
**Refrigerated hydrocarbon and non-
petroleum based liquefied gaseous
fuels — Calibration of membrane tanks
and independent prismatic tanks in
ships — Manual and internal electro-
optical distance-ranging methods**

*Hydrocarbures réfrigérés et combustibles gazeux liquéfiés à base non
pétrolière — Étalonnage des réservoirs à membrane et réservoirs
pyramidaux — Méthodes manuelles et par mesurage électro-optique
interne de la distance*



STANDARDSISO.COM : Click to view the full PDF of ISO 8311:2013



COPYRIGHT PROTECTED DOCUMENT

© ISO 2013

All rights reserved. Unless otherwise specified, no part of this publication may be reproduced or utilized otherwise in any form or by any means, electronic or mechanical, including photocopying, or posting on the internet or an intranet, without prior written permission. Permission can be requested from either ISO at the address below or ISO's member body in the country of the requester.

ISO copyright office
Case postale 56 • CH-1211 Geneva 20
Tel. + 41 22 749 01 11
Fax + 41 22 749 09 47
E-mail copyright@iso.org
Web www.iso.org

Published in Switzerland

Contents

Page

Foreword	iv
Introduction	v
1 Scope	1
2 Normative references	1
3 Terms and definitions	1
4 Precautions	3
4.1 General	3
4.2 Ship's condition during calibration	3
4.3 Tank distortion	3
4.4 Comparison with drawings	4
4.5 Measurements by measuring tape	4
4.6 Measurements by electro-optical distance-ranging (EODR) instrument	4
4.7 Condition of membrane	5
4.8 Safety precautions for work in membrane tanks	5
5 Equipment	5
6 Determination of measuring points	6
7 Calibration by manual method	6
7.1 General	6
7.2 Tank length measurement	7
7.3 Tank width measurement	9
7.4 Tank height measurement	12
7.5 Measurement of bottom undulation and gauge reference height	14
7.6 Correction for temperature	15
8 Calibration by electro-optical distance-ranging (EODR) method	16
8.1 General	16
8.2 Setting up of EODR instrument	16
8.3 Calibration procedure	17
9 Additional measurements	19
9.1 Location of level gauge	19
9.2 Deadwood	19
10 Calculation	19
10.1 General	19
10.2 Calculation of tank volume	20
10.3 Effect of bottom undulation	20
10.4 Area of chamfer portion	20
10.5 Trim corrections	21
10.6 List corrections	21
10.7 Combined trim and list corrections	21
10.8 Correction for tank shell expansion or contraction	21
11 Report and tables	22
12 Recalibration	23
Annex A (informative) Uncertainty associated with tank calibration	24
Annex B (informative) Example of tank capacity table (Tank No.3)	36
Annex C (informative) Example of trim correction table (Tank No. 1)	38
Annex D (informative) Example of list correction table (Tank No. 1)	40
Bibliography	42

Foreword

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

The procedures used to develop this document and those intended for its further maintenance are described in the ISO/IEC Directives, Part 1. In particular the different approval criteria needed for the different types of ISO documents should be noted. This document was drafted in accordance with the editorial rules of the ISO/IEC Directives, Part 2. www.iso.org/directives

Attention is drawn to the possibility that some of the elements of this document may be the subject of patent rights. ISO shall not be held responsible for identifying any or all such patent rights. Details of any patent rights identified during the development of the document will be in the Introduction and/or on the ISO list of patent declarations received. www.iso.org/patents

Any trade name used in this document is information given for the convenience of users and does not constitute an endorsement.

For an explanation on the meaning of ISO specific terms and expressions related to conformity assessment, as well as information about ISO's adherence to the WTO principles in the Technical Barriers to Trade (TBT) see the following URL: Foreword - Supplementary information

The committee responsible for this document is ISO/TC 28, *Petroleum products and lubricants*, Subcommittee SC 5, *Measurement of refrigerated hydrocarbon and non-petroleum based liquefied gaseous fuels*.

This second edition cancels and replaces the first edition (ISO 8311:1989), which has been technically revised.

Introduction

Large quantities of light hydrocarbons consisting of compounds having one to four carbon atoms are stored and transported by sea as refrigerated liquids at pressures close to atmospheric. These liquids can be divided into two main groups, liquefied natural gas (LNG) and liquefied petroleum gas (LPG). Bulk transportation of these liquids requires special technology in ship design and construction to enable ship-borne transportation to be safe and economical.

Quantification of these cargoes in ships' tanks for custody transfer purposes has to be of a high order of accuracy. This International Standard (together with others in the group) specifies methods of internal measurement of ships' tanks, from which tank capacity tables can be derived.

This International Standard covers calibration techniques applicable to membrane type tanks, i.e. self-supporting independent tanks in which the containment system comprises a relatively thin membrane of either stainless steel or high-nickel steel alloy. This International Standard, with some modification, can also be applicable to the calibration of independent prismatic tanks.

[Annex A](#) gives uncertainty associated with the measurement of membrane tanks.

[Annex B](#) gives an example of a tank capacity table relating partial filling volume as a function of liquid level and [Annexes C](#) and [D](#) give examples of trim correction and list correction tables, respectively.

STANDARDSISO.COM : Click to view the full PDF of ISO 8311:2013

STANDARDSISO.COM : Click to view the full PDF of ISO 8311:2013

Refrigerated hydrocarbon and non-petroleum based liquefied gaseous fuels — Calibration of membrane tanks and independent prismatic tanks in ships — Manual and internal electro-optical distance-ranging methods

1 Scope

This International Standard specifies a method for the internal measurement of membrane tanks used in ships for the transport of refrigerated light hydrocarbon fluids. In addition to the actual process of measurement, it sets out the calculation procedures for compiling the tank capacity table and correction tables to be used for the computation of cargo quantities. This International Standard, with some modification, can also be applicable to the calibration of independent prismatic tanks.

For the manual measurement of membrane tanks, the procedures of this International Standard utilize the scaffolding used for the installation of the membranes to support the measuring equipment but, for the internal electro-optical distance-ranging (EODR) method, other safe means of access to the required measuring positions are intended to be used.

2 Normative references

The following documents, in whole or in part, are normatively referenced in this document and are indispensable for its application. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

ISO 7507-1:2003, *Petroleum and liquid petroleum products — Calibration of vertical cylindrical tanks — Part 1: Strapping method*

ISO 7507-4:2010, *Petroleum and liquid petroleum products — Calibration of vertical cylindrical tanks — Part 4: Internal electro-optical distance-ranging method*

IEC 60079-10-1, *Explosive atmospheres — Part 10-1: Classification of areas — Explosive gas atmospheres*

IEC 60079-10-2, *Explosive atmospheres — Part 10-2: Classification of areas — Combustible dust atmospheres*

IEC 60825-1, *Safety of laser products — Part 1: Equipment classification and requirements*

3 Terms and definitions

For the purposes of this document, the following terms and definitions apply.

3.1

automatic tank gauge

ATG

automatic level gauge

ALG

instrument that continuously measures liquid height (dip or ullage) in storage tanks

3.2

chamfer

slanting surface connecting the walls of a tank with its top or bottom surface

3.3

deadwood

any tank fitting that affects the capacity of a tank

3.4

gauge reference point

point from which the liquid depth are measured

3.5

horizontal plane

any plane established parallel to the tank bottom

3.6

horizontal reference line

any horizontal line established by a string

Note 1 to entry: A calibration method using this line is adopted as an alternative to direct measurements, where it is considered impractical to take direct measurements.

3.7

list

transverse inclination of a ship

Note 1 to entry: It is expressed in degrees.

3.8

longitudinal line

line formed by a longitudinal plane crossing a horizontal plane

3.9

longitudinal plane

vertical plane running parallel to the centreline of the tank

3.10

measuring point

one of a series of points on the inside surface of the tank shell from/to which the distance is measured by a tape or a hand-held laser distance meter in case of manual method, or to which the slope distance, vertical angles and horizontal angles are measured by use of the electro-optical distance-ranging instrument

3.11

port

left-hand side of a ship facing forward

3.12

reference target point

fixed point clearly marked on the inside surface to the tank shell or a prism mounted on a tripod

3.13

section line

line formed by a section plane crossing a horizontal plane

3.14

section plane

plane parallel with the fore and aft end walls of a ship's tank

3.15

slope distance

distance measured from the electro-optical distance-ranging instrument to any measuring point or a reference target point

3.16**starboard**

right-hand side of a ship facing forward

3.17**tank-calibration reference temperature**

temperature at which the calibration of a tank has been calculated

3.18**tank capacity table**

tank table

calibration table

capacity table

table showing the capacities of, or volumes in, a tank corresponding to various liquid levels measured from a reference point

3.19**trim**

difference between the fore and aft draught of the vessel

Note 1 to entry: When the aft draught is greater than the forward draught, the vessel is said to be trimmed by the stern. When the aft draught is less than the forward draught, the vessel is said to be trimmed by the head.

3.20**uncertainty**

U

estimate characterizing the range of values within which the true value of a measurand lies

Note 1 to entry: Various types of uncertainty are defined in ISO/IEC Guide 98-3.

3.21**vertical line**

line formed by a section plane on the side walls and formed by a longitudinal plane on the fore and aft end walls

4 Precautions**4.1 General**

This clause outlines the precautions to be taken during measurement. Utmost care and attention shall be exercised in taking measurements, and any unusual occurrence during the measuring work, which might affect the results, shall be recorded.

4.2 Ship's condition during calibration

The calibration methods described in this International Standard may be applied to ships whether afloat or in a dry dock. However, its use for ships in a dry dock is preferred, because trim or list, if any, will remain the same throughout the calibration procedure. Adjustments, manually or automatically shall be made to any measurement by optical level and EODR if the ship's attitude has changed.

4.3 Tank distortion

If unusual distortion is found in the tank, additional measurement shall be taken by the calibrator as considered necessary and sufficient. Notes by the calibrator detailing the extra measurements and the reasons for them shall be included in the calibration report.

The calibrator shall provide detailed sketches of any abnormality of the tank or its fittings where such sketches can materially assist the interpretation of the recorded data.

4.4 Comparison with drawings

If drawings for the tank are available, all measurements taken shall be compared with the corresponding dimensions shown on the drawings. Any measurement showing a significant discrepancy in this comparison shall be rechecked; however, the tank capacity table shall be based on the actual measurements.

4.5 Measurements by measuring tape

When measurements are made with a measuring tape:

- a) the tension specified in the tape calibration certificate shall be applied;
- b) the measuring tape shall be supported so as to prevent it from sagging. If tape sag is unavoidable, the calibrator shall note this and a catenary correction shall be applied during calculation;
- c) take multiple measurements. If the first three consecutive measurements agree within the tolerances specified in d) below, take their mean as the measurement and their standard deviation as the standard uncertainty. If they do not agree within the tolerances specified in d) below, repeat the measurements until two standard deviations of the mean of all measurements is less than the half of the tolerance specified in d) below. Use the mean as the measurement and the standard deviation as the standard uncertainty. Use standard procedures to eliminate obvious outliers;
- d) the following table shows the tolerances against the measurement distance:

Measurement	Tolerance within
Up to 25 m	2 mm
over 25 m	3 mm
for offset	0,5 mm

- e) if the measurements have been interrupted, the last measurements shall be repeated. If the new measurements do not agree, within the required tolerance, with the earlier measurements, then the earlier set shall be rejected.

