



SURFACE VEHICLE RECOMMENDED PRACTICE

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Drive Quality Evaluation for Chassis Dynamometer Testing

RATIONALE

To provide standardized metrics for evaluating drive quality on emissions and fuel economy tests. This document has been revised to include a new drive rating metric and typical driver capability ranges.

FOREWORD

It is generally recognized that the manner in which a vehicle is driven during a chassis dynamometer test can impact emissions and fuel economy results. The speed vs. time tolerances used to validate a test do limit this impact, but even within these constraints drive-related effects can be significant contributors to test variability. This document provides drive quality metrics intended to enable improved monitoring and characterization of driver-related variability.

TABLE OF CONTENTS

1.	SCOPE	2
2.	REFERENCES	2
2.1	Applicable Documents	2
2.1.1	SAE Publications	3
2.2	CFR Publications	3
3.	DEFINITIONS	3
4.	DRIVING SCHEDULES	6
4.1	UDDS	6
4.2	HFEDS	6
4.3	US06	6
4.4	SC03	6
4.5	"Cold" UDDS	6
4.6	Speed Tolerance	6

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5.	ENERGY-BASED DRIVE METRIC (EBDM)	7
5.1	Finite Difference Calculations	7
5.2	Energy Rating (ER)	11
5.3	Distance Rating (DR)	11
5.4	Energy Economy Rating (EER)	12
5.5	Absolute Speed Change Rating (ASCR)	12
5.6	Inertial Work Rating (IWR)	12
5.7	Recommended EBDM Phase Ratings for US Test Cycles.....	13
6.	SUPPLEMENTAL DRIVE RATING METRICS	14
6.1	Root Mean Squared Speed Error (RMSSE)	14
7.	DRIVE SCHEDULE INTENSITY METRICS	14
7.1	Cycle Energy Intensity (CE_{DIST}).....	15
7.2	Road Load and Inertial Work Contributions	15
7.3	ASC per Time (ASC_{Time}).....	15
7.4	Variation in Required Vehicle Power	15
7.5	Cycle Comparison Table	16
8.	LOCAL METRIC.....	17
9.	NOTES	17
9.1	Marginal Indicia	17
APPENDIX A	COEFFICIENT RESOLUTION AND TARGET REFERENCE VALUES.....	18
APPENDIX B	EXCEL-BASED CALCULATOR FOR EBDM DATA.....	19
APPENDIX C	METRIC AND DRIVER CAPABILITY	22
APPENDIX D		23
FIGURE 1	SPEED TOLERANCE DEFINITIONS	7
FIGURE B1	FILE FORMAT FOR DRIVE TRACE DATA	19
FIGURE B2	FIELD LOCATIONS FOR EBDM DRIVE RATINGS.....	21
TABLE 1	CYCLE INTENSITY METRICS FOR VEHICLES IN 2011 EPA TEST CAR DATABASE	17
TABLE A.1	EXAMPLE TARGET CYCLE ENERGY REFERENCE VALUES.....	18
TABLE B1	CYCLE ID DEFINITIONS FOR SAMPLED PHASES	20
TABLE C1	RANGES FOR DRIVE METRICS FROM DRIVER VARIABILITY STUDY	22

1. SCOPE

This SAE Recommended Practice establishes uniform procedures for evaluating conformity between the actual and target drive speeds for chassis dynamometer testing utilizing standard fuel economy and emissions drive schedules.

2. REFERENCES

2.1 Applicable Documents

The following publications form a part of this specification to the extent specified herein. Unless otherwise indicated, the latest issues of the SAE and the Code of Federal Regulations (CFR) publications shall apply.

United States Environmental Protection Agency, Specifications for Electric Chassis Dynamometers, Attachment A, RFP C100081T1, 1991.

2.1.1 SAE Publications

Available from SAE International, 400 Commonwealth Drive, Warrendale, PA 15096-0001, Tel: 877-606-7323 (inside USA and Canada) or 724-776-4970 (outside USA), www.sae.org.

SAE J2263 Road Load Measurement Using Onboard Anemometry and Coastdown Techniques

SAE J2264 Chassis Dynamometer Simulation of Road Load Using Coastdown Techniques

SAE J1711 Recommended Practice for Measuring the Exhaust Emissions and Fuel Economy of Hybrid-Electric Vehicles, Including Plug-in Hybrid Vehicles

2.2 CFR Publications

The CFR is available from the Superintendent of Documents, U.S. Government Printing Office, Mail Stop: SSOP, Washington, DC, 20402-9320, <http://www.gpoaccess.gov/cfr/index.html>.

40 CFR Part 86 Control of Air Pollution from New and In-Use Motor Vehicles and New and In-Use Motor Vehicle Engines; Certification and Test Procedure

40 CFR Part 600 Fuel Economy of Motor Vehicles

3. DEFINITIONS

3.1 ETW CLASS (EQUIVALENT TEST WEIGHT)

Test mass dictated by U.S. Code of Federal Regulations that is assigned to represent a class of test vehicles (40 CFR § 86.129-80). ETW is a weight class, and is not necessarily equal to the as-tested weight of a vehicle.

3.2 DYNAMOMETER SET INERTIA (M_{SET})

The setting that specifies the inertia that is to be simulated by the dynamometer. The M_{SET} equals ETW for regulatory testing using 2WD chassis dynamometers. For testing on a 4WD chassis dynamometer, M_{SET} equals 98.5% of ETW.

3.3 EFFECTIVE TEST MASS (M_E)

Effective Test Mass (M_E) is the sum of 1) the dyno-simulated inertia (M_{SET}) and 2) the effective inertia of the vehicle components (e.g. wheels, axles) that are rotated on the dynamometer. This value describes the total inertial load acting on the vehicle system, and is required to calculate the inertial component of cycle energy.

For light-duty vehicles the effective inertia of the rotating components, per axle, may be estimated by taking 1.5% of the ETW. However vehicles with other than single, normal-sized wheels, such as dual-wheel trucks, may require specific estimation or determination of the effective mass of the rotating drivetrain components. Using 1.5% of ETW per axle, and the definition of M_{SET} above, gives the following equation for determining the effective test mass for both 2WD and 4WD dynamometer testing:

$$M_E = 1.015 \cdot ETW \quad (\text{Eq. 1})$$

3.4 Dyno Target Coefficients: F_x (F_0 , F_1 and F_2)

Target coefficients describe the total force (tire, drivetrain and aerodynamic drag) acting on a vehicle during an on-road coastdown. These coefficients are developed from track data (and/or equivalent analytical methodology), corrected to standard conditions, and possibly adjusted to account for differences between vehicle weight as tested on the track and weight represented by an ETW class assigned for dynamometer testing.

