contributory uncertainties

The equation for discharge is: (see 7.2 and 8.6)

$$Q = F \sum K_f \bar{v}_i \left(\frac{A'_i + A_i}{2} \right) \quad (24)$$

where

Q is the discharge (cubic metres per second);

F is a factor, assumed to be unity, that relates the discrete sum over the finite number of verticals to the integral of the continuous function over the cross-section;

K_f is the coefficient of velocity for the float;

$\bar{v}_i$ is the mean float velocity in the i th segment;

A_i and A'_i are the i th segment areas of upstream and downstream cross-sections, respectively.

The overall uncertainty in discharge is composed of

- uncertainties in width: $u_{b,i}$ in estimating cross-section areas,
- uncertainties in depth: $u_{d,i}$ in estimating cross-section areas (allowing for scour and fill if any),

c) uncertainties in determination of surface float velocities: $u_{v,i}$

composed of:

- the uncertainty in the coefficient of velocity for the float, $u_{k,f}$
- the uncertainty of the length of travel path, $u_{L,i}$
- the uncertainty of the time taken for the passage of the float, $u_{t,i}$

where

$$u_{v,i}^2 = u_{k,f}^2 + u_{L,i}^2 + u_{t,i}^2 \quad (25)$$

d) uncertainty due to the limited number of segments used, u_m .

9.4.3 Combined uncertainty in discharge

The method of calculation is similar to that given in 9.3.2.

$$u_Q = \sqrt{u_m^2 + \frac{1}{m}(u_b^2 + u_d^2 + u_v^2)} \quad (26)$$

9.4.4 Example

Float gauging with 5 paths using surface floats:

$u_m = 7,5 \%$ (Table E.6) This may be reduced provided the areas are determined from a detailed cross-section and the velocities are determined from a smoothed velocity distribution.

$u_{k,f} = 15 \%$ (Table E.4)

$u_L = 5 \%$ (estimated)

$u_t = 5 \%$ (estimated)

$$\begin{aligned} u_v &= \sqrt{u_{k,f}^2 + u_L^2 + u_t^2} \\ &= \sqrt{15^2 + 5^2 + 5^2} \\ &= 16,5 \% \text{ (or taken from Table E.4 alone = 15 \%)} \end{aligned}$$

$u_b = 1 \%$ (estimated)

$u_d = 1 \%$ (estimated)

therefore

$$\begin{aligned} u(Q) &= \sqrt{7,5^2 + \frac{1}{5}(1 + 1 + 16,5^2)} \\ u(Q) &= 10,5 \% \end{aligned}$$

The expanded uncertainty at a level of confidence of approximately 95 %, U_{95} , is obtained by applying a coverage factor of $k = 2$.

Then

$$U_{95}(Q) = k \cdot u(Q)$$

$$= 2 \times 10,5$$

$$= 21 \%$$

Therefore

$$U_{95}(Q) = 21 \%$$

Now, if the measured flow is Q m³/s, the result of the measurement is expressed as:

$$Q \text{ m}^3/\text{s} \pm 21 \% \text{ (expanded uncertainty, coverage } k = 2, \text{ approximate level of confidence} = 95 \%)$$

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Annex A (informative)

Correction for sag, pull, slope and temperature in measurement of cross-section width by tape or wire

A.1 Correction for sag

A.1.1 The correction due to sag of the measuring tape or wire to be applied to the measured length is given by the following formula:

$$k_s = \frac{m^2 l^3}{24 F_T^2} \quad (\text{A.1})$$

where

k_s is the sag correction for length (shortening);

m is the mass of tape or wire per unit length;

l is the actual length of tape or wire which has been previously measured;

F_T is the cable tension.

A.1.2 When the tape or wire has been calibrated on the flat, the horizontal distance between the end marks when it is used in catenary are obtained by subtracting the sag correction from the calibrated length on the flat. Similarly if the tape or wire was calibrated in catenary, the true length on the flat is obtained by adding the catenary correction.

A.1.3 For odd lengths, or lengths differing from that in which the tape or wire was calibrated, the correction for the particular span involved is subtracted from that span to give the corrected horizontal distance if the tape or wire was calibrated on the flat; if it was calibrated in catenary, the correction to be applied is given by Equation (A.2):

$$k = \left(\frac{x}{l} \right) k_s - k_x \quad (\text{A.2})$$

where

k is the correction;

x is the length of span involved;

k_s is the sag correction for length l ;

k_x is the sag correction for length x .