4.6 Measurements by electro-optical distance-ranging (EODR) instrument

When measurements are carried out with an EODR instrument:

- a) the electro-optical distance-ranging instrument shall be verified prior to calibration. The accuracy of the distance-ranging unit as well as the angular measuring unit shall be verified using the procedures given by ISO 7507-4:2010, Annex A;
- b) the tank shall be free from vibration and air-borne dust particles. The floor of the tank should be as free as possible from debris, dust and scales;
- c) lighting, when required, shall be placed within the tank so as not to interfere with the operation the EODR instrument;
- d) the laser beam fitted to the EODR instrument shall be operated in conformity with IEC 60825-1. The hazards, if any, in the area in which the calibration is to be carried out shall be assessed in accordance with IEC 60079-10. The instrument to be used shall be declared (certified) as being safe for use in the area of operation.

4.7 Condition of membrane

Care shall be taken to ensure that the membrane is in contact with the supporting material. In some cases, it may be possible to ensure this contact by applying a vacuum to the space behind the membrane.

4.8 Safety precautions for work in membrane tanks

- a) All regulations covering entry into hazardous areas shall be rigorously observed.
- b) Before a tank which has been in use is entered, a safe-entry certificate issued in accordance with local or national regulations shall be obtained. All lines entering the tank shall be disconnected and blanked.
- c) Hand lamps and other electric instruments shall be of a type approved for use in explosive atmospheres.
- d) The safety of operating personnel shall be safeguarded by strict attention to the following.
 - 1) Ladders shall be inspected before use, and extendable ladders used only within their safe operating range. The footing for each ladder shall be level and firm, and all ladders shall be securely lashed in position before being used.
 - 2) Where painters' cradles or boatswains' (bo'suns') chairs are used, blocks, falls, ropes, etc., shall be tested before erection, and any item of questionable strength or condition shall be replaced. Every care shall be paid to the securing of the equipment and its operational use.
 - 3) If calibration cannot be carried out without the use of scaffoldings, properly constructed steel tube or timber scaffolding shall be erected. Loose bricks, drums, boxes, etc., shall not be used to form staging. Special attention shall be paid at the corners of the scaffolding. It is not uncommon for a plank to be moved from its position on the scaffolding when the tank wall is being lined with membranes.
 - 4) Where appropriate, safety harnesses shall be worn by the calibrator working above ground level.
- e) In some cases, edges of the anchor plates projecting from membrane can be sharp. The use of protective gloves and helmets is especially advised.
- f) Care shall be taken not to damage the membranes with shoes, measuring equipment, etc.

5 Equipment

The equipment used to calibrate the tanks in accordance with this International Standard are intended to conform to the relevant national or other standard.

5.1 Electro-optical distance-ranging (EODR) instrument, capable of achieving uncertainties of tank volumes acceptable in legal metrology. The angular measuring part of the instrument should have a resolution of equal to or better than $3,142 \times 10^{-6}$ rad (0,2 mgon), and the distance-measuring part of the instrument, which is to be used for direct determination of distances, should have a resolution of equal to or better than 1 mm.

The accuracy of EODR equipment can be affected by variations of temperature. The manufacturer's guidance should be followed.

5.2 Hand-held laser distance meter, which may be used, instead of measuring tape, to measure the distance. The hand-held laser distance meter should have a resolution of equal to or better than 1 mm.

5.3 Measuring tape, complying with the specifications for strapping tapes given in ISO 7507-1 or equivalent.

5.4 Automatic level, having an erect image and a magnification of $\times 20$ or greater, capable of being focused to 1,5 m or less and with a spirit level sensitivity of 40 s of arc per 2 mm or less.

5.5 Rule, with graduations in centimetres and millimetres, used to measure deadwood, the offsets between the strings and the tank walls in the case of the manual method, etc. If a wooden rule is used, it shall be fitted with a brass ferrule at each end and shall be free of warp.

5.6 Thermometer, having a suitable range, of an accuracy of $\pm 0,5$ °C.

A mercury thermometer should not be used.

6 Determination of measuring points

The calibration of membrane tanks is basically the measurement of the tank length, width and height between known points. These measuring points are determined by setting out a number of horizontal, longitudinal and section planes.

These planes intersect to form lines along which the measurements of length, width and height shall be taken. The various planes shall be set out at intervals not greater than 5 m; the interval shall be adjusted so that the resulting measurements reflect any change of section and adequately describe any deformation. The points at which measurements are to be taken shall be determined by the calibrator but shall not be more than 5 m apart.

Having determined the measuring points, mark the lines which run on the tank inner walls. Mark the section and longitudinal lines on the top and bottom plates, horizontal and vertical lines on the fore and aft end walls and horizontal and vertical lines on the port and starboard end walls. When measurements are made by an EODR, coordinates of the planned measuring points may be stored in the instrument instead of actually marking the lines or points on the tank inner walls.

7 Calibration by manual method

7.1 General

In the manual method, measurements of the distances between opposite walls of a tank shall be taken by tensioning the tape as specified on the tape certificate. A hand-held laser distance meter, in place of a tape, may be used for the direct measurements.

The lengths of the tanks shall be measured along all the longitudinal lines at each level of the horizontal planes in accordance with [7.2](#).

The widths of the tanks shall be measured along all the section lines set in each horizontal plane in accordance with [7.3](#).

The total heights, upper chamfer heights and side wall heights shall be measured and from these lower chamfer heights shall be calculated in accordance with [7.4](#).

[Annex A](#) gives uncertainty associated with the measurement of membrane tanks with the manual method.

7.2 Tank length measurement

7.2.1 Length measurement on the bottom plate

Measure the distances between the fore and aft end walls along all the longitudinal lines marked on the bottom plate with a measuring tape stretched thereon. The average length on the bottom plate is calculated using Formula (1):

$$L_l = \frac{1}{n} \sum_{i=1}^n L_{l,i} \quad (1)$$

where

- $L_{l,i}$ is the length of a longitudinal line on the bottom plate;
- L_l is the average length of the bottom plate;
- n is the number of longitudinal lines on the bottom plate.

7.2.2 Length measurement on the top plate

Measure the distances on the top plate in a manner similar to that for the bottom plate (see 7.2.1). Care shall be taken to keep the measuring tape in contact with the top plate. The average length on the top plate is calculated using Formula (2):

$$L_u = \frac{1}{n} \sum_{i=1}^n L_{u,i} \quad (2)$$

where

- $L_{u,i}$ is the length of a longitudinal line on the top plate;
- L_u is the average length of the top plate;
- n is the number of longitudinal lines on the top plate.

7.2.3 Length measurement in an intermediate horizontal plane

To avoid inaccurate measurement due to excessive sagging of the measuring tape, apply the horizontal reference line method using a string line.

As shown in Figure 1, lengths in these imaginary planes can be obtained by applying offset corrections at both ends, $a_2, a_3 \dots a_{n-1}$ and $b_2, b_3 \dots b_{n-1}$, to the length measured directly on the side wall. In practice, carry out the following.

- a) Mark P_1 and P_2 , S_1 and S_2 , on both side walls at equal distances from the end walls. Measure the length (L_P , L_S) between the fore and aft end walls with a measuring tape extended along both side walls, supporting the tape on the wall to prevent it from sagging.
- b) Stretch strings between the opposite points P_1 and S_1 , P_2 and S_2 , and measure the offsets between the strings and the end walls ($a_1, a_2 \dots a_n$ and $b_1, b_2 \dots b_n$) with a rule.
- c) In measuring these offsets, take care to put the measuring rule at a right angle to the string.

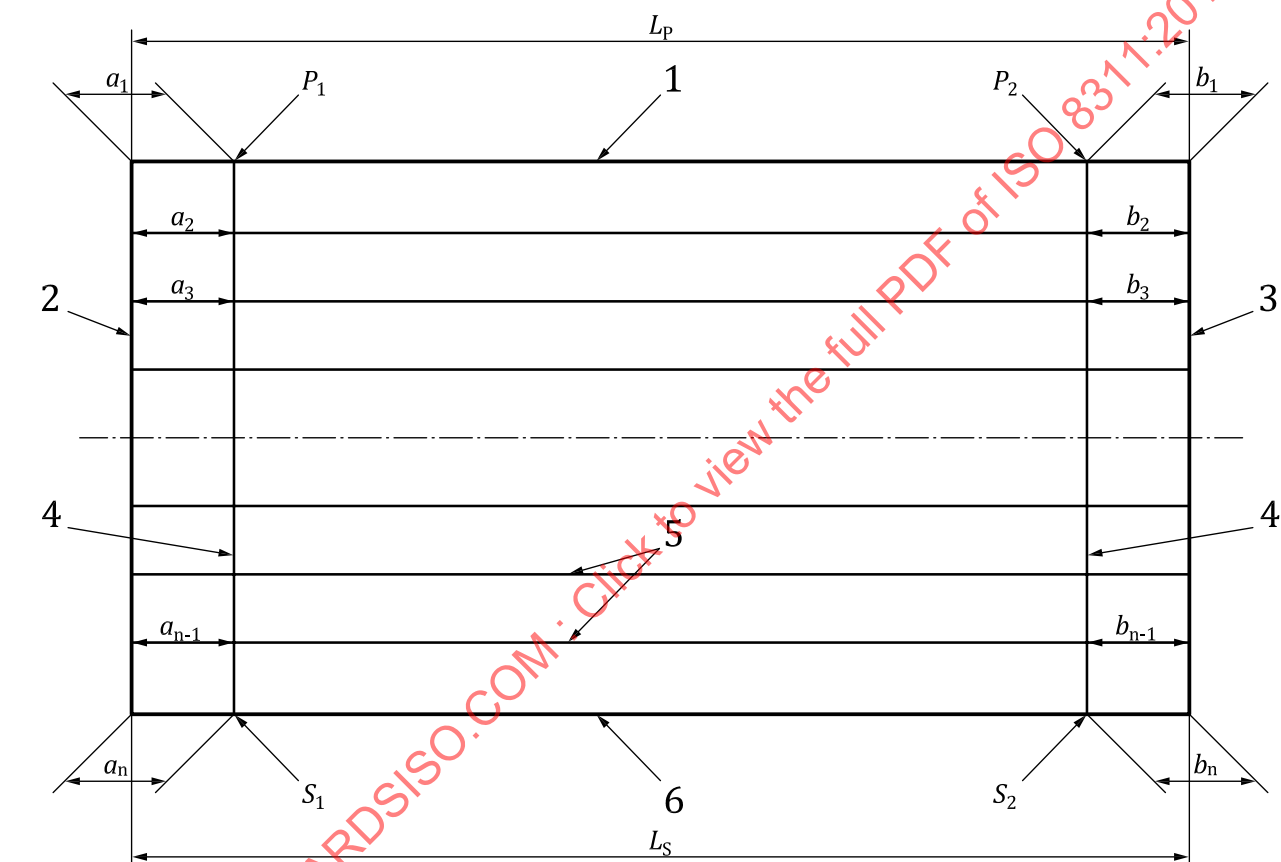
The average length of an intermediate horizontal plane, $L_{m,p}$ is calculated using Formula (3):

$$L_{m,p} = \frac{L_p + L_s - (a_1 + a_n + b_1 + b_n)}{2} + \frac{\sum_{i=1}^n (a_i + b_i)}{n} \quad (3)$$

The averaged length of intermediate part, L_m , is calculated using Formula (4):

$$L_m = \frac{1}{p-2} \sum_{j=2}^{p-1} L_{m,p} \quad (4)$$

where p is the number of intermediate planes.