3.5 SIMULATION MODE

The operating mode where the dynamometer simulates the vehicle inertia and road load commanded by the dynamometer set inertia (M_{SET}) and Dyno Set coefficients (D_x), respectively, so that a vehicle driven on the dynamometer operates as it would on the road.

3.6 VEHICLE SPEED (V)

3.6.1 Roll Speed (V_{ROLL})

The inferred vehicle speed as measured by the dynamometer. Roll encoder speed sampled at 10Hz shall be used as the roll speed, and shall be the same or equivalent speed signal that is used to determine conformance with the speed vs. time tolerance in 40 CFR Part 86.115-78 Appendix 1.

3.6.2 Scheduled Speed (V_{SCHED})

The target vehicle speed as specified by the speed vs. time requirements for a drive schedule. Scheduled speed is defined by a smooth trace drawn through the specified speed versus time relationship (40CFR 600.109–78). A linear interpolation between the 1Hz speed points given in the CFR shall be used to produce the 10Hz scheduled speed trace (V_{SCHED}).

3.6.3 Vehicle Speed – Driven (V_D)

The vehicle speed derived from the roll speed data (V_{ROLL}) for the purposes of calculating the drive metrics described in this document. The driven vehicle speed is used for the calculation of driven cycle energy and is calculated by taking a 0.5 s, double moving average of the 10Hz roll speed signal. After performing the double moving average, all values less than or equal to 0.03 m/s are set to zero. This is done to reduce the impact of noise in the roll speed signal on the results. A moving average was chosen over other filter types as it provides the best compromise between smoothing the time series and preserving the response time of the signal.

The subscript "D" will be used to refer to quantities calculated from the driven vehicle speed.

3.6.4 Vehicle Speed – Target (V_T)

The target vehicle speed, calculated in the same manner as V_D but using the scheduled speed (V_{SCHED}) instead of the roll speed (V_{ROLL}). The target vehicle speed is used for the calculation of target cycle energy.

The subscript "T" will be used to refer to quantities calculated from the target vehicle speed.

3.7 SAMPLING PERIOD (Δt)

The time between successive samples of V_{ROLL} and V_{SCHED} . The calculations in this document require a sampling frequency of 10 Hz, which corresponds to a sampling period of 0.1 s. Higher sampling frequencies may be used if 10 Hz is not possible, however the data must first be downsampled to 10 Hz, using good engineering judgement to ensure representative results, in order to maintain compatibility with the finite-difference calculations defined in Section 5.1.

3.8 VEHICLE ACCELERATION (a)

The acceleration of the vehicle calculated as the time-rate-of-change of the vehicle speed (V). The specifics of this calculation are detailed in Section 5.1.2.

3.9 ROAD LOAD FORCE (F_{RL})

The combination of intrinsic and dyno-simulated forces opposing the vehicle's motion on the dynamometer that are intended to duplicate the internal and external vehicle parasitic forces the engine must work against while driving on the road. These forces are primarily comprised of aerodynamic drag, driveline parasitic losses and tire rolling resistance. The road load force is calculated using vehicle speed (V) and the Dyno Target Coefficients.

$$F_{RL} = F_0 + F_1 \cdot V + F_2 \cdot V^2 \quad (\text{Eq. 2})$$

For testing performed at 20 °F (-7 °C), the road load force should be approximated as $1.10 \times F_{RL}$ unless road load coefficients derived at 20F are used.

3.10 INERTIAL FORCE (F_I)

The combination of intrinsic and dyno-simulated forces opposing the vehicle's motion on the dynamometer that represents the effect of its mass and the rotational inertia of its driveline components while driving on the road. Inertial force is calculated using the effective test mass (M_E) and vehicle acceleration (a).

$$F_I = M_E \cdot a \quad (\text{Eq. 3})$$

Substituting Eq. 1 (See Section 3.3) for M_E gives

$$F_I = 1.015 \cdot ETW \cdot a \quad (\text{Eq. 4})$$

3.11 ENGINE FORCE (F_{ENG})

The sum of the inertial force (F_I) and the road load force (F_{RL}). The engine force represents the sum of all the forces that oppose the vehicle's motion while driving on the dyno. It is equal to the sum of the road load force and inertial force when this sum is positive, and zero when this sum is negative. (A negative sum of F_{RL} and F_I is interpreted as braking, and not considered "engine" force.)

$$F_{ENG} = [F_{RL} + F_I]^+ \quad (\text{Eq. 5})$$

The term "engine" is a general reference to the power-generating system of the vehicle, and its use is not restricted to systems that use an internal combustion engine. In hybrid electric or battery-electric vehicles F_{ENG} may represent, in part or in whole, work that is done by an electric motor.

3.12 DISTANCE INCREMENT (d)

The incremental distance traveled by the vehicle during each sampled data point, calculated from the 10 Hz vehicle speed (V) and the sampling period (Δt).

3.13 ACCUMULATED DISTANCE (D)

The total distance traveled by the vehicle, calculated by summing the distance increments (d) over the test cycle.

3.14 ENGINE WORK INCREMENT (w)

The incremental work done by the vehicle during each sampled data point, calculated by multiplying the engine force (F_{ENG}) by the distance increment (d) for each 10 Hz sampled data point.

3.15 CYCLE ENERGY (CE)

The net energy a vehicle must provide in order to drive a test cycle on a chassis dynamometer. Cycle energy is calculated by summing the engine work increments (w) over the test cycle. By definition, the engine work increments are always positive (since $F_{\text{ENG}} \geq 0$), so negative work is excluded from the cycle energy summation. The exclusion of negative work is appropriate since it is associated primarily with braking events and represents energy that is not recovered unless the vehicle is equipped with a regenerative braking system (alternative equations for the summation of work for vehicles equipped with regenerative braking may be considered in future revisions of this document).

Note that the engine work increment (w) may still be positive even during decelerations. This is because even though the inertial force is negative during decelerations, engine force (F_{ENG}) will still be positive if the magnitude of the road load force is greater than the magnitude of the inertial force. In this case the engine is still doing work, but the output from the engine is insufficient to maintain the vehicle's speed.