The above correction is positive if x is less than l , it is negative if x is more than l .

A.2 Correction for pull

A.2.1 If the pull applied to the tape or wire is not the same as that used during calibration, the following correction for pull shall be applied:

$$k_f = \frac{l(F_T - F_l)}{AE} \quad (\text{A.3})$$

where

k_f is the length correction for pull;

l is the actual length of tape or wire;

F_T is the pull at the time of measurement;

F_l is the pull corresponding to l during calibration;

A is the area of cross-section of tape or wire;

E is the Young's modulus of the material of the tape or wire.

A.3 Correction for slope

A.3.1 The correction for slope, if measured as an angle, is given by Equation (A.4):

$$k_i = l(1 - \cos \beta) \quad (\text{A.4})$$

where

k_i is the correction for slope;

β is the angle of slope.

A.3.2 The correction for slope, if measured as a difference in height, is given by Equation (A.5):

$$k_i = \frac{y^2}{2l} - \frac{y^4}{8l^3} \quad (\text{A.5})$$

where y is the difference in height.

NOTE 1 The term $\frac{y^4}{8l^3}$ is negligible for a slope of about 8° or less.

NOTE 2 This correction is always negative.

A.4 Correction for temperature

The correction due to temperature is negative or positive according to whether the temperature at measurement time is less or more than the temperature at calibration of the tape or wire, and is given by Equation (A.6):

$$k_1 = l\lambda\Delta\theta \quad (\text{A.6})$$

where

l is the actual length of tape or wire;

k_1 is the correction for temperature;

λ is the coefficient of thermal expansion;

$\Delta\theta$ is the increase or decrease in temperature from the temperature at calibration.

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Annex B (informative)

Distance measurement across the cross-section

B.1 Angular method

A theodolite is set up on one of the banks and angular measurements taken to the boat used for taking soundings and its position fixed (see Figure B.1). Alternatively, a sextant may be used from the boat to note the readings to two flags, one fixed on the cross-section and the other at right angles to it.

$$MC = CE \tan \alpha \quad (B.1)$$

B.2 Linear method

Four flags (A, B, C and D) are fixed, two on each bank along the cross-section line (see Figure B.2). One more flag, E, is fixed on one of the banks on a line at right angles to the cross-section line and passing through the flag point B, nearer to the water's edge and at a known distance from it (BE). An observer, with a flag in his hand, then moves along the bank from C, towards a position N, along a line perpendicular to the cross-sectional line, until the corresponding flag E on the opposite bank, the flag on the boat M, and the flag in his hand N are all in one line. The perpendicular distance from the flag in his hand to the cross-section line (CN) is determined and the distance of the boat is computed as follows:

$$MC = CN \tan \alpha \quad \text{where } \alpha = \hat{C}NM$$

$$\tan \alpha = \frac{BC}{(BE + CN)}$$

$$\therefore MC = \frac{CN \times BC}{BE + CN} \quad (B.2)$$

If the channel is very wide so that objects on the opposite bank are not clearly visible, the position of the boat is fixed from measurements made on one bank only (see Figure B.3). Two flags (N and E), on lines perpendicular to the cross-sectional line, and on the same side, are marked on one bank of the river such that the distance of the boat is computed as follows:

$$MD = DE \tan \theta \quad (B.3)$$

where $\theta = \hat{M}ED$.

B.3 Pivot-point method

When the river is wide and flat land is available, the pivot-point method may be used. In Figure B.4, the distance AP is approximately half the width of the river and PD is about one-fifth of AP. On line DD', points are marked at fixed intervals depending on the width between the selected verticals. The boat moving on line A A' can be fixed in the selected vertical by lining up with points P and E₁, E₂, etc. A second set of pivot-points on the other bank may be used if required. The computation is undertaken as follows:

$$\frac{AB_n}{PA} = \frac{DE_n}{PD}$$

$$\therefore AB_n = \frac{DE_n \times PA}{PD} \quad (\text{B.4})$$

where n is the number of pivot points.