Key

1	port side wall	4	string line
2	aft end wall	5	longitudinal lines
3	fore end wall	6	starboard side wall
L_p	length of port side wall		
L_s	length of starboard side wall		
P_1, P_2, S_1, S_2	markings on both side walls at equal distances from end walls		
$a_1, a_2 \dots a_n$ and b_1, b_2 $\dots b_n$	offsets between strings and end walls		

Figure 1 — Plan view of an intermediate horizontal plane

7.2.4 Tank length

The tank length, L , is calculated from L_u , L_m and L_l :

$$L = \frac{L_m \times (p-2) + L_u + L_l}{p} \quad (5)$$

Alternatively, another formula of equal or better accuracy may be used when it is considered adequate in the light of the shape of the tank.

7.3 Tank width measurement

7.3.1 Width measurement on the bottom plate

Measure distances between side walls along all the section lines marked on the bottom plate with a measuring tape stretched thereon. The average width on the bottom plate is calculated using Formula (6):

$$w_l = \frac{1}{n} \sum_{i=1}^n w_{l,i} \quad (6)$$

where

- $w_{l,i}$ is the width of a section line on the bottom plate;
- w_l is the average width of the bottom plate;
- n is the number of section lines on the bottom plate.

7.3.2 Width measurement on the top plate

Measure distances on the top plate in a manner similar to that for the bottom plate (see 7.3.1). Care shall be taken to keep the measuring tape in contact with the top plate. The average width on the top plate is calculated using Formula (7):

$$w_u = \frac{1}{n} \sum_{i=1}^n w_{u,i} \quad (7)$$

where

- $w_{u,i}$ is the width of a section line on the top plate;
- w_u is the average width of the top plate;
- n is the number of section lines on the top plate.

7.3.3 Width measurement on an intermediate horizontal plane

Measure tank width in the same way as in the length measurement by actual measurement of w_f and w_a in combination with the string as shown in Figure 2.

The average width of an intermediate horizontal plane, $w_{m,p}$ is calculated using Formula (8):

$$w_{m,p} = \frac{w_f + w_a - (c_1 + c_n + d_1 + d_n)}{2} + \frac{\sum_{i=1}^n (c_i + d_i)}{n} \quad (8)$$

The average of the averaged length of intermediate part, w_m , is calculated using Formula (9):

$$w_m = \frac{1}{p-2} \sum_{j=2}^{p-1} w_{m,p} \quad (9)$$

where p is the number of intermediate planes.

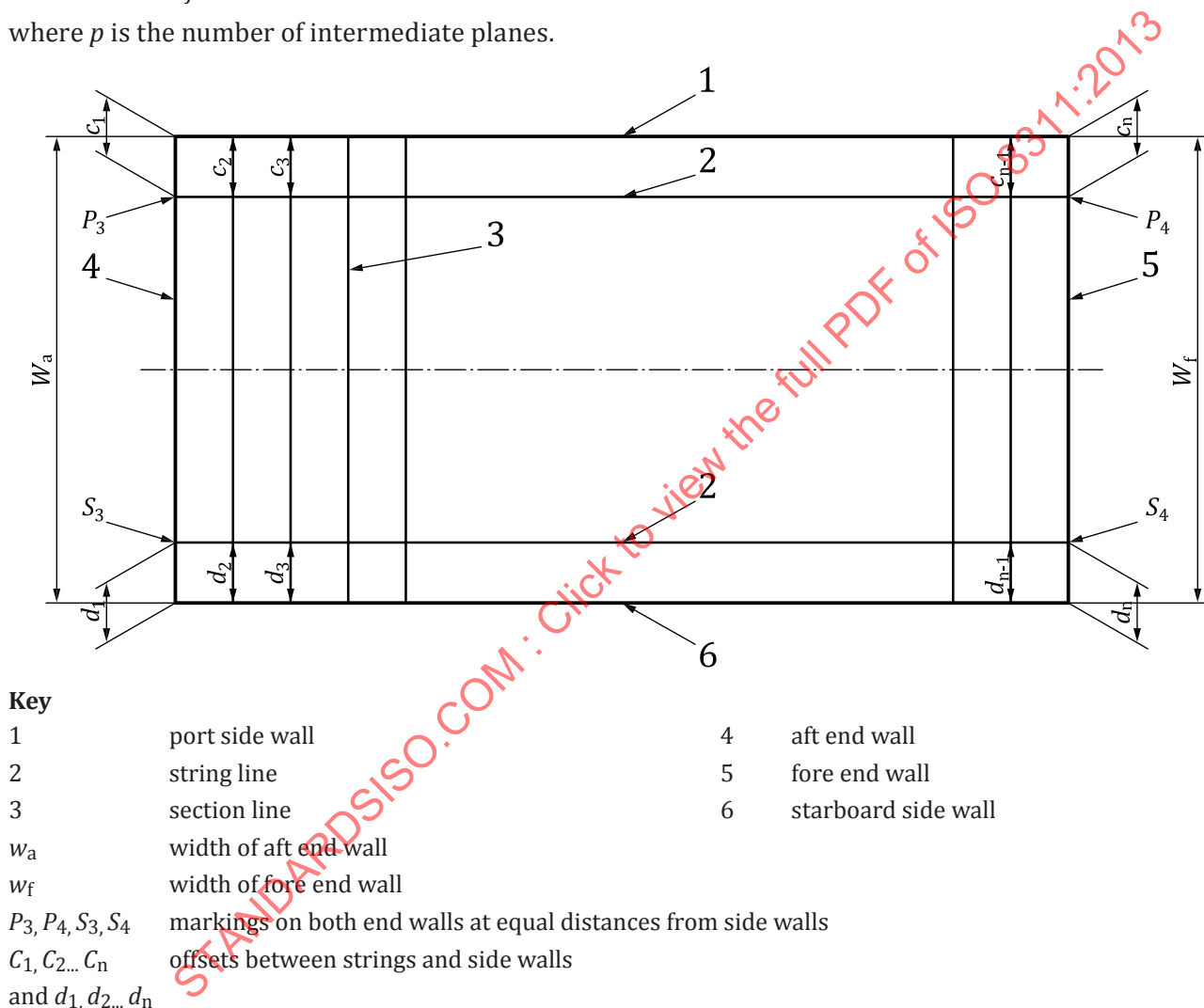


Figure 2 — Plan view of an intermediate horizontal plane

Alternatively, another formula of equal or better accuracy may be used when it is considered adequate. For example, side wall may be approximated by a linear regression line of the x - and y -coordinates of each measuring point on the side wall (see 8.3.3).

7.3.4 Trapezoidal tank

If the tank width is less at one end, measure the width in the intermediate horizontal planes in the same way as in 7.3.3, as shown in Figure 3.

The average width, w_f , of the fore end wall and the average width, w_a , of the aft end wall are calculated using Formulae (10) and (11).

$$w_f = w'_f - \frac{c'_1 + c'_n + d'_1 + d'_n}{2} + \frac{\sum_{i=1}^n (c'_i + d'_i)}{n} \quad (10)$$

and

$$w_a = w'_a - \frac{c'_1 + c'_n + d'_1 + d'_n}{2} + \frac{\sum_{i=1}^n (c'_i + d'_i)}{n} \quad (11)$$

where $c'_1, c'_2 \dots c'_n$ and $d'_1, d'_2 \dots d'_n$ are the offsets between strings and side walls.

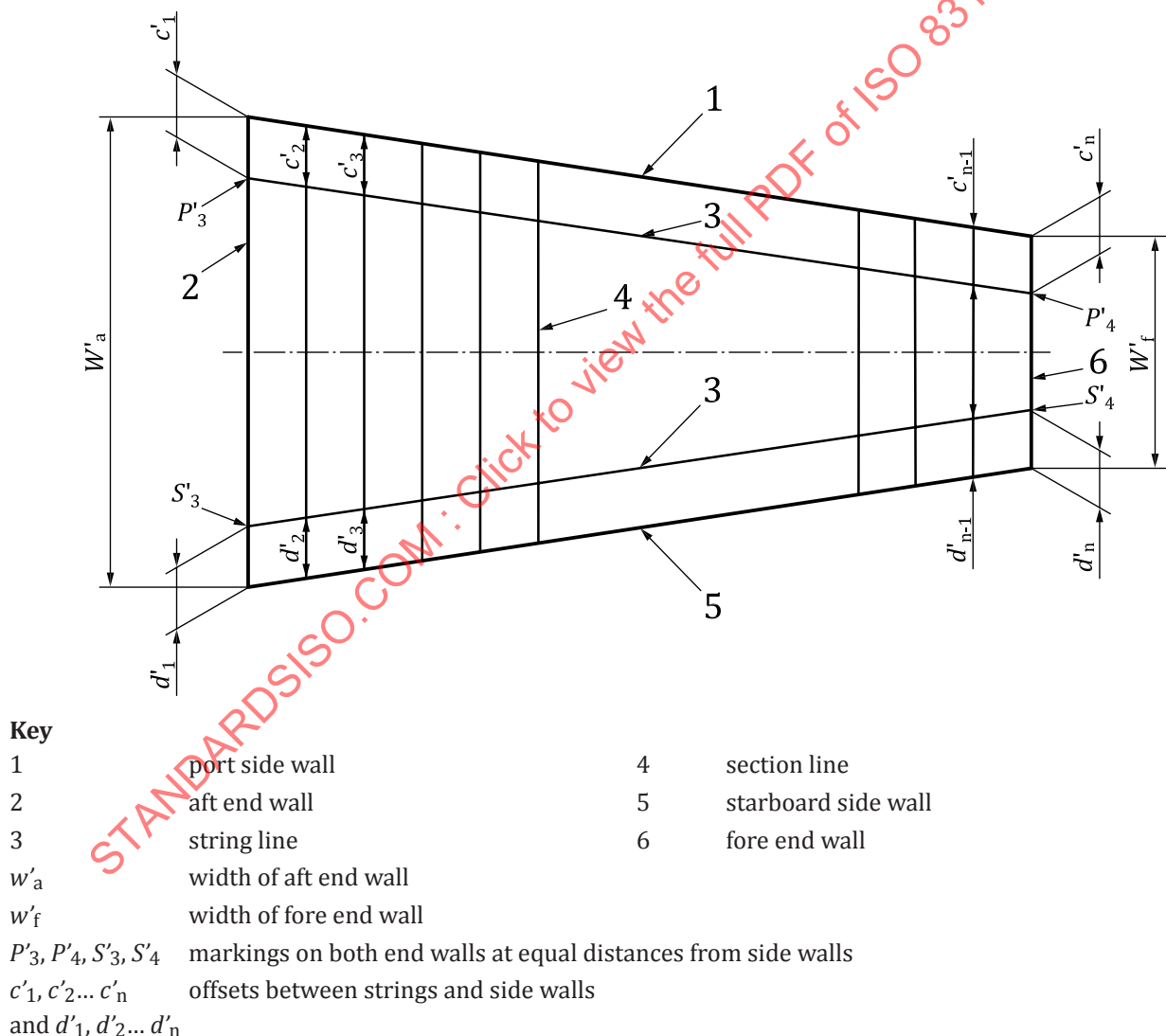
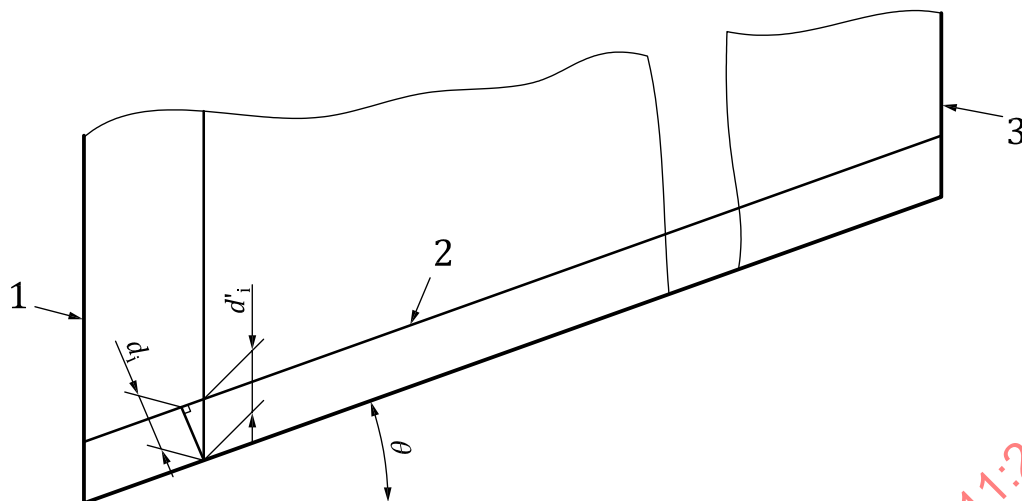