4. DRIVING SCHEDULES

There are five driving schedules referenced in this document which are required by the EPA and the California Air Resources Board during emissions and fuel economy certification of vehicles with internal combustion engines. They are the Urban Dynamometer Driving Schedule (UDDS), the "Cold" UDDS, the Highway Fuel Economy Driving Schedule (HFEDS), the US06 Driving Schedule (US06), and the SC03 Driving Schedule (SC03).

4.1 UDDS

The Urban Dynamometer Driving Schedule is defined in 40 CFR Part 86, Appendix 1. It has a duration of 22 min, 52 s. It is used to represent vehicle city driving.

4.2 HFEDS

The Highway Fuel Economy Driving Schedule is defined in 40 CFR Part 600, Appendix 1. It has a duration of 12 min, 45 s. It is used to represent vehicle highway driving. The Highway Fuel Economy Test (HFET) consists of two HFEDS cycles.

4.3 US06

The US06 Driving Schedule is defined in 40 CFR Part 86, Appendix 1. It has a duration of 10 min. It is used to represent vehicles driving at high speeds and with aggressive accelerations. Dynamometer load reduction for low-powered vehicles may be used in accordance with 40 CFR Part 86.108 00(b)(2)(ii). The US06 cycle is subdivided into a "City" test (0-130 s and 495-600 s) and a "Highway" test (130-495 s) for the purposes of 5-cycle fuel economy labeling [40 CFR § 86.159-08 Exhaust emission test procedures for US06 emissions].

NOTE: If dynamometer load reduction for low-powered vehicles is utilized, the energy-related evaluations outlined in this Recommended Practice are not valid.

4.4 SC03

The SC03 Driving Schedule is defined in 40 CFR Part 86, Appendix 1. It has a duration of 10 min. It is used to represent vehicle operation with air conditioning.

4.5 "Cold" UDDS

Same as UDDS schedule. The test is performed in cold ambient conditions as defined in 40 CFR Part 86, Subpart C.

4.6 Speed Tolerance

The speed tolerance at any given time on these driving schedules is defined by the upper and lower limits, as described in 40 CFR (Part 86.115-78 and Appendix 1).

The diagrams in Figure 1 show the EPA range of acceptable speed tolerances for typical points, per § 86.115-78: EPA Urban Dynamometer Driving Schedules. The curve on the left is typical of portions of the speed curve that are increasing or decreasing throughout the 2-s time interval. The curve on the right is typical of portions of the speed curve that include a maximum or minimum value.

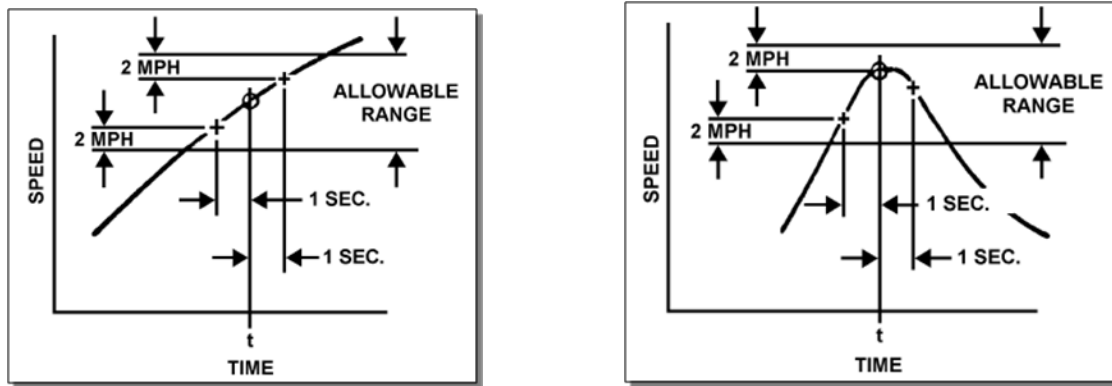


FIGURE 1 - SPEED TOLERANCE DEFINITIONS

EPA provides additional guidance per § 86.128-00 (d): The vehicle shall be driven with appropriate accelerator pedal movement necessary to achieve the speed versus time relationship prescribed by the driving schedule. Both smoothing of speed variations and excessive accelerator pedal perturbations are to be avoided.

5. ENERGY-BASED DRIVE METRIC (EBDM)

5.1 Finite Difference Calculations

Throughout this section, quantities that represent 10 Hz data (time series data) are subscripted with an index, i or j . This index may assume a value from 1 to N , where 1 represents the first data point in the series, 2 represents the next, and so on. Summations over the range from 1 to N represent summation over the entire test cycle.

5.1.1 Driven and Target Speeds (V_D , V_T)

The driven and target vehicle speeds are calculated by taking a 0.5 s, double moving average of the 10Hz roll speed and scheduled speed signals, respectively. The 0.5 s double moving average of the roll speed is calculated as follows:

Step 1: Take a 0.5 s moving average of the 10Hz roll speed (V_{ROLL}).

$$V_{ROLL_AVG_1_i} = \frac{1}{5} \sum_{j=i-2}^{j=i+2} V_{ROLL_j} \quad (\text{Eq. 6})$$

$V_{ROLL_AVG_1_i}$ is set to 0 if $i < 3$ or $i > N-2$, in order to avoid a condition where $j < 1$ or $j > N$.

Step 2: Take a 0.5 s moving average of $V_{ROLL_AVG_1}$. The result is the driven vehicle speed (V_D), and the intermediate quantity, $V_{ROLL_AVG_1}$, is not used for any further calculations.

$$V_{D_i} = V_{ROLL_AVG_2_i} = \frac{1}{5} \sum_{j=i-2}^{j=i+2} V_{ROLL_AVG_1_j} \quad (\text{Eq. 7})$$

Again, V_{D_i} is set to 0 if $i < 3$ or $i > N-2$.