B.4 Other methods

Other methods using high technology such as Differential Global Positioning Systems (DGPS) are available.

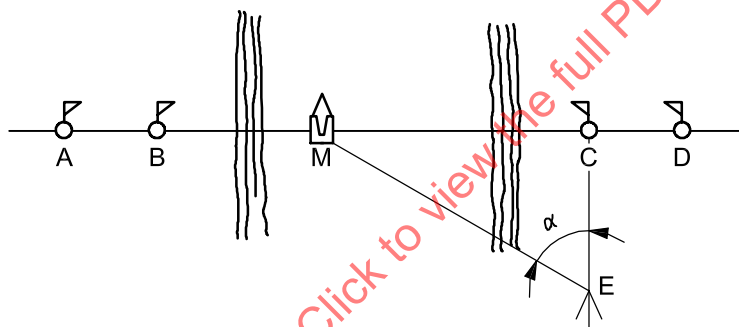


Figure B.1 — Angular method

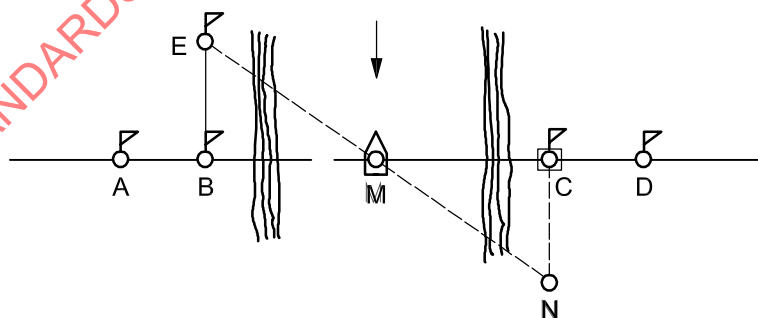


Figure B.2 — Linear method

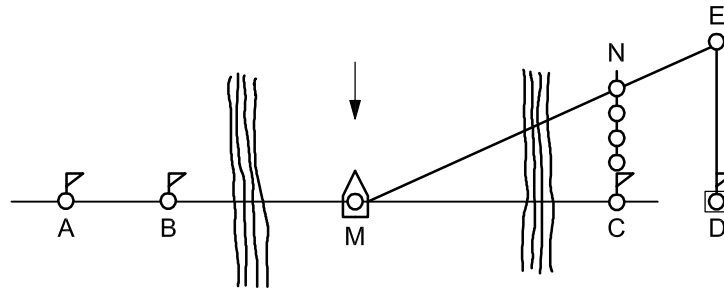
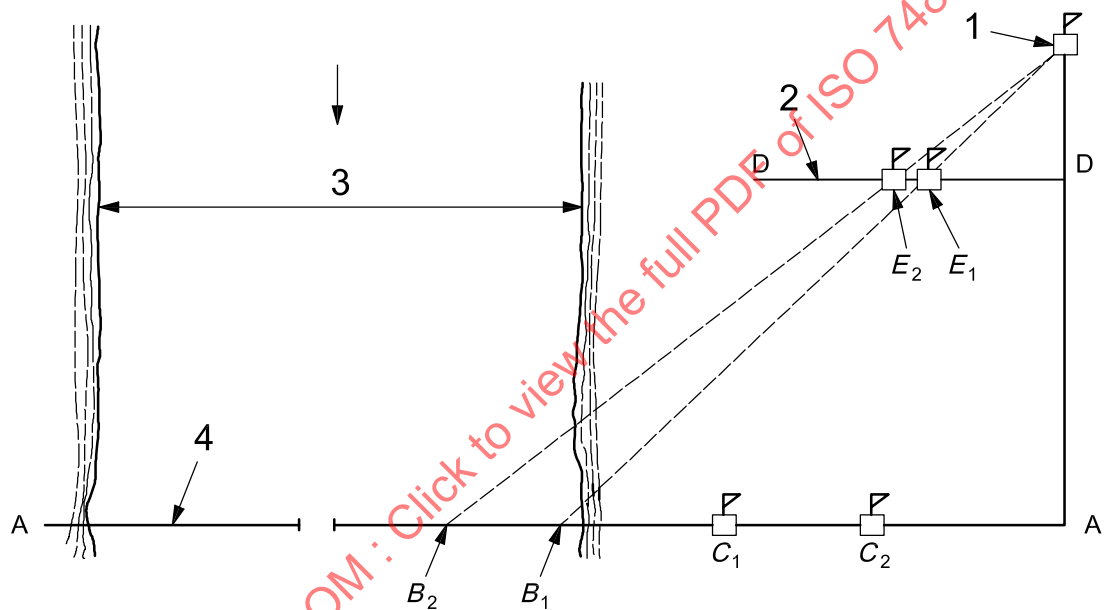