Figure 3 — Plan view of an intermediate horizontal plane (trapezoidal tank)

As shown in [Figure 3](#), the offsets to be taken in measuring the widths should theoretically be the ones parallel to the fore and aft end walls ($c'_1 \dots c'_n, d'_1 \dots d'_n$), and the offsets d_i measured at right angles to the side wall should be corrected, as shown in [Figure 4](#), to d'_i measured parallel to the fore and aft walls $d'_1 = d_1 / \cos \theta$ where θ is the angle between the side wall and the plane at right angles to the fore and aft walls.



Key

1 aft end wall

2 string line

3 fore end wall

d_i offsets at right angles to side wall

d'_i parallel to fore and aft walls by a formula, $d'_i = \frac{d_i}{\cos \theta}$

θ angle between side wall and plane at right angles to fore and aft walls, taken from the drawings

Figure 4 — Correction of offsets

Alternatively, another formula of equal or better accuracy may be used when it is considered adequate in the light of the shape of the tank. For example, side wall may be approximated by a linear regression line of the x - and y -coordinates of each measuring point on the side wall and the width calculated as distances between intersections of the fitted lines with the tank end walls (see 8.3.3).

7.4 Tank height measurement

7.4.1 Measurement of total height

On the top and bottom plates, draw section lines and longitudinal lines which will make grids on both plates. Using a measuring tape, measure the distances between the intersections of these lines on the top plate and the corresponding points on the bottom plate, i.e. along all vertical lines, and calculate the arithmetic mean using Formula (12):

$$h_t = \frac{1}{n} \sum_{i=1}^n h_{t,i} \quad (12)$$

where

$h_{t,i}$ is the total height along a vertical line;

h_t is the average total height;

n is the number of vertical lines.

Alternatively, another formula of equal or better precision may be used when it is considered adequate in the light of the shape of the tank. For example, the arithmetic mean may be the weighted average in case of trapezoidal tanks.

7.4.2 Measurement of side wall height

Measure the distance between the bottom of the upper chamfer and the top of the lower chamfer, along all vertical lines drawn on both side walls, and obtain the arithmetic mean using Formula (13):

$$h_m = \frac{1}{n} \sum_{i=1}^n h_{m,i} \quad (13)$$

where

$h_{m,i}$ is the side wall height along a vertical line;

h_m is the average side wall height;

n is the number of vertical lines.

7.4.3 Measurement of lower chamfer height

- Set a reference plane with an optical level approximately parallel to the bottom and the end walls with some clearance from the top of the lower chamfer.
- Measure height d_1 between this reference plane and the bottom plate along all the vertical lines, and take another measurement d_2 between the reference plane and the top of the lower chamfer at the corners of the tank.
- The height of the lower chamfer is calculated using Formulae (14) and (15):

$$h_{l,i} = d_{1,i} - d_{2,i} \quad (14)$$

$$h_l = \frac{1}{n} \sum_{i=1}^n h_{l,i} \quad (15)$$

where

$h_{l,i}$ is the lower chamfer height along a vertical line;

h_l is the average lower chamfer height;

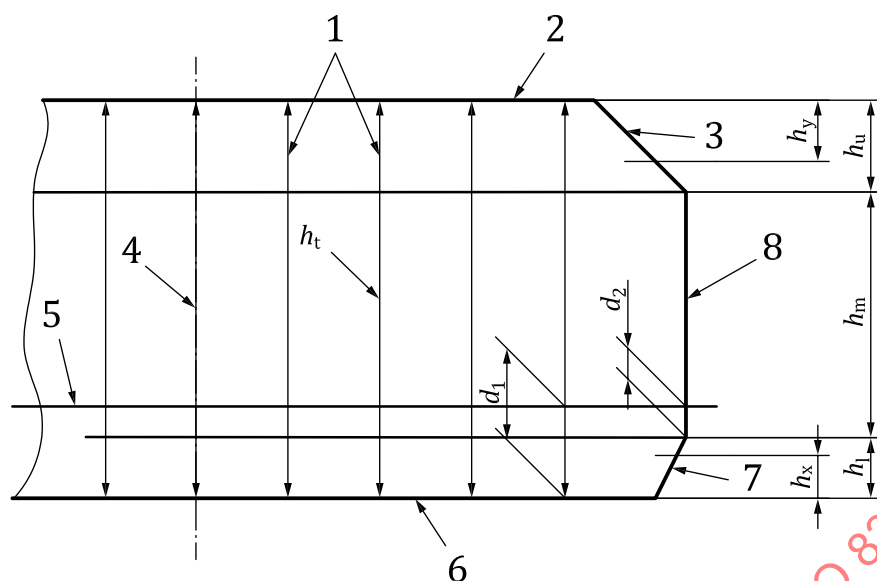
n is the number of vertical lines.

7.4.4 Height of upper chamfer

After heights h_t , h_m and h_l have been obtained, the height of the upper chamfer h_u is calculated using Formula (16):

$$h_u = h_t - h_m - h_l \quad (16)$$

[Figure 5](#) shows a transverse section view of a tank indicating where measurements are required and the values used in calculating chamfer.



Key

1	vertical lines	4	centreline
2	tank top	5	horizontal reference line
3	upper chamfer	6	tank bottom
7	lower chamfer	8	side wall
d_1	height between the horizontal reference line and bottom plate along the vertical lines		
d_2	height between the horizontal reference line and top of the lower chamfer at the corners of a tank		
h_1	lower chamfer height		
h_m	side wall height		
h_t	total height		
h_u	height of upper chamfer		
h_x	arbitrary height in the lower chamfer portion		
h_y	arbitrary height in the upper chamfer portion		

Figure 5 — Transverse section view

7.5 Measurement of bottom undulation and gauge reference height

7.5.1 Set reference lines by an optical level with some clearance from the tank bottom. Figure 6 shows an expanded transverse section of the tank bottom to illustrate the measurements used in the assessment of bottom undulation.

7.5.2 Measure the offsets between the bottom plate and the reference plane along all the vertical lines set on the fore and aft end walls. The average of the measurements is denoted as RB .

7.5.3 Likewise, take measurements of the depths at all intersections of the longitudinal lines with the section lines on the bottom plate. The average of these measurements as well as of the measurements used in obtaining RB is denoted as RA .

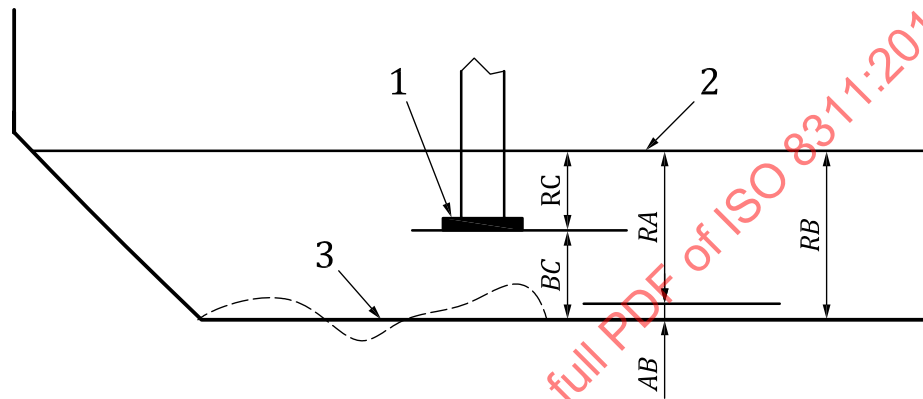
7.5.4 Calculate the numerical difference AB between the average reference offset RB and the average depth measurement RA using Formula (17):

$$AB = |RA - RB| \quad (17)$$

The increase or decrease in volume due to bottom undulation is obtained by multiplying the difference AB by the area of the tank bottom plate.

7.5.5 Measure the depth RC between the reference plane and gauge reference point (see [Figure 6](#)). The clearance BC of the gauge reference point in relation to the tank bottom is then calculated using Formula (18):

$$BC = RB - RC \quad (18)$$



Key

- 1 gauge reference point
- 2 reference plane
- 3 zero level

Figure 6 — Transverse section view of tank bottom

7.6 Correction for temperature

The atmospheric temperature in the tank shall be measured at intervals of 2 h or less and, when this differs from the calibration temperature of the measuring tape, the measurements shall be corrected for the expansion or contraction of the tape. In the case of independent prismatic tanks, the measurements

shall be corrected for the contraction or expansion of the measuring tape and tank material using Formula (19):

$$C = D \times (\alpha_s - \alpha_t) \times (T - t) \quad (19)$$

where

- C is the total correction to the measured length for the effect of temperature;
- D is the measured length;
- α_s is the mean coefficient of linear expansion of the measuring tape;
- α_t is the mean coefficient of linear expansion of the metal from which the tank is constructed;
- T is the calibration temperature of the measuring tape;
- t is the average temperature of the tank during measurement.

If C is less than 0,5 mm, the correction may be ignored.

8 Calibration by electro-optical distance-ranging (EODR) method

8.1 General

In EODR method, average distances between opposite walls of a tank shall be calculated from the coordinates of the measuring points on these walls.