Step 3: After performing the double moving average, all values for V_{D_i} less than or equal to 0.03 m/s are set to zero. This is done to reduce the impact of noise in the roll speed signal on the results

The target vehicle speed (V_T) is calculated in the same manner, using the 10 Hz scheduled speed (V_{SCHED}) instead of the roll speed (V_{ROLL}).

$$V_{\text{SCHED_AVG_1}_i} = \frac{1}{5} \sum_{j=i-2}^{j=i+2} V_{\text{SCHED}_j} \quad (\text{Eq. 8})$$

$$V_{T_i} = V_{\text{SCHED_AVG_2}_i} = \frac{1}{5} \sum_{j=i-2}^{j=i+2} V_{\text{SCHED_AVG_1}_j} \quad (\text{Eq. 9})$$

Both V_D and V_T have units of m/s.

5.1.2 Driven and Target Vehicle Acceleration (a_D , a_T)

The driven and target acceleration of the vehicle are calculated from the 10Hz driven and target vehicle speeds using a central-difference approximation. The sampling period, Δt , should be expressed in s so that the acceleration will have units of m per s per s (m/s^2). a_{D_i} and a_{T_i} are set to 0 if $i = 1$ or N .

$$a_{D_i} = \frac{V_{D_{i+1}} - V_{D_{i-1}}}{t_{i+1} - t_{i-1}} = \frac{V_{D_{i+1}} - V_{D_{i-1}}}{2\Delta t} \quad (\text{Eq. 10})$$

$$a_{T_i} = \frac{V_{T_{i+1}} - V_{T_{i-1}}}{t_{i+1} - t_{i-1}} = \frac{V_{T_{i+1}} - V_{T_{i-1}}}{2\Delta t} \quad (\text{Eq. 11})$$

$$2\Delta t = 0.2 \text{ seconds @10Hz}$$

5.1.3 Driven and Target Distance Increment (d_D , d_T)

The driven and target distance increments are calculated by multiplying the 10Hz driven and target vehicle speeds by the sampling period. The distance increment will have units of m.

$$d_{D_i} = V_{D_i} \cdot \Delta t \quad (\text{Eq. 12})$$

$$d_{T_i} = V_{T_i} \cdot \Delta t \quad (\text{Eq. 13})$$

$$\Delta t = 0.1 \text{ seconds @10Hz}$$

5.1.4 Driven and Target Accumulated Distance (D_D , D_T)

The driven and target accumulated distances are calculated by summing the distance increments over the test cycle. The accumulated distance will have units of m.

$$D_D = \sum_{i=1}^N d_{D_i} \quad (\text{Eq. 14})$$

$$D_T = \sum_{i=1}^N d_{T_i} \quad (\text{Eq. 15})$$

5.1.5 Driven and Target Road Load Forces (F_{RL-D} , F_{RL-T})

The driven and target road load forces are calculated by using the 10 Hz driven and target vehicle speeds and Dyno Target coefficients as shown below. The Dyno Target coefficients should be expressed in units of N, m and s so that the road load force will have units of N.

$$F_{RL-Di} = F_0 + F_1 \cdot V_{Di} + F_2 \cdot V_{Di}^2 \quad (\text{Eq. 16})$$

$$F_{RL-Ti} = F_0 + F_1 \cdot V_{Ti} + F_2 \cdot V_{Ti}^2 \quad (\text{Eq. 17})$$

NOTE: Dyno Target coefficients are typically reported in units of lbf, lbf/(mi/h), and lbf/(mi/h)². In this case, multiplying F_0 , F_1 and F_2 by 4.448, 9.9504 and 22.25839, respectively, will convert these terms to the appropriate units for the calculations specified in this document (N, N/(m/s), and N/(m/s)²).

5.1.6 Driven and Target Inertial Forces (F_{I-D} , F_{I-T})

The driven and target inertial forces are calculated by multiplying the driven and target vehicle accelerations by the effective test mass. The effective test mass should be expressed in kg so that the inertial force will have units of N.

$$F_{I-Di} = M_E \cdot a_{Di} = 1.015 \cdot ETW \cdot a_{Di} \quad (\text{Eq. 18})$$

$$F_{I-Ti} = M_E \cdot a_{Ti} = 1.015 \cdot ETW \cdot a_{Ti} \quad (\text{Eq. 19})$$

NOTE: ETW is typically reported in units of lbf. In this case, multiplying ETW by 0.4536 will convert this value to the appropriate units for the calculations specified in this document (kg).

5.1.7 Driven and Target Engine Force (F_{ENG-D} , F_{ENG-T})

The driven and target engine forces are calculated by summing the driven and target road load and inertial forces. Where this sum is negative, the driven and target engine forces are set to zero. The engine force will have units of N.

$$F_{ENG-Di} = \begin{cases} F_{RL-Di} + F_{I-Di} & \text{for } F_{RL-Di} + F_{I-Di} > 0 \\ 0 & \text{for } F_{RL-Di} + F_{I-Di} \leq 0 \end{cases} \quad (\text{Eq. 20})$$

$$F_{ENG-Ti} = \begin{cases} F_{RL-Ti} + F_{I-Ti} & \text{for } F_{RL-Ti} + F_{I-Ti} > 0 \\ 0 & \text{for } F_{RL-Ti} + F_{I-Ti} \leq 0 \end{cases} \quad (\text{Eq. 21})$$

5.1.8 Driven and Target Road Load Work Increment (w_{RL-T})

The target incremental work that must be done by the vehicle at each sampled data point due to the road load force (F_{RL-T}). The road load work increment has units of joules.

$$w_{RL-Di} = F_{RL-Di} \cdot d_{Di} \quad (\text{Eq. 22})$$

$$w_{RL-Ti} = F_{RL-Ti} \cdot d_{Ti} \quad (\text{Eq. 23})$$

5.1.9 Driven and Target Inertial Work Increment (w_{I-T})

The target incremental work that must be done by the vehicle at each sampled data point due to the inertial force (F_{I-T}). The inertial work increment has units of joules.

$$w_{I-Di} = F_{I-Di} \cdot d_{Di} \quad (\text{Eq. 24})$$

$$w_{I-Ti} = F_{I-Ti} \cdot d_{Ti} \quad (\text{Eq. 25})$$

5.1.10 Driven and Target Engine Work Increment (w_D , w_T)

The driven and target work increments are calculated by multiplying the driven and target engine forces by the driven and target distance increments, respectively. The work increment will have units of joules (J). Note that incremental engine work is always positive (or zero) since it is calculated using F_{ENG} .