Figure B.3 — Linear method from one bank



Key

- 1 pivot point
- 2 line of direction blocks
- 3 channel width
- 4 cross-section line

Figure B.4 — Pivot-point method

Annex C (informative)

Corrections for wetted length of wire when measuring depths with wire not normal to surface

C.1 The following tables are based on *Measurement and computation of streamflow, Vol. 1, Measurement of stage and discharge*, the United States Geological Survey, Water Supply, Paper No. 2175, 1982. It should be noted that a correction must also be made for the change between the vertical length and the slant length of the line above the water surface. If the point of suspension of the sounding line is at a vertical distance X above the surface and the angle between the sounding line and vertical is a , then the air line correction k_{1a} to be applied is given by the formula:

$$k_{1a} = (\sec a - 1) X \quad (\text{C.1})$$

The percentage correction ($k_{1a} \cdot 100/X$) to be deducted from the measured length of the sounding line, for angles up to 30° , is given in Table C.1.

Table C.1 — Air-line correction

Vertical angle	Correction %	Vertical angle	Correction %
4°	0,24	18°	5,15
6°	0,55	20°	6,42
8°	0,98	22°	7,85
10°	1,54	24°	9,46
12°	2,23	26°	11,26
14°	3,06	28°	13,26
16°	4,03	30°	15,47

The wet-line correction k_{1w} (see Table C.2), also expressed as a percentage to be deducted from the measured length of the sounding line, is estimated on the assumptions that the horizontal drag pressure on the weight in the comparatively still water near the bottom can be neglected, that the velocity distribution in the vertical is normal, and that the sounding wire and the weight are designed to offer little resistance to the water current.

The uncertainties in this estimation are such that significant errors may be introduced if the angle of the sounding wire with the vertical is more than 30° .

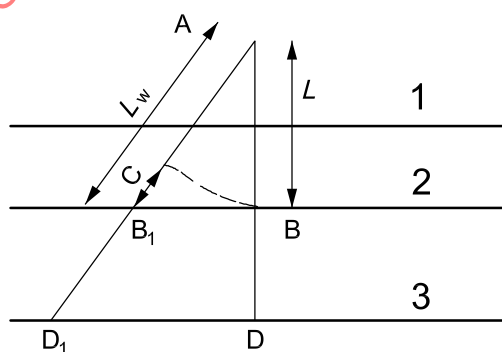
Table C.2 — Wet line correction

Vertical angle	Correction %	Vertical angle	Correction %
4°	0,06	18°	1,64
6°	0,16	20°	2,04
8°	0,32	22°	2,48
10°	0,50	24°	2,96
12°	0,72	26°	3,50
14°	0,98	28°	4,08
16°	1,28	30°	4,72

The corrections given in this table are percentages of the wet-line depth (see also ISO/TR 9209).

C.2 Figure C.1 shows a typical situation where the position of a current-meter is affected by the velocity of the water. The required position for the current-meter is at point B, a distance L from the point of suspension. The velocity of the water will cause the current-meter to be pulled downstream so that the angle of suspension is α .

$$\begin{aligned}\cos \alpha &= \frac{L}{L_W} \\ L_W &= L + C \\ \therefore \cos \alpha &= \frac{L}{L + C} \\ L + C &= \frac{L}{\cos \alpha} \\ C &= \frac{L}{\cos \alpha} - L\end{aligned}$$



Key

- 1 water level
- 2 point of suspension
- 3 bed level

Figure C.1 — Wet line correction

If the cross-section is pre-surveyed then the value of L is either known or can be measured on site. The angle α can be measured and the correction factor C calculated. The process may be iterative as the angle, α , may alter as the current-meter is lowered into the water.