Note that as alternatives to the formulae in 8.3.2, 8.3.3 and 8.3.4, other methods of equal or better uncertainties, e.g. least square method, may be used to calculate tank dimensions.

8.2 Setting up of EODR instrument

The EODR instrument shall be set up with the following steps.

- a) The number and locations of the instrument stations shall be determined in order not to exceed incidence-angle limitations of equipment. If more than one station is necessary, survey traverse techniques should be used to move from one station to the other.
- b) The instrument shall be set up with care, particularly in the horizontal and vertical axes and according to the procedure and instructions given by the manufacturer.
- c) The instrument shall be set up so as to be stable and free from external vibrations. If necessary, the tank shell, in the vicinity of the instrument, shall be made firm and steady by placing heavy weights in the area. The legs of the tripod on which the instrument is mounted may be steadied using suitable devices to prevent slippage on the tank bottom.
- d) The sighting lines from the instrument to the tank shell shall not be obstructed.
- e) At least the minimum settling time recommended by the manufacturer should be allowed before the instrument is used.
- f) If the distance-measurement part is separate, parallax adjustment should be made at the start. The distance optical beam and laser beams should be adjusted after temperature equilibrium, to ensure zero parallax, and then locked in position.
- g) Select two reference target points. The reference target points should be approximately 100 gon apart and preferably on the same horizontal plane as this instrument.

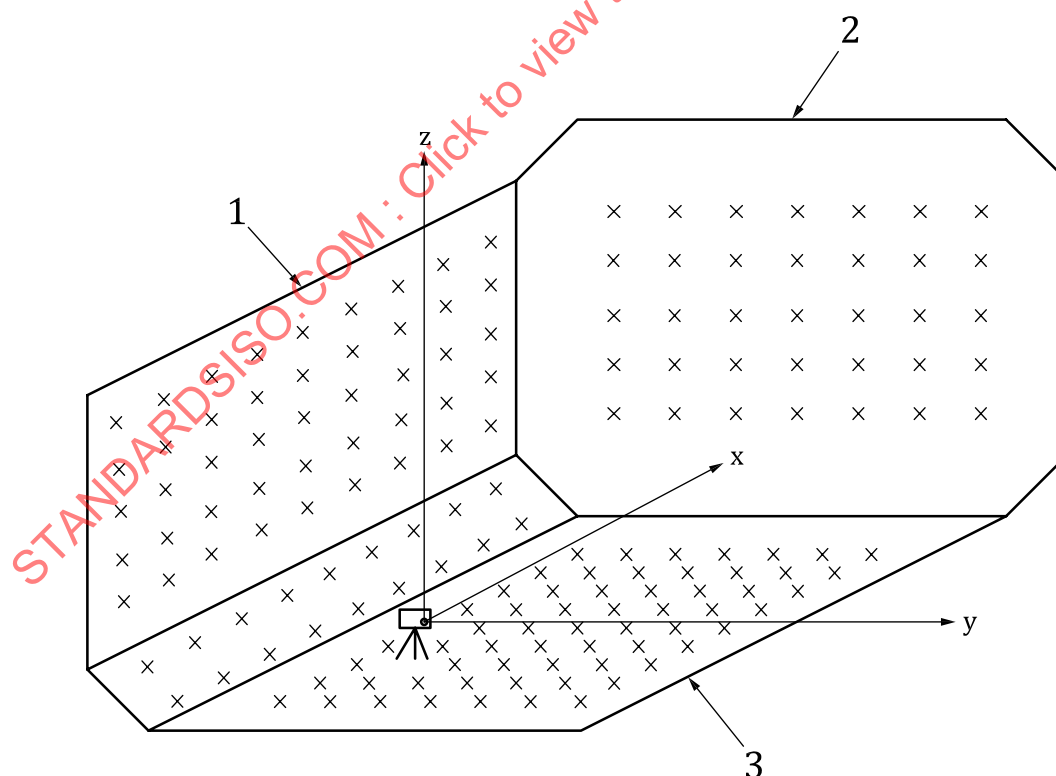
- h) Measure and record the horizontal angle, the vertical angle and the slope distance to each reference target point. Two successive readings, at each point, shall be taken and they shall agree within the following tolerance. Compute and record the average angles and distance to each point.
- 1) the **slope distance** to each reference target point at the beginning and end of the calibration shall be within $\pm 2\text{mm}$.
 - 2) the **horizontal and vertical angles** to each reference target point at the beginning and end of the calibration shall be within $\pm 0,01$ gon.

8.3 Calibration procedure

8.3.1 General

The tanks shall be calibrated with the following steps.

- a) Measure the horizontal and vertical angles and the slope distance to each measuring point on a surface and express the position of the targets as a point in the Cartesian coordinate (see [Figure 7](#)).
- b) After all measurements from one measurement station are completed, repeat the measurements to the reference target points.
- c) If the repeated horizontal and vertical angles and slope distances to each reference target point do not agree with measurements taken in [8.2 h\)](#), within the tolerances given in that paragraph, determine the reasons for such disagreement, eliminate the cause and repeat the calibration procedure.
- d) Carry out all measurements without interruption.



Key

- 1 side plate
- 2 end plate
- 3 bottom plate

Figure 7 — Measuring points

8.3.2 Determination of length

The positions of the fore end wall and aft end wall on the x-axis are determined by averaging the x-coordinate of the measuring points on the respective walls. The length of the tank (L) is given by adding the average of $x_{\text{(aft)}}$ and the average of $x_{\text{(fore)}}$ i.e.:

$$L = \left| \frac{\sum x_{n(\text{fore})}}{n_{(\text{fore})}} \right| + \left| \frac{\sum x_{n(\text{aft})}}{n_{(\text{aft})}} \right| \quad (20)$$

NOTE $x_{n(\text{fore})}$ and $x_{n(\text{aft})}$ are absolute values of the EODR measurements.

8.3.3 Determination of width

The position of the port and starboard side walls on the y-axis are determined by the averaging the y-coordinate of the measuring points on the respective walls. The width intermediated horizontal plane (w) is given by adding the average of $y_{\text{(port)}}$ and the average of $y_{\text{(starboard)}}$ i.e.:

$$w = \left| \frac{\sum y_{n(\text{starboard})}}{n_{(\text{starboard})}} \right| + \left| \frac{\sum y_{n(\text{port})}}{n_{(\text{port})}} \right| \quad (21)$$

NOTE $y_{n(\text{starboard})}$ and $y_{n(\text{port})}$ are absolute values of the EODR measurements.

In case the horizontal plane of tank is trapezoidal, side wall is assumed as the linear regression line of the x- and y-coordinates of each measuring point on the side wall i.e.:

$$x = ay + b$$

$$a = \frac{\sum_{i=1}^n (y_i - \bar{Y})(x_i - \bar{X})}{\sum_{i=1}^n (y_i - \bar{Y})^2}$$

$$b = \bar{X} - a\bar{Y} \quad (22)$$

8.3.4 Determination of height

The position of the bottom and top plates on the z-axis are determined by averaging the z-coordinate of the measuring points on the respective plates. The total height of tank (h_t) is given by adding the average of $z_{\text{(bottom)}}$ from the average of $z_{\text{(top)}}$ i.e.:

$$h_t = \frac{\sum z_{n(\text{top})}}{n_{(\text{top})}} + \frac{\sum z_{n(\text{bottom})}}{n_{(\text{bottom})}} \quad (23)$$

NOTE $z_{n(\text{top})}$ and $z_{n(\text{bottom})}$ are absolute values of the EODR measurements.

Chamfer is assumed as the linear regression line (Z) of the y- and z-coordinates of each measuring points on the chamfer part.

The height of each side of the octagon is given by a set of coordinates thereby $w_{f(\text{top})}$, $w_{a(\text{bottom})}$, $h_{u(\text{upper})}$, $h_{m(\text{middle})}$ and $h_{l(\text{lower})}$ are determined. The heights of each pair of chamfers may be averaged.

9 Additional measurements

9.1 Location of level gauge

The location of the level gauge shall be indicated by the distances from the nearby wall and the bottom of the lower chamfer and recorded for inclusion in the calculation of trim and list corrections.

9.2 Deadwood

9.2.1 The volume of deadwood such as pipe columns, ladders, submerged pumps and any other structures in the tank shall be calculated from their dimensions. However, when the dimensions are not readily obtainable due to the complexity of the shape, the volume may be calculated from the mass of the item and the density of its material of construction, provided that the uncertainty of the calculated volume is negligible with respect to the overall measurement accuracy. For each item of deadwood, the volume shall be calculated as function of height above the gauge reference point.

9.2.2 The volume of internal piping containing cargo fluid shall be calculated as the difference between the external and internal volumes of the piping, i.e. the volume of the metal.

9.2.3 The volume of membrane tongues or corrugations shall be calculated from the drawings.

9.2.4 For tank volume calibrations, the height of the deadwood above the gauge reference point and volume of the deadwood at that level shall be measured.

10 Calculation

10.1 General

The tank capacity table shall be compiled in accordance with the principles set out in [10.2](#) and [10.3](#) and taking account of chamfer portions (see [10.4](#)).

The tank volume (see [Figure 8](#)) is given by Formula (24):

$$V = \left[\left(\frac{w_u + w_m}{2} \times h_u \right) + w_m \times h_m + \left(\frac{w_m + w_l}{2} \times h_l \right) \right] \times L \quad (24)$$

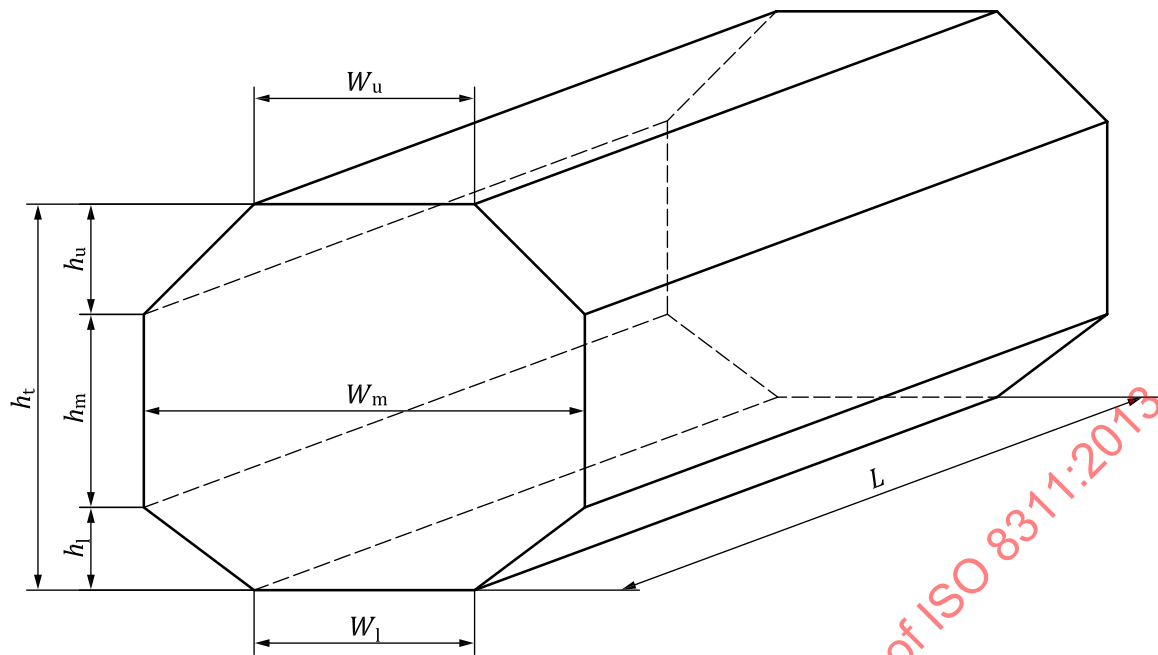


Figure 8 — Elements of tank volume calculation

Corrections shall be made in accordance with 10.5 to 10.8.