$$w_{Di} = F_{ENG-Di} \cdot d_{Di} \quad (\text{Eq. 26})$$

$$w_{Ti} = F_{ENG-Ti} \cdot d_{Ti} \quad (\text{Eq. 27})$$

5.1.11 Driven and Target Cycle Energy (CE_D , CE_T)

The driven and target cycle energy are calculated by summing the driven and target engine work increments over the test cycle. The cycle energy will have units of joules.

$$CE_D = \sum_{i=1}^N w_{Di} \quad (\text{Eq. 28})$$

$$CE_T = \sum_{i=1}^N w_{Ti} \quad (\text{Eq. 29})$$

Alternatively, the equations for cycle energy may be equivalently represented using the sum of inertia and road load forces. Substituting equations from Sections 5.1.7, 5.1.8, 5.1.9, gives

$$CE_D = \sum_{i=1}^N \left[\left(1.015 \cdot ETW \cdot a_{Di} + F_0 + F_1 V_{Di} + F_2 V_{Di}^2 \right) \cdot d_{Di} \right]^+ \quad (\text{Eq. 30})$$

$$CE_T = \sum_{i=1}^N \left[\left(1.015 \cdot ETW \cdot a_{Ti} + F_0 + F_1 V_{Ti} + F_2 V_{Ti}^2 \right) \cdot d_{Ti} \right]^+ \quad (\text{Eq. 31})$$

NOTE: Only positive values of the force-distance products in Equation 28 and Equation 29 are included in the summation.

5.1.12 Driven and Target Absolute Speed Change Summation (ASC_D , ASC_T)

The ASC is the discrete approximation for the integral of the absolute magnitude of acceleration. It indicates the extent of velocity variation that is exhibited over the driven and scheduled cycles. Multiplication by the sampling period, Δt , provides the correct "weight" for each data point in the approximation of the integral. ASC has units of m per s (m/s), although it should not be interpreted as a velocity.

$$ASC_D = \Delta t \sum_{i=1}^N |a_{Di}| \quad (\text{Eq. 32})$$

$$ASC_T = \Delta t \sum_{i=1}^N |a_{Ti}| \quad (\text{Eq. 33})$$

$$\Delta t = 0.1 \text{ seconds @10Hz}$$

5.1.13 Driven and Target Inertial Work (IW_D , IW_T)

The total work done by the engine against inertial loading. Only positive values of the inertial work increment (w_{I-T}) are considered since negative inertial work is not recovered by the engine (this assumption is not valid for vehicles with regenerative braking systems). Negative inertial work is taken to represent either: 1) energy dissipated by braking and thus not recovered by the vehicle or 2) energy that serves to reduce the road load work required of the engine during non-braking decelerations.

$$IW_D = \sum_{i=1}^N [w_{I-Di}]^+ \quad (\text{Eq. 34})$$

$$IW_T = \sum_{i=1}^N [w_{I-Ti}]^+ \quad (\text{Eq. 35})$$

5.2 Energy Rating (ER)

The Energy Rating for a test is defined as the percent difference between the total driven and target cycle energy as defined in Section 5.1.11.

$$ER = \frac{CE_D - CE_T}{CE_T} \cdot 100 \quad (\text{Eq. 36})$$

5.3 Distance Rating (DR)

The Distance Rating for a test is defined as the percent difference between the total driven and scheduled distance as defined in Section 5.1.4.

$$DR = \frac{D_D - D_T}{D_T} \cdot 100 \quad (\text{Eq. 37})$$

5.4 Energy Economy Rating (EER)

The EER is defined as the percentage difference between the distance per unit cycle energy for the driven and target traces. Since fuel economy is a measure of the distance traveled per unit of fuel consumed, the effect of distance driven must also be considered in an assessment of a drive quality that is intended to correlate with fuel economy.

$$EER = - \frac{\left(\frac{D}{CE}\right)_D - \left(\frac{D}{CE}\right)_T}{\left(\frac{D}{CE}\right)_T} \cdot 100 \quad (\text{Eq. 38})$$

The negative sign in front of the right-hand-side of Equation 36 associates lower values of fuel economy with higher values of EER, similar to the expected relationship for ER and DR. The EER may be expressed as a combination of the Energy Rating (ER) and Distance Rating (DR) as follows:

$$EER = \left[1 - \frac{DR/100 + 1}{ER/100 + 1} \right] \cdot 100 \quad (\text{Eq. 39})$$

5.5 Absolute Speed Change Rating (ASCR)

The ASCR is defined as the percentage difference between the ASC for the driven and target traces. It provides an indicator of the "smoothness" of the driven trace relative to the scheduled trace. A driven trace that is "smoother" will have a lower ASC than the scheduled trace and so will result in a negative ASCR.

$$ASCR = \frac{ASC_D - ASC_T}{ASC_T} \cdot 100 \quad (\text{Eq. 40})$$

The ASCR is particularly well-suited to quantifying small speed changes that might come about from throttle perturbations. It should be noted that these perturbations ONLY affect the ASC when they are sufficient to change the speed of the vehicle. It is possible for a driver to intentionally produce small, high-frequency throttle movements that do not result in dynamometer roll speed changes. Such movements would not be captured by a speed-based metric. While such throttle movements can be intentionally produced, they are considered unlikely to occur in practice since they do not contribute toward making a vehicle follow a target trace.

5.6 Inertial Work Rating (IWR)

The IWR is defined as the percentage difference between the inertial work for the driven and target traces. It can indicate when the drive style might substantially impact the overall efficiency of the engine, such that a metric based strictly on cycle energy might not fully characterize observed deviations from expected emission rates.

$$IWR = \frac{IW_D - IW_T}{IW_T} \cdot 100 \quad (\text{Eq. 41})$$

5.7 Recommended EBDM Phase Ratings for US Test Cycles

5.7.1 City (FTP and FTP4)

The drive ratings specified in Section 5.1-5.4 must be calculated individually for each phase of the FTP ("3-bag") and FTP4 ("4-bag") tests. Additionally, weighted city ratings should be calculated by using the weighted values of the relevant quantities: The weighted distance-per-cycle-energy values are used to calculate the weighted EER, the weighted ASC values are used to calculate the weighted ASCR, and the weighted positive inertial work values are used to calculate the weighted IWR, as defined by Equations 40-51 in this section:

FTP-Weighted EER

$$\left(\frac{D}{CE} \right)_{\text{Weighted FTP}} = \frac{1}{0.43 \left(\frac{CE_{\text{phase1}} + CE_{\text{phase2}}}{D_{\text{phase1}} + D_{\text{phase2}}} \right) + 0.57 \left(\frac{CE_{\text{phase2}} + CE_{\text{phase3}}}{D_{\text{phase2}} + D_{\text{phase3}}} \right)} \quad (\text{Eq. 42})$$

$$EER_{\text{Weighted FTP}} = - \frac{(D/CE)_{\text{Weighted FTP}_D} - (D/CE)_{\text{Weighted FTP}_T}}{(D/CE)_{\text{Weighted FTP}_T}} \cdot 100 \quad (\text{Eq. 43})$$

FTP4-Weighted EER

$$\left(\frac{D}{CE} \right)_{\text{Weighted FTP4}} = \frac{1}{0.43 \left(\frac{CE_{\text{phase1}} + CE_{\text{phase2}}}{D_{\text{phase1}} + D_{\text{phase2}}} \right) + 0.57 \left(\frac{CE_{\text{phase3}} + CE_{\text{phase4}}}{D_{\text{phase3}} + D_{\text{phase4}}} \right)} \quad (\text{Eq. 44})$$

$$EER_{\text{Weighted FTP4}} = - \frac{(D/CE)_{\text{Weighted FTP4}_D} - (D/CE)_{\text{Weighted FTP4}_T}}{(D/CE)_{\text{Weighted FTP4}_T}} \cdot 100 \quad (\text{Eq. 45})$$

FTP-Weighted ASCR

$$ASC_{\text{Weighted FTP}} = 0.43(ASC_{\text{phase1}} + ASC_{\text{phase2}}) + 0.57(ASC_{\text{phase2}} + ASC_{\text{phase3}}) \quad (\text{Eq. 46})$$

$$ASCR_{\text{Weighted FTP}} = \frac{ASC_{\text{Weighted FTP}_D} - ASC_{\text{Weighted FTP}_T}}{ASC_{\text{Weighted FTP}_T}} \cdot 100 \quad (\text{Eq. 47})$$

FTP4-Weighted ASCR

$$ASC_{\text{Weighted FTP4}} = 0.43(ASC_{\text{phase1}} + ASC_{\text{phase2}}) + 0.57(ASC_{\text{phase3}} + ASC_{\text{phase4}}) \quad (\text{Eq. 48})$$

$$ASCR_{\text{Weighted FTP4}} = \frac{ASC_{\text{Weighted FTP4}_D} - ASC_{\text{Weighted FTP4}_T}}{ASC_{\text{Weighted FTP4}_T}} \cdot 100 \quad (\text{Eq. 49})$$

FTP-Weighted IWR

$$IW_{\text{Weighted FTP}} = 0.43(IW_{\text{phase1}} + IW_{\text{phase2}}) + 0.57(IW_{\text{phase2}} + IW_{\text{phase3}}) \quad (\text{Eq. 50})$$

$$IWR_{\text{Weighted FTP}} = \frac{IW_{\text{Weighted FTP}_D} - IW_{\text{Weighted FTP}_T}}{IW_{\text{Weighted FTP}_T}} \cdot 100 \quad (\text{Eq. 51})$$

FTP4-Weighted IWR

$$IW_{\text{Weighted FTP4}} = 0.43(IW_{\text{phase1}} + IW_{\text{phase2}}) + 0.57(IW_{\text{phase3}} + IW_{\text{phase4}}) \quad (\text{Eq. 52})$$

$$IWR_{\text{Weighted FTP4}} = \frac{IW_{\text{Weighted FTP4_D}} - IW_{\text{Weighted FTP4_T}}}{IW_{\text{Weighted FTP4_T}}} \cdot 100 \quad (\text{Eq. 53})$$

These weighted calculations produce a drive rating that reflects the weighted fuel economy result reported for the City test. The weighted equations in this section also apply to the Cold FTP.

5.7.2 Highway (HFET) and SC03 Reporting

Highway and SC03 drive metrics are reported for the sampled HFEDS or SC03 phase. Warm-up phases do not require a drive rating.

5.7.3 US06 Reporting

Drive ratings for the US06 test are calculated for the sampled phase of the US06. Warm-up phases do not require a drive rating. The rating must be calculated separately for the "City" and "Highway" portions (See Section 4.3) in addition to calculating an overall test cycle result. Data from the two regions of the test that make up the "City" portion of the cycle are treated as a single phase for the drive rating calculations.

6. SUPPLEMENTAL DRIVE RATING METRICS

For a well-trained driver, it is expected that an energy-based metric will capture the majority of the fuel economy impact that is attributable to drive quality. However, energy alone cannot always fully characterize a drive. This is because the drive energy approach quantifies only the net energy demanded by a drive, and not a drive's impact on engine efficiency (i.e., fundamentally different drive styles can produce the same net demanded energy). For example, small, rapid throttle movements may not significantly impact net energy, but can reduce fuel economy. The supplemental metrics provided in this section are intended to complement the energy-based drive metrics given in Section 5 by capturing certain drive characteristics that are not always reflected in an energy analysis.

6.1 Root Mean Squared Speed Error (RMSSE)

The RMSSE metric provides the driver's performance in meeting the schedule speed trace throughout the test cycle in terms of the Root Mean Squared (RMS) Speed Error. The value is always a positive number with lower values (closer to zero) indicating better performance. RMS Speed Error has units of miles per hour (mi/h).

$$RMSSE = 2.237 \cdot \sqrt{\frac{\sum_{i=1}^N (V_{Di} - V_{Ti})^2}{N}} \quad (\text{Eq. 54})$$

The multiplier (2.237) is included in Equation 52 to convert the output to mi/h, assuming that VD and VT are in units of m/s as specified in 5.1.1.

7. DRIVE SCHEDULE INTENSITY METRICS

The intent of this section is to introduce several quantities that may be used in the future to quantify the "intensity" of a particular drive schedule. As new schedules are developed, it is expected that one or more of these intensity metrics may provide an indication of the expected fuel economy that would be exhibited by a vehicle driving the schedule, relative to its fuel economy when driving other schedules.