10.2 Calculation of tank volume

The tank table shall be compiled by means of multiple horizontal areas calculated at each centimetre of height starting from the tank bottom as the zero level. Each horizontal area shall be obtained from the average length L and the average width w , taking into account the deadwood affecting the area.

10.3 Effect of bottom undulation

Any increase or decrease in volume arising from tank bottom undulation shall be adjusted in relation to the gauge reference point (see 7.5.5).

10.4 Area of chamfer portion

10.4.1 The area at an arbitrary height in the lower chamfer portion of the tank shall be calculated as a function of h_x (see Figure 5) employing h_l (see 7.4.3 and 8.3.4) as well as horizontal areas at the top and the bottom of the chamfer.

$$A_x = A_l + (A_m - A_l) \times \frac{h_x}{h_l} \quad (25)$$

where

- A_x is the area at an arbitrary height in the lower chamfer portion;
- A_m is the horizontal area at the top of the lower chamfer;
- A_l is the horizontal area at the bottom of the lower chamfer;
- h_x is the arbitrary height in the lower chamfer;
- h_l is the height of lower chamfer.

10.4.2 For the middle part of the tank, one and the same area may be used for calculation.

10.4.3 The area at an arbitrary height in the upper chamfer portion of the tank shall be calculated as a function of h_y (see [Figure 5](#)) employing h_u (see [7.4.4](#) and [8.3.4](#)) as well as horizontal areas at the top and the bottom of the chamfer.

$$A_y = A_m - (A_m - A_u) \times \frac{h_y}{h_u} \quad (26)$$

where

- A_y is the area at an arbitrary height in the upper chamfer portion;
- A_m is the horizontal area at the bottom of the upper chamfer;
- A_u is the horizontal area at the top of the upper chamfer;
- h_y is the arbitrary height in the upper chamfer;
- h_u is the height of upper chamfer.

10.5 Trim corrections

Trim corrections shall be given as an addition to or subtraction from the apparent liquid level measured by the tank gauge. Trim corrections are calculated by comparison of the liquid levels given by the same volume of liquid in the tank with the ship upright and on even keel, and with the ship upright and in the condition of trim under consideration.

10.6 List corrections

List corrections shall be given as an addition to or subtraction from the apparent liquid level as measured by the tank gauge. List corrections are calculated by comparison of the liquid levels given by the same volume of liquid in the tank with the ship on even keel and upright, and with the ship on even keel and in the list condition under consideration.

10.7 Combined trim and list corrections

The trim and list corrections compiled in accordance with [10.5](#) and [10.6](#) may be combined in one table.

10.8 Correction for tank shell expansion or contraction

The correction for tank shell expansion or contraction is unnecessary for membrane tanks where the construction or construction materials are such that thermal contraction effects on volume are insignificant.

In case of independent prismatic tank, correction of tank volume for cryogenic loaded condition shall be made by means of the coefficient of expansion of the material of the tank shell, using Formula (27):

$$F_v = 1 - 3\alpha_t(t_1 - t_2) \quad (27)$$

where

- F_v is the correction factor for tank shell expansion or contraction;
- α_t is the mean coefficient of linear expansion of the metal from which the tank is constructed;
- t_1 is the tank-calibration reference temperature for the tank table;
- t_2 is the actual temperature of the liquid or vapour.

11 Report and tables

The following report and tables shall be bound into a book and kept on board the ship. In addition to the hard copies, the tables may be electronically stored in the ship's custody transfer measurement system.

- a) The calibration report includes:
 - 1) name of calibrator;
 - 2) place of calibration;
 - 3) date of calibration;
 - 4) tank dimensions;
 - 5) measurement method;
 - 6) tank-calibration reference temperature;
 - 7) total tank capacity;
 - 8) uncertainty of measurement;
 - 9) directions for use of tables.
- b) Tank capacity is tabulated against the gauge readings at suitable intervals. A second column may give the differences between the readings. An example of a tank capacity table is given in [Annex B](#).
- c) Trim correction tables to be applied to gauge readings are tabulated at suitable intervals of gauge reading for various conditions of trim both by head and by stern. An example of a trim correction table is given in [Annex C](#).
- d) List correction tables to be applied to gauge readings are tabulated at suitable intervals of gauge reading for conditions of list at 0,5° intervals. An example of a list correction table is given in [Annex D](#).
- e) In the case of independent prismatic tanks, correction table for expansion/contraction of tank shell is to be applied for the difference between the tank-calibration reference temperature of the tank capacity table and the actual temperature of the liquid and vapour.
- f) Thermal correction tables for ATG, which provide corrections for any effect of changes in temperature, pressure or cargo properties of the respective cargo components (see ISO 18132-1 and ISO 18132-3).

12 Recalibration

Tanks should be recalibrated as required by national regulations or if the calibration becomes suspect for any reason, e.g. deformation or modification. Change of ATGs may require reproduction of relevant correction tables.

STANDARDSISO.COM : Click to view the full PDF of ISO 8311:2013

Annex A (informative)

Uncertainty associated with tank calibration

A.1 General

This annex describes calculations of uncertainty associated with tank calibration by the manual method (see [Clause 7](#)).

A.2 Symbols

a_1	Offset between string and aft end wall on port side wall, by rule	m
a_i	Offset between string and aft end wall, by rule	m
a_n	Offset between string and aft end wall on starboard side wall, by rule	m
A_{rule}	Uncertainty of rule	m
A_{tape}	Uncertainty of steel tape	m
A_{temp}	Uncertainty of thermometer	°C
b_1	Offset between string and fore end wall on port side wall, by rule	m
b_i	Offset between string and fore end wall, by rule	m
b_n	Offset between string and fore end wall on starboard side wall, by rule	m
c_i	Sensitivity coefficient	–
C_{ten}	Tension coefficient of steel tape	/N
D	Distance measured by steel tape	m
d	Distance measured by rule	m
D_{dir}	Distance obtained by direct method	m
d_i	Measurand by rule	m
D_i	Measurand by steel tape	m
D_{ref}	Distance obtained by reference line method	m
E_{ten}	Ratio of tension difference against T_{std}	–
h_i	Measurand of height	m
h_l	Height of lower chamfer	m
h_m	Height of side wall	m
h_t	Total tank height	m
h_u	Height of upper chamfer	m

k	Coverage factor	–
L	Tank length	m
L_i	Measurand of length	m
L_l	Averaged tank length on bottom plate	m
L_m	Averaged tank length of intermediate part	m
L_p	Tank length on port side wall measured by steel tape	m
L_{ref}	Tank length obtained by reference line method	m
L_s	Tank length on starboard side wall by steel tape	m
L_u	Averaged tank length on top plate	m
n	Number of measurement	–
P	Horizontal plane	–
R_{rule}	Resolution of rule	m
R_{tape}	Resolution of steel tape	m
T_{std}	Standard tension of steel tape	N
$u(D_{cal})$	Standard uncertainty of steel tape due to calibration	m
$u(d_{cal})$	Standard uncertainty of rule due to calibration	m
$u(D_{dev})$	Standard uncertainty of steel tape due to measurement deviation	m
$u(D_i)$	Standard uncertainty of steel tape due to a component i .	m
$u(d_i)$	Standard uncertainty of rule due to a component i .	m
$u(d_{dev})$	Standard uncertainty of rule due to measurement deviation	m
$u(D_{res})$	Standard uncertainty of steel tape due to resolution	m
$u(d_{res})$	Standard uncertainty of rule due to resolution	m
$u(D_{ten})$	Standard uncertainty of steel tape due to tension	m
$u(D_{th})$	Standard uncertainty of rule due to temperature	m
$u(d_{th})$	Standard uncertainty of steel tape due to temperature	m
$u(D_{va})$	Standard uncertainty of steel tape due to variation	m
$u(d_{va})$	Standard uncertainty of rule due to variation	m
$u(x_i)$	Standard uncertainty of a component x_i	–
$u_c(D)$	Combined uncertainty of steel tape	–
$u_c(d)$	Combined uncertainty of rule	–
$u_c(y)$	Combined uncertainty of y	–
$u_r(x)$	Standard uncertainty of x sorted with random component	–

$u_s(x)$	Standard uncertainty of x sorted with systematic component	–
V	Tank volume	m^3
V_D	Estimated variation of steel tape measurement	m
V_d	Estimated variation of rule measurement	m
w_i	Average width of a horizontal plane P_j	m
w_l	Tank width at lower part	m
w_m	Tank width at middle part	m
w_u	Tank width at upper part	m
δ	Deviation from the reference point	m
α	Temperature coefficient of steel tape	$/^{\circ}C$
θ	Deviation in angle	$^{\circ}$

A.3 Determination of combined standard uncertainty

The combined standard uncertainty, $u_c(y)$, is given by Formula (A.1) where all input quantities are independent.

$$u_c^2(y) = \sum_{i=1}^n \left[\left(\frac{\partial y}{\partial x_i} \right) \times u(x_i) \right]^2$$

(A.1)

where $y = f(x_1, x_2, x_3, ..., x_n)$

A.4 Mathematical model

See [Figure A.1](#).

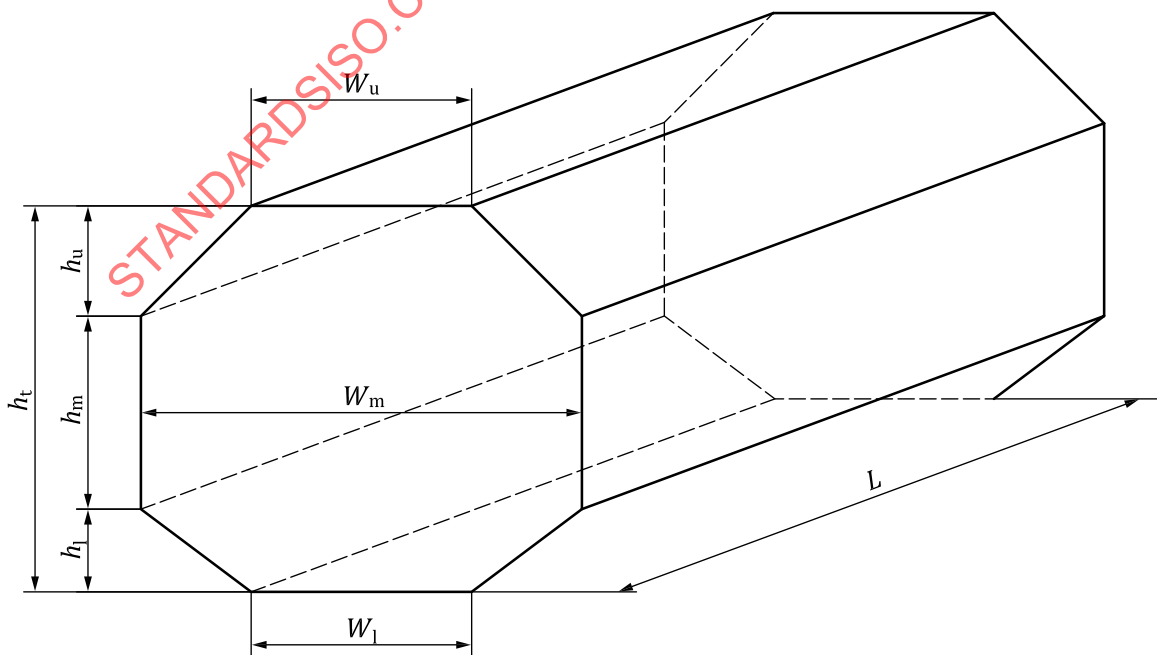


Figure A.1 — Typical membrane tank overview

From 10.1, the tank volume is given by Formula (A.2):

$$V = \left[\left(\frac{w_u + w_m}{2} \times h_u \right) + w_m \times h_m + \left(\frac{w_m + w_l}{2} \times h_l \right) \right] \times L \quad (\text{A.2})$$

A.5 Contributory variance

The contributory variance is given by Formula (A.3):

$$u_c^2(V) = c_L^2 u^2(L) + c_{w_u}^2 u^2(w_u) + c_{w_m}^2 u^2(w_m) + c_{w_l}^2 u^2(w_l) + c_{h_u}^2 u^2(h_u) + c_{h_m}^2 u^2(h_m) + c_{h_l}^2 u^2(h_l) \quad (\text{A.3})$$

h_u is given indirectly by the following formula:

$$h_u = h_t - (h_l + h_m)$$

Therefore, it can be rewritten as:

$$\begin{aligned} u_c^2(V) &= c_L^2 u^2(L) + c_{w_u}^2 u^2(w_u) + c_{w_m}^2 u^2(w_m) + c_{w_l}^2 u^2(w_l) + c_{h_u}^2 \left[u^2(h_t) + u^2(h_l) + u^2(h_m) \right] \\ &+ c_{h_m}^2 u^2(h_m) + c_{h_l}^2 u^2(h_l) \end{aligned} \quad (\text{A.4})$$

A.6 Sensitivity coefficients

The sensitivity coefficients in Formula (A.4) can be obtained by Formula (A.5) to (A.11):

$$c_L = \frac{\partial V}{\partial L} = \frac{(w_u + w_m)h_u + 2w_m h_m + (w_m + w_l)h_l}{2} \quad (\text{A.5})$$

$$c_{h_u} = \frac{\partial V}{\partial h_u} = \frac{L(w_u + w_m)}{2} \quad (\text{A.6})$$

$$c_{h_m} = \frac{\partial V}{\partial h_m} = Lw_m \quad (\text{A.7})$$

$$c_{h_l} = \frac{\partial V}{\partial h_l} = \frac{L(w_m + w_l)}{2} \quad (\text{A.8})$$

$$c_{w_u} = \frac{\partial V}{\partial w_u} = \frac{Lh_u}{2} \quad (\text{A.9})$$

$$c_{w_m} = \frac{\partial V}{\partial w_m} = \frac{L(h_u + 2h_m + h_l)}{2} = \frac{L(h_t + h_m)}{2} \quad (\text{A.10})$$

$$c_{w_l} = \frac{\partial V}{\partial w_l} = \frac{Lh_l}{2} \quad (\text{A.11})$$

A.7 Cause of uncertainties

A.7.1 General

The causes of uncertainty associated with tank calibration are attributed to measurement method, source and effect, and each cause is classified into systematic and random effects.

A.7.2 Classification by method

A.7.2.1 General

The manual calibration of membrane tanks described in this standard includes direct method and reference line method.

A.7.2.2 Direct method

When measurements are taken directly by steel tape, the combined uncertainty, $u_c(D)$, is the sum of the uncertainty inherent in the steel tape.

$$u_c^2(D) = \sum_{i=1}^n u^2(D_i) \quad (\text{A.12})$$

A.7.2.3 Reference line method

The combined uncertainty associated with the reference line method applied to the measurement of the averaged tank length of an intermediate part is derived from Formula (A.13):

$$L_{m,p} = \frac{L_P + L_S - (a_1 + a_n + b_1 + b_n)}{2} + \frac{\sum_{i=1}^n (a_i + b_i)}{n}$$

$$L_{m,p} = \frac{L_P + L_S - (a_1 + a_n + b_1 + b_n)}{2} + \bar{a}_i + \bar{b}_i \quad (\text{A.13})$$

The combined uncertainty, $u_c(L_m)$, is given as:

$$u_c^2(L_m) = c_{L_P}^2 u^2(L_P) + c_{L_S}^2 u^2(L_S) + c_{a_1}^2 u^2(a_1) + c_{a_n}^2 u^2(a_n) + c_{b_1}^2 u^2(b_1) + c_{b_n}^2 u^2(b_n) + c_{\bar{a}_i}^2 u^2(\bar{a}_i) + c_{\bar{b}_i}^2 u^2(\bar{b}_i) \quad (\text{A.14})$$

And the sensitivity coefficients are as shown as follows:

$$c_{L_P} = c_{L_S} = c_{a_1} = c_{a_n} = c_{b_1} = c_{b_n} = \frac{\partial L}{\partial L_P} = \frac{1}{2} \quad (\text{A.15})$$

$$c_{\bar{a}_i} = c_{\bar{b}_i} = \frac{\partial L}{\partial \bar{a}_i} = 1 \quad (\text{A.16})$$

In addition,

$$u(L_P) = u(L_S) \quad (\text{A.17})$$

$$u(a_1) = u(a_n) = u(b_1) = u(b_n) \quad (\text{A.18})$$

$$u(\bar{a}_i) = u(\bar{b}_i) \quad (\text{A.19})$$

Thus, the combined uncertainty, $u_c(L_{m,p})$, for length is given in Formula (A.20):

$$u_c^2(L_{m,p}) = \frac{u^2(L_p)}{2} + u^2(a_1) + 2u^2(\bar{a}_i) \quad (\text{A.20})$$

Similarly, the combined uncertainty, $u_c(w_{m,p})$, for width is:

$$u_c^2(w_{m,p}) = \frac{u^2(w_F)}{2} + u^2(c_1) + 2u^2(\bar{c}_i) \quad (\text{A.21})$$

A.7.3 Classification by source

A.7.3.1 General

Steel tapes and rule are used for the manual calibration of membrane tanks.

A.7.3.2 Measured by steel tape

See Formula (A.12).

A.7.3.3 Measured by rule

The combined uncertainty, $u_c(d)$, of the rule measurement is given as Formula (A.22):

$$u_c^2(d) = \sum_{i=1}^n u^2(d_i) \quad (\text{A.22})$$

A.7.4 Classification by effect

The source of uncertainty comprised of random and systematic components. The random effect refers to the effect caused by a random component, which can be reduced by adopting an average of the measurement values. Systematic effects cannot be reduced by adopting an average of the measurement values.

In the manual measurement of membrane tanks, the combined uncertainty, $u_c(h_i)$, associated with the height measurement is described by Formula (23):

$$u_c^2(h_i) = \frac{u_r^2(h_i)}{n} + u_s^2(h_i) \quad (\text{A.23})$$

For length and width measurements, the random effects are reduced in accordance with the number of horizontal planes.

$$u_c^2(L_i) = \frac{u_r^2(L_i)}{n \times p} + u_s^2(L_i) \quad (\text{A.24})$$

$$u_c^2(w_i) = \frac{u_r^2(w_i)}{n \times p} + u_s^2(w_i) \quad (\text{A.25})$$

NOTE Refer to [Table A.1](#), [A.7.7](#) and [A.7.8](#).

A.7.5 Integration of uncertainties

A.7.5.1 General

The uncertainties classified in [A.7.2](#) and [A.7.3](#) are combined according to the measurement methods.

A.7.5.2 Combined uncertainty for direct method

For direct method, Formulae (A.12) and (A.23) are integrated as follows:

$$u_c^2(D_{\text{dir}}) = \sum_{i=1}^n \left(\frac{u_r^2(D_i)}{n} + u_s^2(D_i) \right) \quad (\text{A.26})$$

A.7.5.3 Combined uncertainty for reference line method

For the reference line method, Formulae (A.12), (A.20), (A.21), (A.22), (A.24) and (A.25) are integrated as follows:

$$u_c^2(D_{\text{ref}}) = \frac{1}{2} \sum_{i=1}^n \left(\frac{u_r^2(D_i)}{n \times p} + u_s^2(D_i) \right) + \sum_{j=1}^j \left(\frac{u_r^2(d_j)}{n \times p} + u_s^2(d_j) \right) + 2 \sum_{k=1}^k \left(\frac{u_r^2(d_k)}{n \times p} + u_s^2(d_k) \right) \quad (\text{A.27})$$

A.7.6 Grouping of uncertainties

Components of uncertainty are grouped into random and systematic.

Table A.1 — Uncertainty grouping

Component of uncertainty		Reason
Random components		
	due to tension (only for steel tape)	Measurement value is varied by variance of giving standard tension to the tape. The giving tension varies every measurement around the standard tension.
	due to the resolution of tape or rule	Measurement value is varied by the resolution of the tape or rule. It varies at the half of the resolution.
	due to variation	This is estimation of the variance of the population.
	due to tank wall undulation	This is estimation of the variance of the population.
Systematic components		
	due to calibration or characteristic	Measurement value is always biased if the same tape or rule is used for series of measurement.
	due to temperature	Measurement value is always biased if the same thermometer is used for temperature correction.
	due to measurement deviation	Measurement value is always biased around the centre of ideal point.