7.1 Cycle Energy Intensity (CE_{DIST})

Cycle energy intensity is the energy that is required to drive the cycle (CE_T), normalized by the total distance of the cycle (D_T). CE_{DIST} has units of joules per meter.

$$CE_{Dist} = \frac{CE_T}{D_T} \quad (\text{Eq. 55})$$

7.2 Road Load and Inertial Work Contributions

7.2.1 Inertial Work Fraction (IWF)

The fraction of the total target cycle energy that the engine must provide that is due to inertial loading. The IWF is a unitless quantity.

$$IWF = \frac{IW_T}{CE_T} \quad (\text{Eq. 56})$$

7.2.2 Road Load Work Fraction (RLWF)

The fraction of the total target cycle energy that the engine must provide that is due to road load work. Because the road load work and the inertial work together represent all of the work done by the engine, the road load work fraction can be defined in terms of the IWF. The RLWF is a unitless quantity.

$$RLWF = 1 - IWF \quad (\text{Eq. 57})$$

7.3 ASC per Time (ASC_{Time})

This is the absolute speed change (ASC_T), normalized by the total time of the test cycle (as defined in Section 4). ASC_{Time} has units of m-per-s-per-s (m/s^2).

$$ASC_{Time} = \frac{ASC_T}{\text{totaltime}} \quad (\text{Eq. 58})$$

7.4 Variation in Required Vehicle Power

It is important to quantify not only the total energy that is required to drive a test cycle, but also the variation in the power demands that will be made on the propulsion system. Large variations in the required power will affect overall operating efficiency, which will impact fuel economy.

7.4.1 Power (P)

The instantaneous power required to drive the test cycle, calculated by multiplying the engine force (F_{ENG-T}) by the velocity (V_T). Note that this is identical to dividing the engine work increment (w_T) by the sampling period (Δt). The power will have units of watts (W).

$$P_i = F_{ENG-Ti} \cdot V_{Ti} = \frac{w_{Ti}}{\Delta t} \quad (\text{Eq. 59})$$

7.4.2 Absolute Power Change (APC)

The calculation of the absolute power change is analogous to the calculation of the absolute speed change (ASC), using the time-derivative of the power in place of acceleration (a). The time-derivative of power is calculated from the power using a central-difference approximation in the same manner that the acceleration is calculated from the velocity. The APC will have units of W.

$$APC = \Delta t \sum_{i=1}^N \left| \frac{dP}{dt} \right|_i \quad (\text{Eq. 60})$$

7.4.3 Absolute Power Change per Time (APC_{Time})

This is the absolute power change (APC), normalized by the total time of the test cycle, in s (as defined in Section 4). The APC_{Time} will have units of W per s (W/s).

$$APC_{\text{Time}} = \frac{APC}{\text{totaltime}} \quad (\text{Eq. 61})$$

7.5 Cycle Comparison Table

Table 1 provides a comparison of intensity metrics for various cycles. Note that since ASC per time is obtained strictly from the drive schedule, it does not depend on vehicle-specific data (e.g., ETW, Dyno Target coefficients). For this reason ASC per time (and ASC) may be regarded as fixed properties of a given test cycle. This is not true for other intensity metrics that are tabulated in Table 1, hence the inclusion of a mean and standard deviation.

For a particular combination of metric and drive schedule, the mean and standard deviation were obtained by performing the calculations using the ETW and Dyno Target coefficients for the 1226 unique vehicle configurations listed in the 2011 EPA Test Car database. Entries for which the reported Dyno Set and Dyno Target coefficients were equal were excluded from the population.

For metrics that are represented per unit time or distance (CE, ASC, APC), the weighted FTP values were calculated by applying phase weightings separately to the numerator and denominator. For IWR, the summed positive inertial work and the cycle energy were weighted separately and then divided as shown in Equation 54. Note that target values for the 4-bag total, the weighted 3-bag test and the weighted 4-bag test are the same, since the scheduled speed for phases 1 and 3 is the same, and the scheduled speed for phases 2 and 4 is the same.

TABLE 1 - CYCLE INTENSITY METRICS FOR VEHICLES IN 2011 EPA TEST CAR DATABASE

Test Cycle/Metric	CE _{DIST} (J/m)		IWF (%)		APC _{TIME} (W/s)		ASC _{TIME} (m/s ²)
	Mean	Std Dev	Mean	Std Dev	Mean	Std Dev	-
FTP Phase 1, 3	611	131	55%	3%	2470	511	0.41
FTP Phase 2	517	107	67%	3%	1508	311	0.39
FTP (3-Bag)	578	122	59%	3%	2026	419	0.40
FTP4 (4-Bag)	563	118	61%	3%	1863	385	0.40
FTP & FTP4 Weighted	563	118	61%	3%	1863	385	0.40
Highway (HFEDS)	552	128	25%	3%	2008	417	0.17
US06 City	1167	243	79%	2%	5695	1179	1.04
US06 Highway	793	186	32%	3%	12360	2569	0.31
US06 Total	875	196	46%	4%	9738	2022	0.60
SC03	615	129	65%	3%	2450	507	0.42
LA92*	729	155	60%	3%	3839	795	0.51

¹The LA92 cycle, also known as the "Unified Cycle," is not currently used for any regulatory testing but is included here because it is a widely-known cycle that may be used for regulatory testing in the future. The LA92 was developed by CARB in 1992 to represent a more aggressive urban driving style than the UDDS.

8. LOCAL METRIC

It is possible for the measured fuel economy and/or emissions to be significantly affected by severe, short-duration excursions from the scheduled drive trace. Due to their short duration, the impact of these excursions might not be reflected in drive metrics that are summed or averaged over the entire cycle, such as those described in Sections 5 and 6. The development of suitable "local" metrics that are capable of identifying significant, discrete drive events will be addressed in a future revision of the document.

9. NOTES

9.1 Marginal Indicia

A change bar (I) located in the left margin is for the convenience of the user in locating areas where technical revisions, not editorial changes, have been made to the previous issue of this document. An (R) symbol to the left of the document title indicates a complete revision of the document, including technical revisions. Change bars and (R) are not used in original publications, nor in documents that contain editorial changes only.

APPENDIX A - COEFFICIENT RESOLUTION AND TARGET REFERENCE VALUES

A.1 COEFFICIENT AND METRIC RESOLUTION

Number of decimal digits.

F_0 xxx.xx lbf

F_1 x.xxxx lbf/(mi/h)

F_2 0.xxxxx lbf/(mi/h)²

ETW, M_E 1 lb

ER xx.xx %

DR xx.xx %

EER xx.xx %

ASCR xx.xx %

A.2 TARGET CYCLE REFERENCE VALUES

Table A.1 shows the cycle energy reference values for each phase.