A.7.7 Uncertainties associated with steel tape

A.7.7.1 Standard uncertainty of steel tape due to tension

In case that the tension applied to the tape deviates from the standard tension, the uncertainty is given by Formula (A.28).

$$u(D_{\text{ten}}) = D \times \frac{C_{\text{ten}} \times T_{\text{std}} \times E_{\text{ten}}}{\sqrt{3}} \quad (\text{A.28})$$

A.7.7.2 Standard uncertainty of steel tape due to resolution

The probability distribution can be considered as a rectangular distribution. The uncertainty is given by Formula (A.29).

$$u(D_{\text{res}}) = \frac{R_{\text{tape}}}{2 \times \sqrt{3}} \quad (\text{A.29})$$

A.7.7.3 Standard uncertainty of steel tape due to variation

Variation can be found if multiple measurements are made. This variation can either be statistically analysed in accordance with the series of observations or be estimated from the repeatability described in 4.5. In the latter case, the uncertainty is given by Formula (A.30).

$$u(D_{\text{va}}) = \frac{V_D}{2 \times \sqrt{3}} \quad (\text{A.30})$$

A.7.7.4 Standard uncertainty due to tank wall undulation

Undulation of the tank walls can be the source of uncertainty. It can either be statistically analysed or be estimated from the experience. In the latter case, the uncertainty is given by the Formula (A.31).

$$u(D_{\text{ud}}) = \frac{V_{\text{uD}}}{2 \times \sqrt{3}} \quad (\text{A.31})$$

A.7.7.5 Standard uncertainty of steel tape due to calibration

In the case that an expanded calibration uncertainty is stated on the certificate, the standard uncertainty is calculated by dividing it by the coverage factor ($k = 2$):

$$u(D_{\text{cal}}) = \frac{A_{\text{tape}}}{2} \quad (\text{A.32})$$

In the case that an expanded calibration uncertainty is not found on the certificate, but the steel tape is manufactured according to an industrial standard, the probability distribution can be considered as a rectangular distribution. In such case, the uncertainty is given by Formula (A.33).

$$u(D_{\text{cal}}) = D \times \frac{A_{\text{tape}}}{\sqrt{3}} \quad (\text{A.33})$$

A.7.7.6 Standard uncertainty of steel tape due to temperature

The uncertainty of thermometer is stated on the calibration certificate or is declared by the manufacturer of the thermometer. In either case, the probability distribution can be considered as a rectangular distribution and the uncertainty is given by Formula (A.34):

$$u(D_{\text{th}}) = D \times \frac{\alpha \times A_{\text{temp}}}{\sqrt{3}} \quad (\text{A.34})$$

A.7.7.7 Standard uncertainty of steel tape due to measurement deviation

If there is some deviation in angle from the point to the other, the probability distribution can be considered as a triangle distribution. The uncertainty is given by Formula (A.35):

$$u(D_{\text{dev}}) = \frac{D - D \times \cos \theta}{2 \times \sqrt{6}} \quad (\text{A.35})$$

A.7.8 Uncertainties associated with rule

A.7.8.1 Standard uncertainty of rule due to resolution

The probability distribution can be considered as a rectangular distribution. The uncertainty is given by Formula (A.36):

$$u(d_{\text{res}}) = \frac{R_{\text{rule}}}{2 \times \sqrt{3}} \quad (\text{A.36})$$

A.7.8.2 Standard uncertainty of rule due to variation

Similar to [A.7.7.3](#):

$$u(d_{\text{va}}) = \frac{V_{\text{d}}}{2 \times \sqrt{3}} \quad (\text{A.37})$$

A.7.8.3 Standard uncertainty due to tank wall undulation

Similar to [A.7.7.4](#):

$$u(d_{\text{ud}}) = \frac{V_{\text{ud}}}{2 \times \sqrt{3}} \quad (\text{A.38})$$

A.7.8.4 Standard uncertainty of rule due to calibration

Similar to [A.7.7.5](#):

$$u(d_{\text{cal}}) = d \times \frac{A_{\text{rule}}}{\sqrt{3}} \quad (\text{A.39})$$

A.7.8.5 Standard uncertainty of rule due to temperature

Similar to [A.7.7.6](#):

$$u(d_{\text{th}}) = d \times \frac{\alpha \times A_{\text{temp}}}{\sqrt{3}} \quad (\text{A.40})$$

A.7.8.6 Standard uncertainty of rule due to measurement deviation

If there is some deviation from the point, the probability distribution can be considered as a triangle distribution. The uncertainty is given by Formula (A.41):

$$u(d_{\text{dev}}) = \frac{d - \sqrt{d^2 + \delta^2}}{\sqrt{6}} \quad (\text{A.41})$$

A.8 Numerical example

The following tables ([Tables A.2](#), [A.3](#), [A.4](#), [A.5](#) and [A.6](#)) show uncertainty calculations of tank volume in relation to the manual measurement. In this example, a non-trapezoidal cargo tank on a 145 000 m³ type LNG carrier is considered.

Table A.2 — Numerical example

Measurement distance by steel tape D , m		L	w	h
	upper	44,904	22,525	27,562
	middle		39,106	15,053
	lower		30,689	4,222
Accuracy of steel tape A_{tape} , m	The accuracy of strapping tape is prescribed in ISO 7507-1:2003, Annex A. $A_{\text{tape}} = \frac{1,5}{30\,000} = 0,000\,05$			
Temperature coefficient α , /°C	14×10^{-6}			
Accuracy of thermometer A_{temp} , °C	It is described in 5.7 as $\pm 0,5$ °C.			
Standard tension of steel tape T_{std} , N	50			
Tension coefficient C_{ten} , /N	$3,01 \times 10^{-6}$			
Tension difference E_{ten} , %	10			
Minimum resolution of steel tape R_{tape} , m	0,001			
Deviation in angle θ , °	1,0			
Estimated limited value of variation of steel tape V_D , m	0,002 for measurement up to 25 m 0,003 for measurement over than 25 m			
Estimated limited value of variation due to tank wall undulation V_{uD} , m	0,030			
Number of measurement at same point n_D	2			
Measurement distance by rule d , m	0,150			
Accuracy of rule A_{rule} , m	It is prescribed in JIS B7516. $A_{\text{rule}} = \frac{0,10 + 0,05 \times (d / 0,5)}{1\,000} = 0,000\,15$ Calculation result of the fraction less than 1 of $d/0,5$ shall round up to an integer.			
Minimum resolution of rule R_{rule} , m	0,001			
Deviation from measurement point δ , m	0,005			
Estimated limited value of variation of rule V_d , m	0,000 5			
Estimated limited value of variation due to tank wall undulation V_{ud} , m	0,030			
Number of measurement at same point n_d	2			

Table A.3 — Influence to volume due to uncertainty of length measurement

	Direct method $L = 44,904 \text{ m}$		Reference line method $d = 0,150 \text{ m}$		
	Upper part	Lower part	Middle part		
			L_p	a_1	a_i
n_D, n_d	2		2		
n	5	9	1	1	18
p	1	1	4		

Table A.3 (continued)

		Direct method $L = 44,904 \text{ m}$		Reference line method $d = 0,150 \text{ m}$		
		Upper part	Lower part	Middle part		
				L_p	a_1	a_i
$u_r(L_i)$	$u(D_{\text{ten}})$, m	0,000 39	0,000 39	0,000 39	-	-
	$u(D_{\text{res}})$ or $u(d_{\text{res}})$, m	0,000 29	0,000 29	0,000 29	0,000 29	0,000 29
	$u(D_{\text{va}})$ or $u(d_{\text{va}})$, m	0,001 73	0,001 73	0,001 73	0,000 29	0,000 29
	$u(D_{\text{ud}})$ or $u(d_{\text{ud}})$, m	0,008 66	0,008 66	0,008 66	0,001 44	0,001 44
$u_s(L_i)$	$u(D_{\text{cal}})$ or $u(d_{\text{cal}})$, m	0,001 30	0,001 30	0,001 30	0,000 07	0,000 07
	$u(D_{\text{th}})$ or $u(d_{\text{th}})$, m	0,000 18	0,000 18	0,000 18	0,000 00	0,000 00
	$u(D_{\text{dev}})$ or $u(d_{\text{dev}})$, m	0,001 40	0,001 40	0,001 40	0,000 02	0,000 02
$\Sigma u_r^2(L_i)$, m^2		$78,2 \times 10^{-6}$	$78,2 \times 10^{-6}$	$78,2 \times 10^{-6}$	$2,25 \times 10^{-6}$	$2,25 \times 10^{-6}$
$\Sigma u_s^2(L_i)$, m^2		$3,66 \times 10^{-6}$	$3,66 \times 10^{-6}$	$3,66 \times 10^{-6}$	$0,007 9 \times 10^{-6}$	$0,007 9 \times 10^{-6}$
Coefficient		1	1	0,5	1	2
Coeff. $\times u_r^2(L)/(n \times p)$, m^2		$7,82 \times 10^{-6}$	$4,35 \times 10^{-6}$	$4,89 \times 10^{-6}$	$0,281 \times 10^{-6}$	$0,031 3 \times 10^{-6}$
Coeff. $\times u_s^2(L)$, m^2		$3,66 \times 10^{-6}$	$3,66 \times 10^{-6}$	$1,83 \times 10^{-6}$	$0,007 8 \times 10^{-6}$	$0,015 6 \times 10^{-6}$
$u^2(L)$, m^2		$11,5 \times 10^{-6}$	$8,01 \times 10^{-6}$	$6,72 \times 10^{-6}$	$0,289 \times 10^{-6}$	$0,046 8 \times 10^{-6}$
$\Sigma u^2(L)$, m^2		$26,6 \times 10^{-6}$				
c_L^2 , m^4		9912				
$c_L^2 u^2(L)$, m^6		26,1				

Table A.4 — Influence to volume due to uncertainty of width measurement

		Direct method	Reference line method 0,150 m					
		$w_l = 30,689 \text{ m}$	$w_u = 22,525 \text{ m}$			$w_m = 39,106 \text{ m}$		
			w_f	c_1	c_i	w_f	c_1	c_i
n_D, n_d		2	2			2		
n		10	1	1	20	1	1	20
p		1	1			4		
$u_r(w)$	$u(D_{\text{ten}})$, m	0,000 27	0,000 20	-	-	0,000 34	-	-
	$u(D_{\text{res}})$ or $u(d_{\text{res}})$, m	0,000 29	0,000 29	0,000 29	0,000 29	0,000 29	0,000 29	0,000 29
	$u(D_{\text{va}})$ or $u(d_{\text{va}})$, m	0,001 73	0,001 15	0,000 29	0,000 29	0,001 15	0,000 29	0,000 29
	$u(D_{\text{ud}})$ or $u(d_{\text{ud}})$, m	0,008 66	0,008 66	0,001 44	0,001 44	0,008 66	0,001 44	0,001 44
$u_s(w)$	$u(D_{\text{cal}})$ or $u(d_{\text{cal}})$, m	0,000 89	0,000 65	0,000 07	0,000 07	0,001 13	0,000 07	0,000 07
	$u(D_{\text{th}})$ or $u(d_{\text{th}})$, m	0,000 12	0,000 09	0,000 00	0,000 00	0,000 16	0,000 00	0,000 00
	$u(D_{\text{dev}})$ or $u(d_{\text{dev}})$, m	0,000 95	0,000 70	0,000 02	0,000 02	0,001 22	0,000 02	0,000 02
$\Sigma u_r^2(w_i) \times 10^{-6}$, m^2		78,2	76,5	2,25	2,25	76,5	2,25	2,25
$\Sigma u_s^2(w_i) \times 10^{-6}$, m^2		1,71	0,921	0,007 8	0,007 8	2,78	0,007 8	0,007 8
Coefficient		1	0,5	1	2	0,5	1	2
Coeff. $\times u_r^2(w)/(n \times p) \times 10^{-6}$, m^2		3,91	19,1	1,13	0,113	4,78	0,281	0,028 1
Coeff. $\times u_s^2(w) \times 10^{-6}$, m^2		1,71	0,461	0,007 8	0,015 6	1,39	0,007 8	0,015 6
$u^2(w) \times 10^{-6}$, m^2		5,62	19,6	1,13	0,128	6,17	0,289	0,043 7
$\Sigma u^2(w) \times 10^{-6}$, m^2		5,62	20,8			6,50		