TABLE A.1 - EXAMPLE TARGET CYCLE ENERGY REFERENCE VALUES

Test/Target Values	Cycle	CE_T^* (MJ)
FTP	UDDS Phase 1	3.434
FTP	UDDS Phase 2	3.132
FTP	UDDS Phase 3	3.434
FTP	3-Bag FTP	10.000
FTP	4-Bag FTP	13.132
FTP	3-Bag FTP (weighted)	6.566
FTP	4-Bag FTP (weighted)	6.566
Highway	Highway (HFEDS)	8.947
SC03	SC03	3.455
US06	US06 Total	10.829
US06	US06 City	3.163
US06	US06 Highway	7.666

CE_T determined using the following reference values: ETW = 4000lbs F_0 = 40 F_1 = 0.4 F_2 = 0.02

10Hz target drive traces are available at <http://www.epa.gov/nvfel/testing/dynamometer.htm>

APPENDIX B - EXCEL-BASED CALCULATOR FOR EBDM DATA

An Excel-based calculator is available to perform the EBDM calculations on one or more tests at a time. The calculator operates on input files that contain the data required for the calculations, and produces an output report sheet that can be saved as a separate worksheet. Both the calculator file by contacting William Ott (Ott.William@epamail.epa.gov) at the US Environmental Protection Agency in Ann Arbor, Michigan.

A template for the input files can also be obtained along with the calculator. Otherwise, input files should meet the following criteria:

- Files should be comma separated value (.csv), or Microsoft Excel (.xls, .xlsx, .xlsm) type.
- There should be no embedded images or other data in the file.
- Field locations and formatting for the input parameters and 10Hz drive trace data are shown in Figure B1.
- Cycle ID numbers are defined in Table B1.
- Field locations for the test/vehicle parameters and calculated EBDM drive ratings are shown in Figure B2.

	A	B	C	D	E	F	G	H
1	Test Facility	{test facility}			Time	Cycle ID	V_{ROLL_i}	V_{SCHED_i}
2	Manufacturer	{manufacturer}		10Hz Data-->	{0}	{cycle ID}	[V _{ROLL_1}]	[V _{SCHED_1}]
3	Model	{vehicle model}			{0.1}	{cycle ID}	[V _{ROLL_2}]	[V _{SCHED_2}]
4	Vehicle ID	{vehicle ID}			{0.2}	{cycle ID}	[V _{ROLL_3}]	[V _{SCHED_3}]
5	Veh Configuration	{veh configuration}						
6	Test Date	{test date}						
7	Test Type	{FTP, Highway, etc.}						
8	Test ID	{Test ID}						
9	ETW (lbs)	{xxxx}						
10	F0 (lbs)	{xxx.xx}						
11	F1 (lbs/mph)	{x.xxxx}						
12	F2 (lbs/mph ²)	{0.xxxxx}						
13	Speed Units	{mph or kph}						
14	Regen braking	{Y or N}						
15	{For Cold FTP, F0,F1,F2 are multiplied by 1.1}							
16								
17								
18								
19	Sampled Phase Definitions							
20	Test Type	Test Phase	Cycle ID					
21	FTP/FTP4	FTP/FTP4 Phase 1	1					
22		FTP/FTP4 Phase 2	2					
23		FTP/FTP4 Phase 3	3					
24		FTP4 Phase 4	4					
25	Highway*	Highway (HFEDS)	5					
26	SC03*	SC03	6					
27	US06*	Full Cycle	7					
28		US06 City	8					
29		US06 Highway	9					
30	Cold FTP	Cold FTP Phase 1	10					
31		Cold FTP Phase 2	11					
32		Cold FTP Phase 3	12					
33	for all tests*	Unsampled Phases	0					
34	*Report sampled phases only. Unsampled phases should be removed or identified by Cycle ID = 0							

FIGURE B1 - FILE FORMAT FOR DRIVE TRACE DATA

TABLE B1 - CYCLE ID DEFINITIONS FOR SAMPLED PHASES

Test Type	Test Phase	Cycle ID
FTP/FTP4	FTP/FTP4 Phase 1	1
	FTP/FTP4 Phase 2	2
	FTP/FTP4 Phase 3	3
	FTP4 Phase 4	4
Highway	Highway (HFEDS)	5
SC03	SC03	6
US06	Full Cycle	7
	US06 City	8
	US06 Highway	9
Cold FTP	Cold FTP Phase 1	10
	Cold FTP Phase 2	11
	Cold FTP Phase 3	12
for all tests*	Unsampled Phases	0

NOTE: Un-sampled phases are removed from the 10Hz test data or identified by Cycle ID = 0.

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File Name:	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	AA
20 Worksheet:																											
21 Test Facility:																											
22 Manufacturer:																											
23 Model:																											
24 Vehicle ID:																											
25 Vch Config:																											
26 Test Date:																											
27 Test Type:																											
28 Test ID:																											
29 ETV (lbs):																											
30 F0 (lbs):																											
31 F1 (lbs/imp):																											
32 F2 (lbs/imp):																											
33 Speed Units:																											
34 Regen braking:																											
35																											
36																											
37 File Name:																											
38 Worksheet:																											
39 Test Facility:																											
40 Manufacturer:																											
41 Model:																											
42 Vehicle ID:																											
43 Vch Config:																											
44 Test Date:																											
45 Test Type:																											
46 Test ID:																											
47 ETV (lbs):																											
48 F0 (lbs):																											
49 F1 (lbs/imp):																											
50 F2 (lbs/imp):																											
51 Speed Units:																											
52 Regen braking:																											
53																											
54																											
55 File Name:																											
56 Worksheet:																											
57 Test Facility:																											
58 Manufacturer:																											
59 Model:																											
60 Vehicle ID:																											
61 Vch Config:																											
62 Test Date:																											
63 Test Type:																											
64 Test ID:																											
65 ETV (lbs):																											
66 F0 (lbs):																											
67 F1 (lbs/imp):																											
68 F2 (lbs/imp):																											
69 Speed Units:																											
70 Regen braking:																											
71																											
72																											

FIGURE B2 - FIELD LOCATIONS FOR EBDM DRIVE RATINGS